



# **Geometry Representation**

**Computer Graphics**

**Yu-Ting Wu**

# Outline

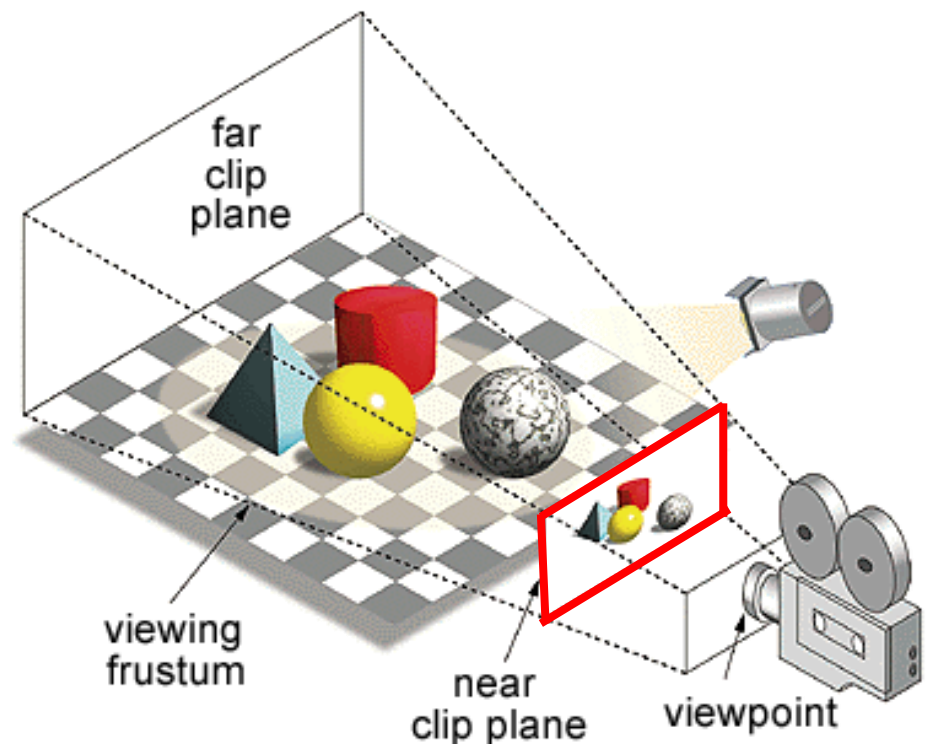
- [Geometric properties and coordinate systems](#)
- [Draw shapes with OpenGL](#)
- [Triangle meshes](#)

# Outline

- **Geometric properties and coordinate systems**
- Draw shapes with OpenGL
- Triangle meshes

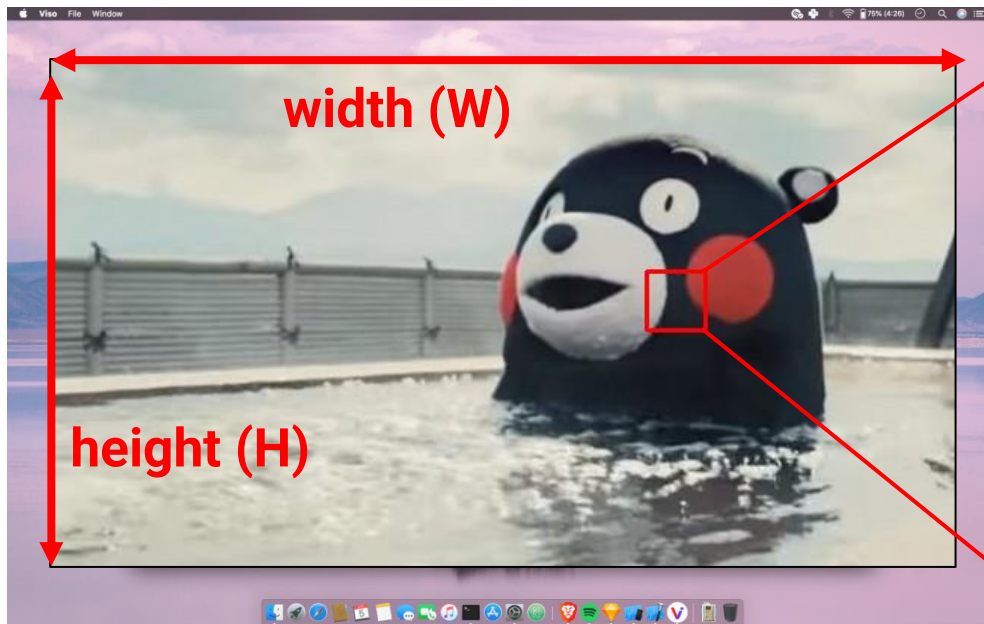
# Rendering Process: 3D to 2D

- In computer graphics, we generate an **image** from a **virtual 3D world**
- We are going to introduce the image representation first



# Pixels

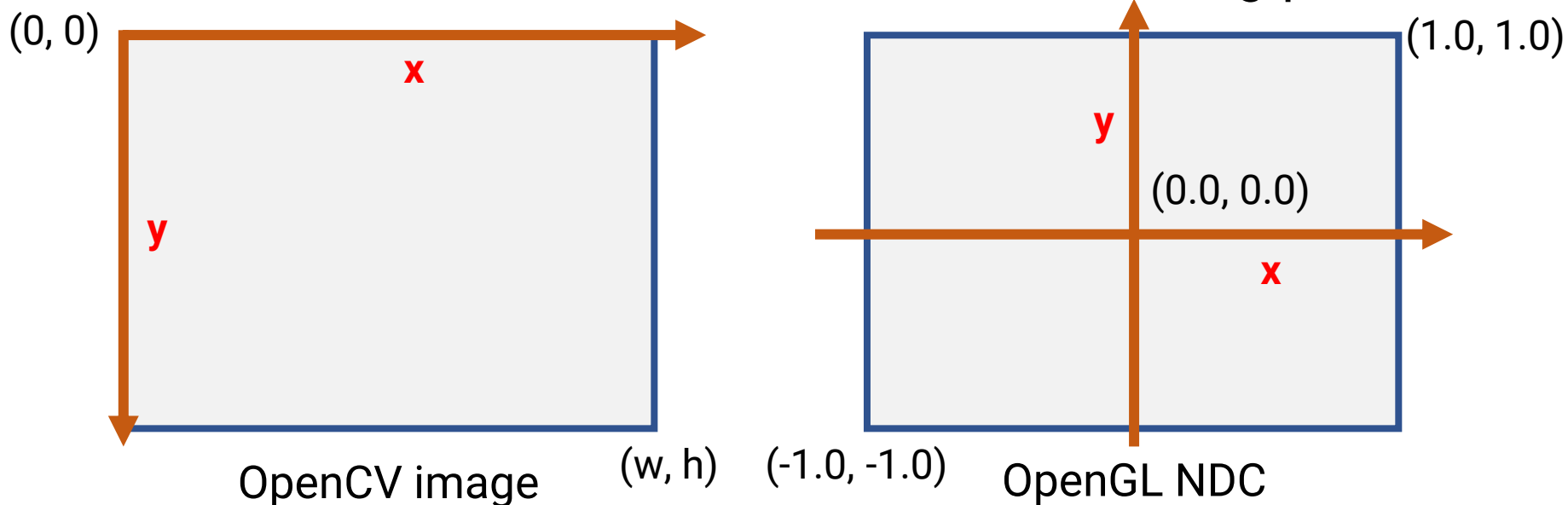
- A 2D image (on a screen) is a **rectangular array of pixels** (small, usually square, dots of color)
  - Merge optically when viewed at a suitable distance to produce the impression of continuous tones



Resolution:  $W \times H$   
(e.g.,  $800 \times 600$ )

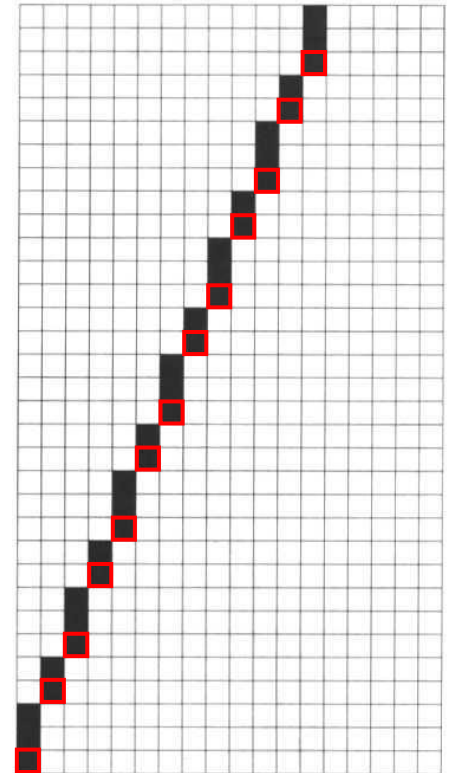
# 2D Coordinate

- Used to identify the position on a 2D surface (e.g., image)
- The coordinate of a 2D image **depends on libraries**
- For an image (or screen), the coordinate is a pair of positive integers
- For other cases, the coordinates can be floating-point



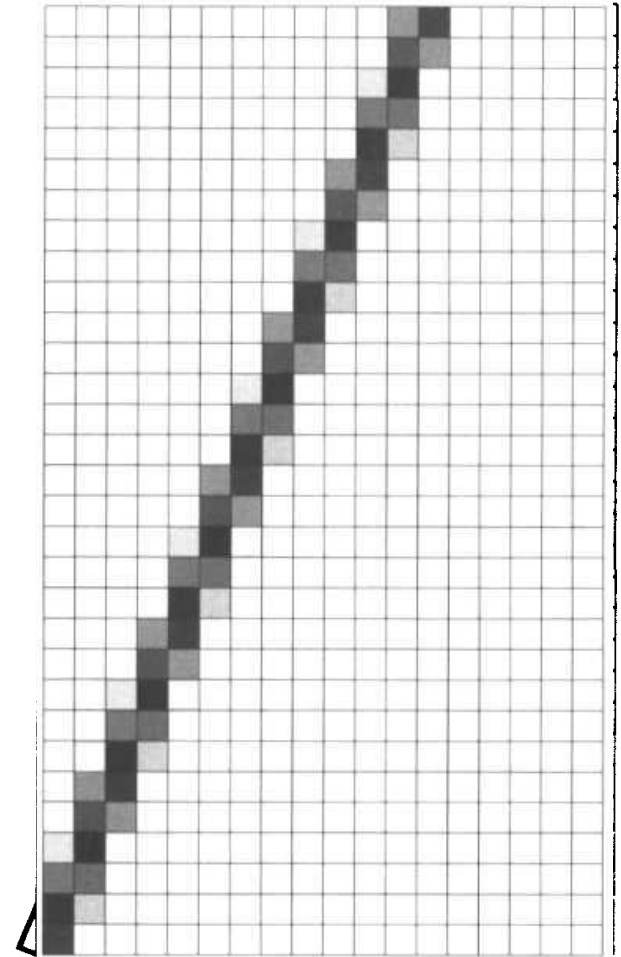
# Rendering of Math (Continuous to Discrete)

- The coordinates of a shape can be floating-point
- However, when the shapes come to the screen and become pixels, they should be **discretized**
- Example:  $y = 5x/2 + 1$   
pass through (0, 1), (1, 4), (2, 6), (3, 9) ...
- Jaggedness is inevitable!
  - Due to the use of a grid of discrete pixels



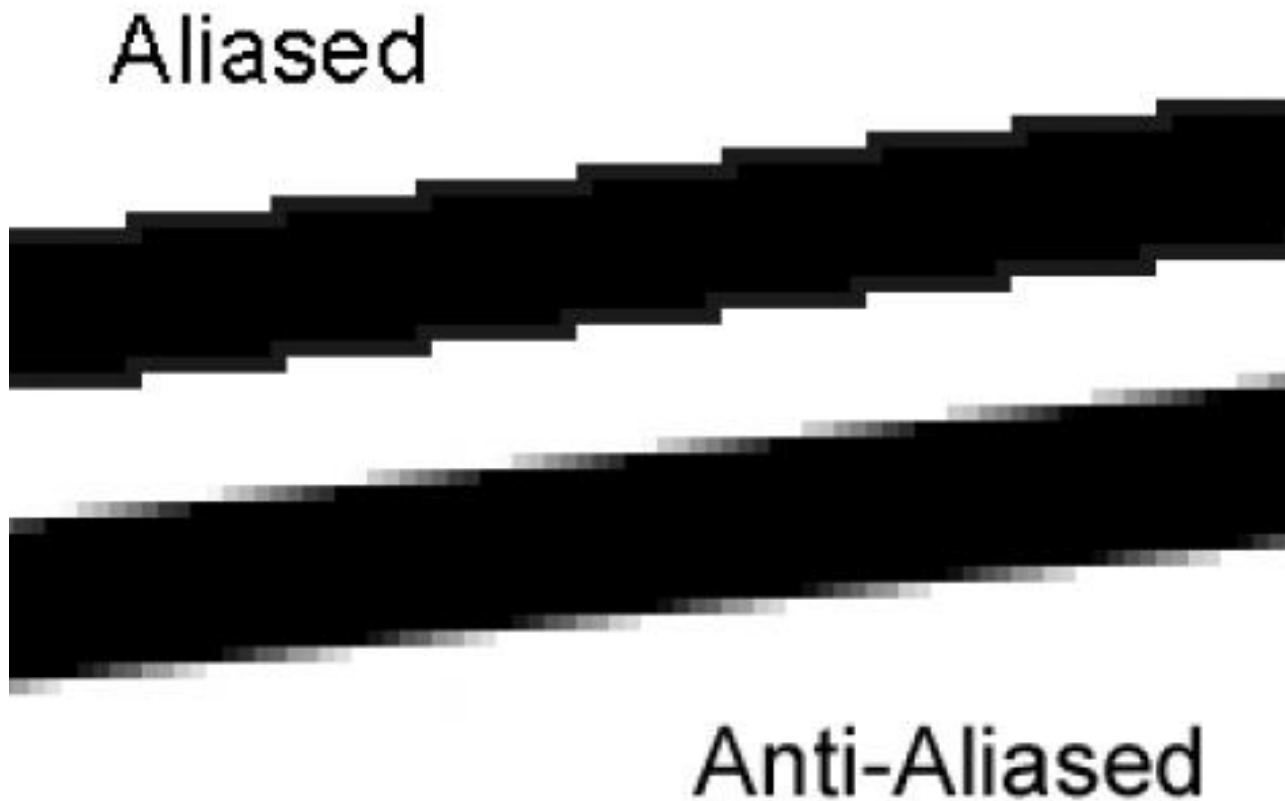
# Anti-aliasing

- Anti-aliasing is a **practical** technique to reduce the jaggies
- Use intermediate grey values
  - In the frequency domain, it relates to reducing the frequency of the signal
- Coloring each pixel in a shade of grey whose **brightness is proportional to the area** of the intersection between the pixels and a “**one-pixel-wide**” line



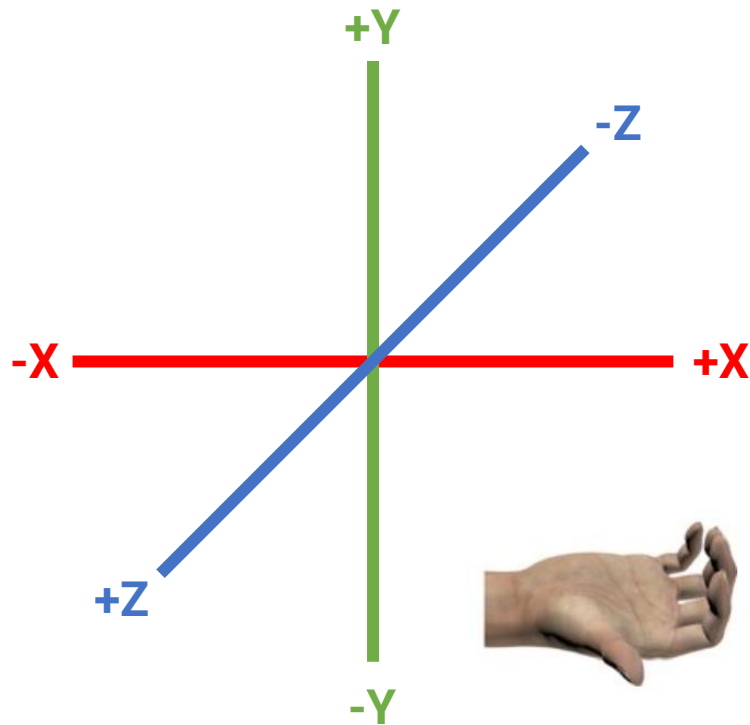


# Anti-aliasing (cont.)

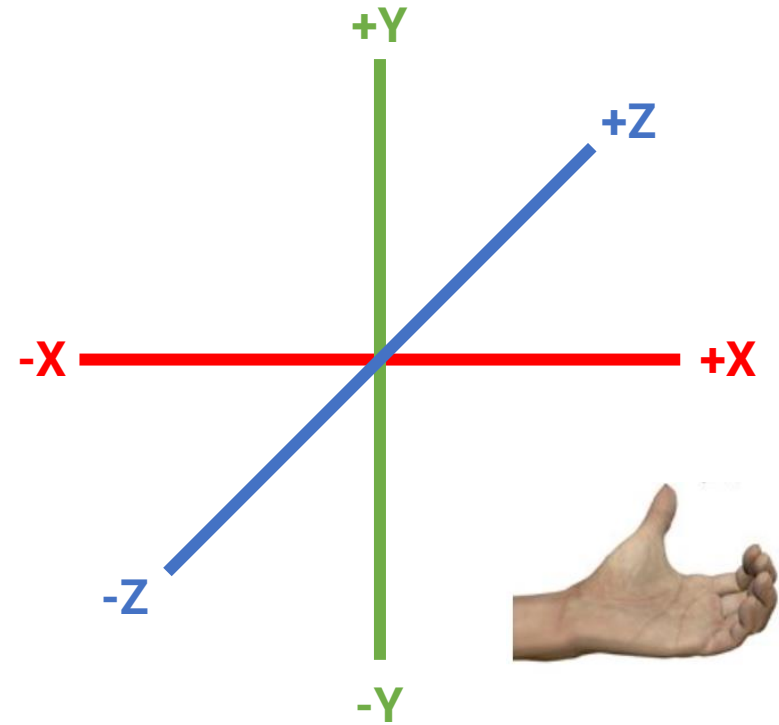


# Description of the 3D World

- 3D coordinate systems



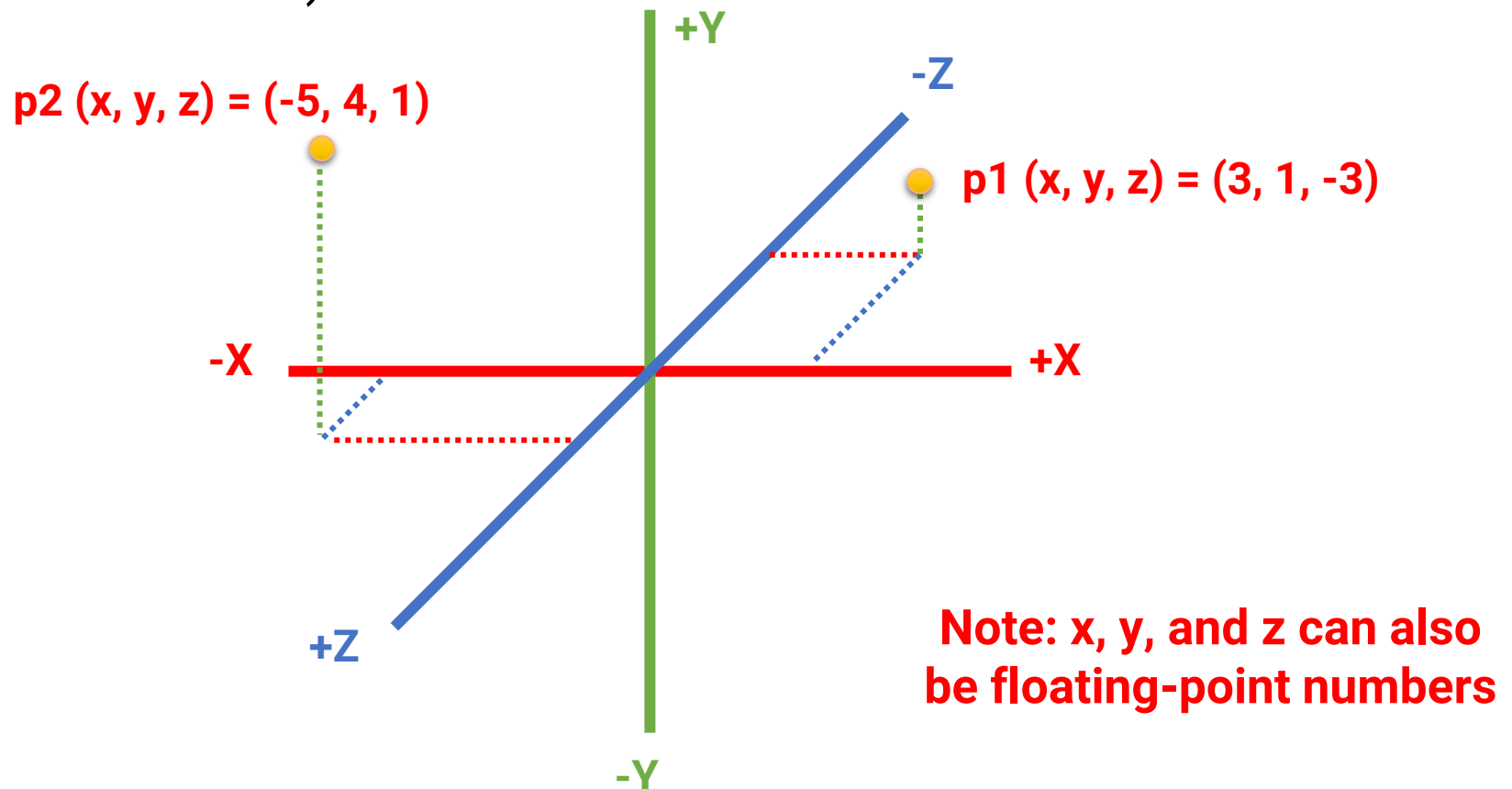
**OpenGL**  
(Right-Hand-Side)



**DirectX**  
(Left-Hand-Side)

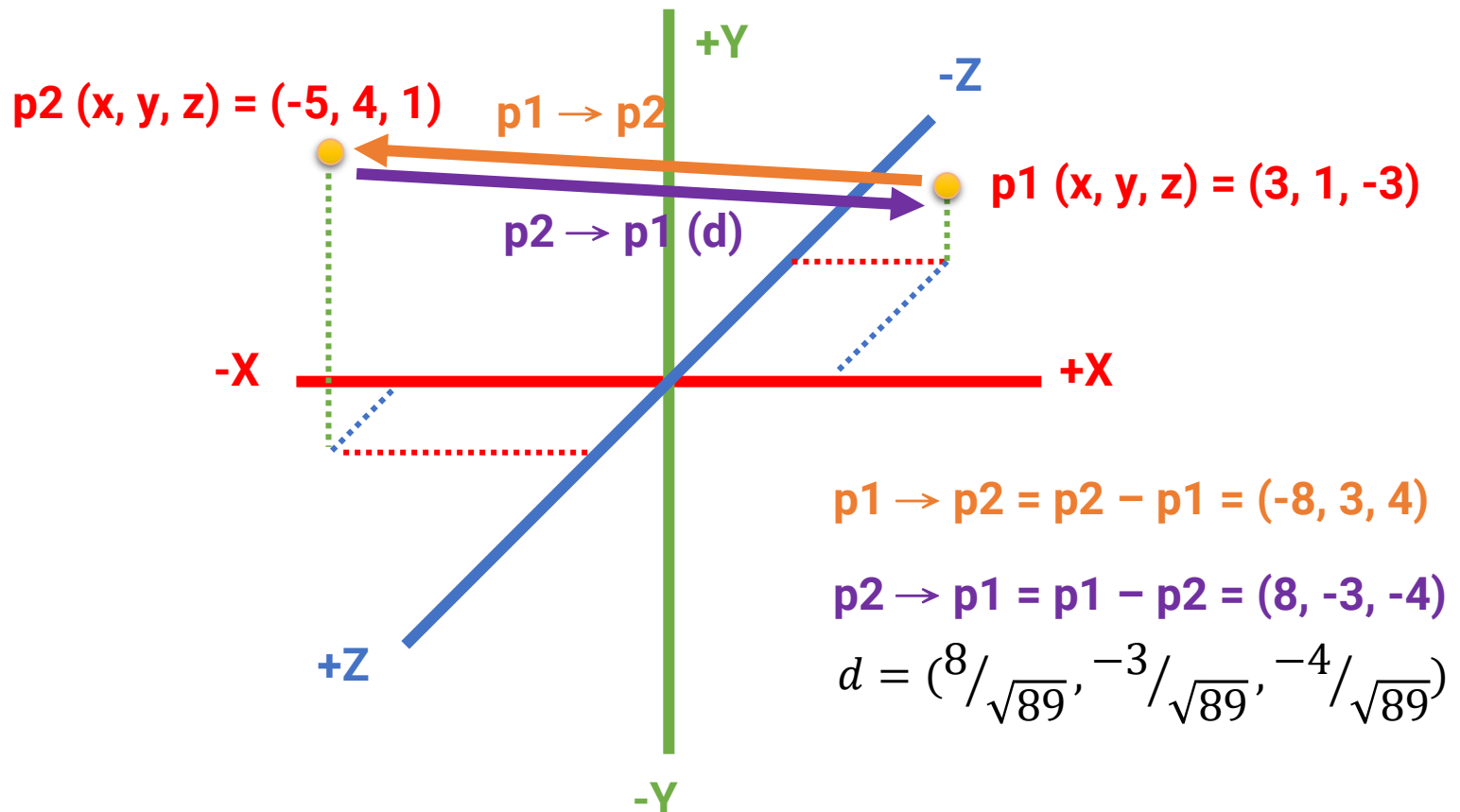
# Points in 3D Space

- Described by a 3D coordinate (the components in x, y, and z axes)



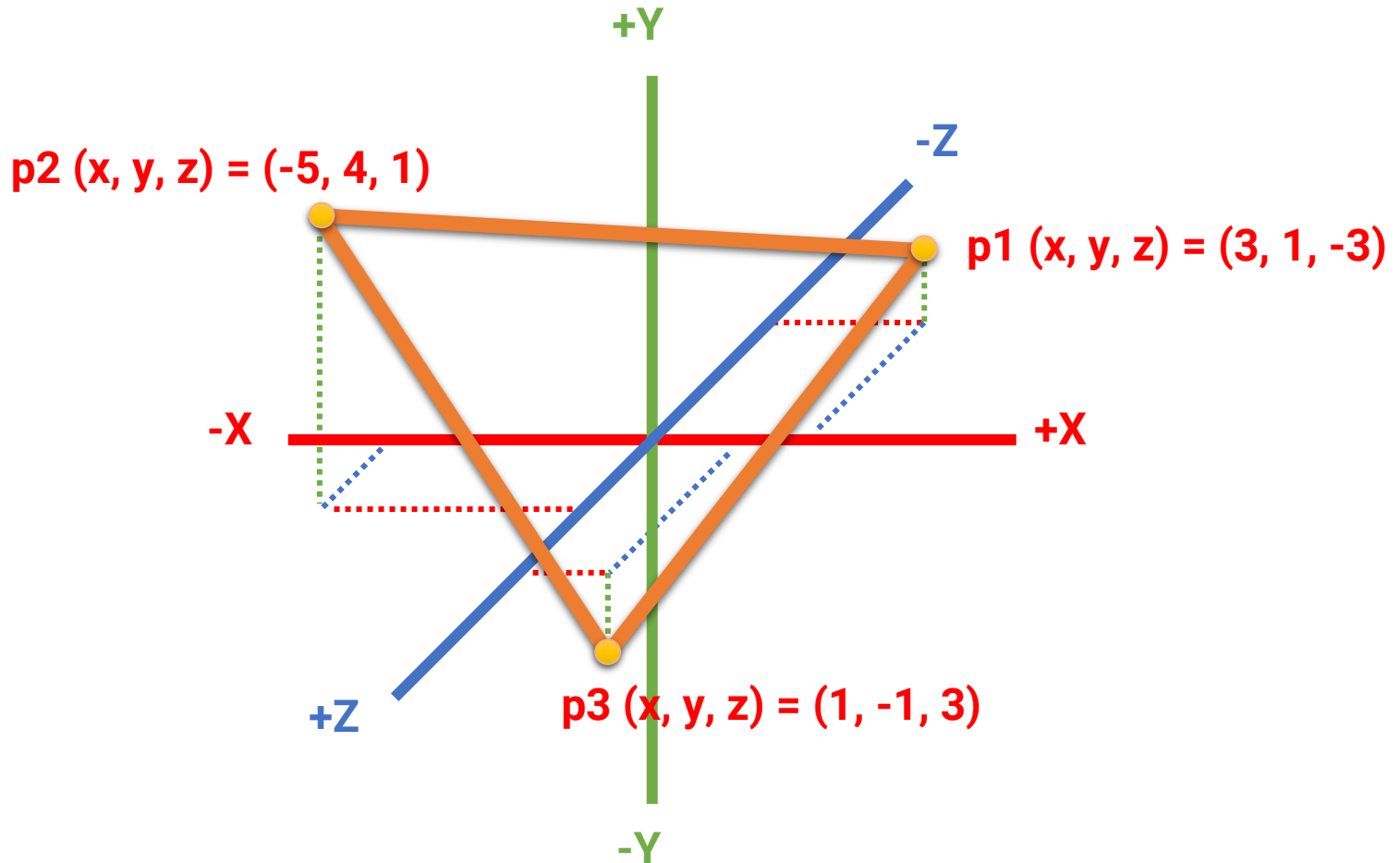
# Vector in 3D Space

- Represent direction (e.g., movement) in the 3D world
- Usually described in a **normalized** version



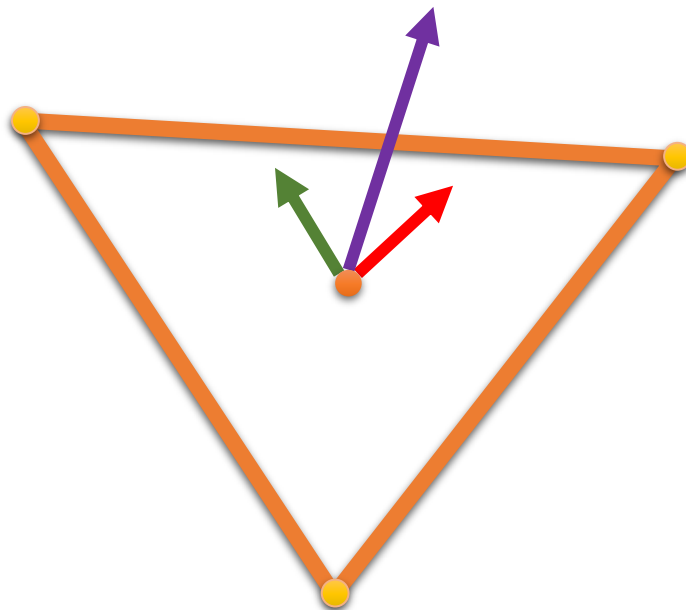
# Triangles in 3D

- Composed of three points as endpoints (called **vertices**)



# 3D Surface Normal

- A **surface normal** is a vector that is **perpendicular** to a surface at a particular position
- Represent the **orientation** of the face
- The length of a normal should be equal to **1**



→ normal ( $n_x, n_y, n_z$ )

→ tangent

→ binormal

# Outline

- Geometric properties and coordinate systems
- **Draw shapes with OpenGL**
- Triangle meshes

# Library for Supporting Drawing

- **GLEW: The OpenGL Extension Wrangler Library ([link](#))**
  - A cross-platform open-source C/C++ extension loading library
  - Provide efficient run-time mechanisms for determining which OpenGL extensions are supported on the target platform
- **GLM: OpenGL Mathematics ([link](#))**
  - A **header-only** C++ mathematics library for graphics software based on the **OpenGL Shading Language (GLSL) specifications**

**Put the library (\*.h, \*.lib, \*.dll) in the project like what we do for FreeGLUT**



# Enable GLEW and Add Init. Functions

```
int main(int argc, char** argv)
{
    // Setting window properties.
    glutInit(&argc, argv);
    glutInitDisplayMode(GLUT_DOUBLE | GLUT_RGBA | GLUT_DEPTH);
    glutInitWindowSize(640, 360);
    glutInitWindowPosition(100, 100);
    glutCreateWindow("OpenGL Renderer");

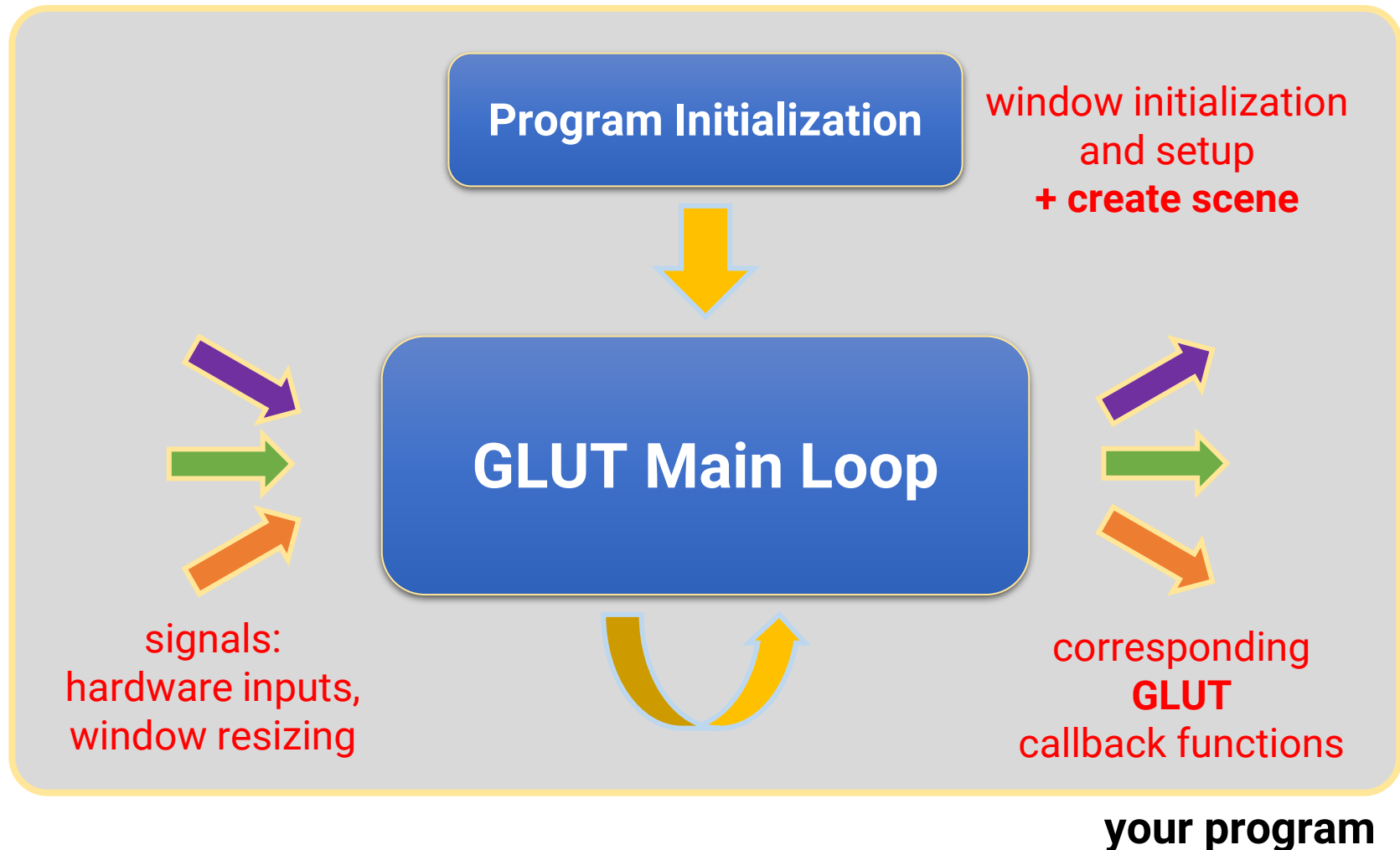
    // Initialize GLEW.
    // Must be done after glut is initialized!
    GLenum res = glewInit();
    if (res != GLEW_OK) {
        std::cerr << "GLEW initialization error: "
                  << glewGetErrorString(res) << std::endl;
        return 1;
    }

    // Initialization.
    SetupRenderState();
    SetupScene();

    // Register callback functions.
    glutDisplayFunc(RenderSceneCB);

    // OpenGL and FreeGlut headers.
    #include <glew.h>
    #include <freeglut.h>
}
```

# Recap: Life Cycle of a GLUT Program



# Draw a Single Point

```
// Global variables.
```

```
GLuint vbo; vertex buffer object
```

```
void SetupScene()
```

```
{
```

```
    // Draw a single point.
```

```
    float VertexPosition[3] = {0.0f, 0.0f, 0.0f};
```

```
    // Generate the vertex buffer.
```

```
    glGenBuffers(1, &vbo);
```

```
    glBindBuffer(GL_ARRAY_BUFFER, vbo);
```

```
    glBufferData(GL_ARRAY_BUFFER, sizeof(VertexPosition), VertexPosition, GL_STATIC_DRAW);
```

```
}
```

**create a vertex buffer and upload vertex data (initialization)**

```
void RenderSceneCB()
```

```
{
```

```
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);
```

```
    // Render a point on screen.
```

```
    glEnableVertexAttribArray(0);
```

```
    glBindBuffer(GL_ARRAY_BUFFER, vbo);
```

```
    glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, sizeof(float)*3, 0);
```

```
    glDrawArrays(GL_POINTS, 0, 1); // # vertices = 1.
```

```
    glDisableVertexAttribArray(0);
```

```
    glutSwapBuffers();
```

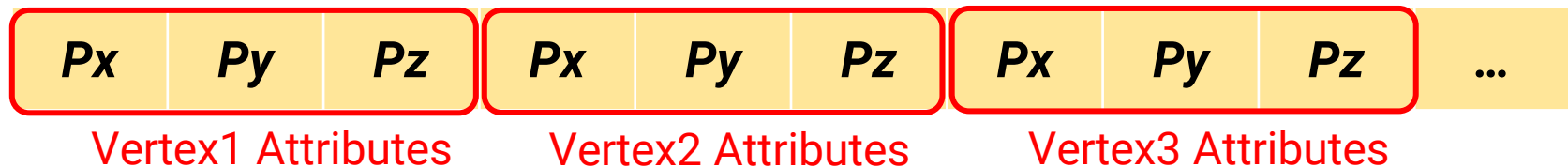
**render shapes with the vertex buffer**

```
}
```

# Vertex Buffer

- A buffer storing the **vertex attribute data**
- Possible vertex attributes include (but are not limited to)
  - **Vertex position**
  - Vertex normal (optional)
  - Texture coordinate (optional)
- Will be passed to GPU for rendering

position-only vertex stream



position-normal vertex stream

Vertex1 Attributes

Vertex2 Attributes

# Vertex Buffer (cont.)

- **Generate a buffer**

- void `glGenBuffers`(GLsizei n, GLuint \* **buffers**);

- **Upload data into the buffer**

- void `glBindBuffer`(GLenum **target** , GLuint **buffer**); [\[Link\]](#)

- void `glBufferData`( [\[Link\]](#)

- GLenum **target** ,
    - GLsizei ptr size ,
    - const void \* data ,
    - GLenum usage );

```
float VertexPosition[3] = {0.0f, 0.0f, 0.0f};
// Generate the vertex buffer.
glGenBuffers(1, &vbo);
glBindBuffer(GL_ARRAY_BUFFER, vbo);
glBufferData(GL_ARRAY_BUFFER, sizeof(VertexPosition), VertexPosition, GL_STATIC_DRAW);
```

# Vertex Buffer (cont.)

## • Render with the vertex buffer

- void `glEnableVertexAttribArray`(GLuint `index`);
- void `glVertexAttribPointer`(
  - GLuint `index`, The index of the attribute  
E.g., 0 for position, 1 for normal, etc.
  - GLint `size`, Number of components of the attribute
  - GLenum `type`, Type of the attribute component
  - GLboolean `normalized`,
  - GLsizei `stride`, The byte offset to the same attribute  
of the next vertex
  - const void \* `pointer` The byte offset of the first component

```
glEnableVertexAttribArray(0);
glBindBuffer(GL_ARRAY_BUFFER, vbo);
glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, sizeof(float)*3, 0);
```

# Vertex Buffer (cont.)

- void `glVertexAttribPointer`(

...

GLsizei `stride` , The byte offset to the same attribute  
of the next vertex

const void \* `pointer`

The byte offset of the first component

);

position-only vertex stream



position offset = 0      position stride =  $4 \cdot 3$

position-normal vertex stream



position offset = 0      normal offset =  $4 \cdot 3$       position stride = normal stride =  $4 \cdot 6$

# Vertex Buffer (cont.)

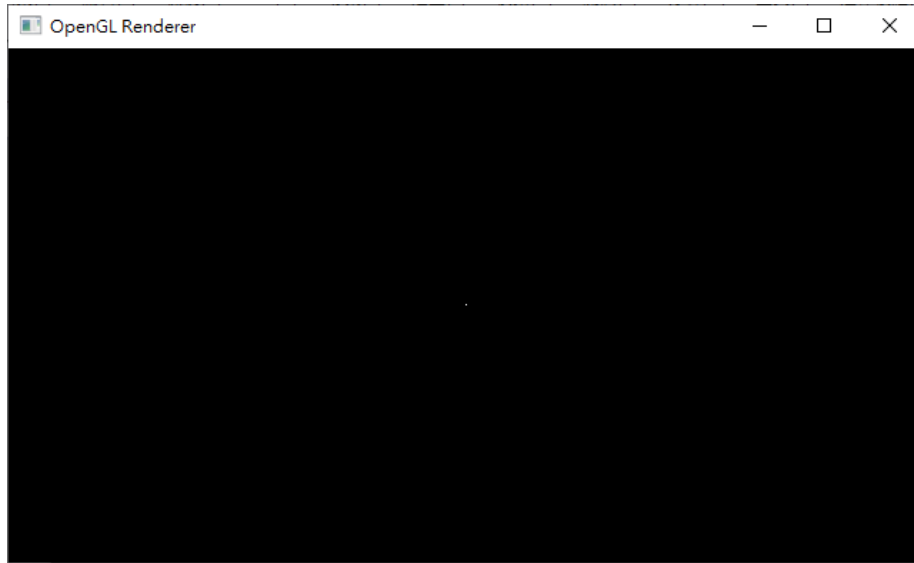
- void **glDrawArrays**(
  - GLenum **mode**, — The type of the primitive  
E.g., GL\_POINTS, GL\_LINE\_LOOP,  
GL\_TRIANGLES, etc.
  - GLint **first**, — The start index
  - GLsizei **count** — The number of **indices** to be rendered
- void **glDisableVertexAttribArray**(GLuint index );

```
// Render a point on screen.
glEnableVertexAttribArray(0);
glBindBuffer(GL_ARRAY_BUFFER, vbo);
glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, sizeof(float)*3, 0);
glDrawArrays(GL_POINTS, 0, 1); // # vertices = 1.
glDisableVertexAttribArray(0);
```

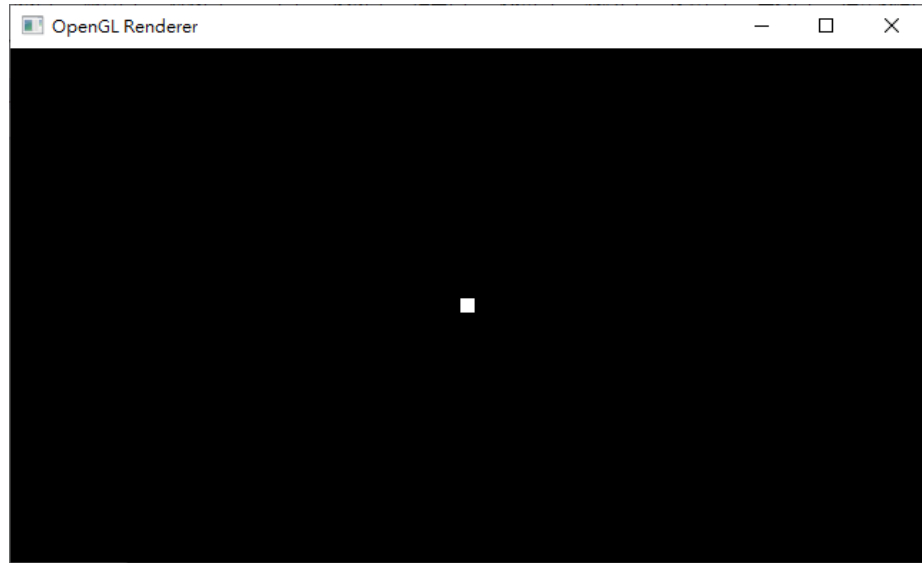


# Change the Point Size

- void **glPointSize**(GLfloat size)

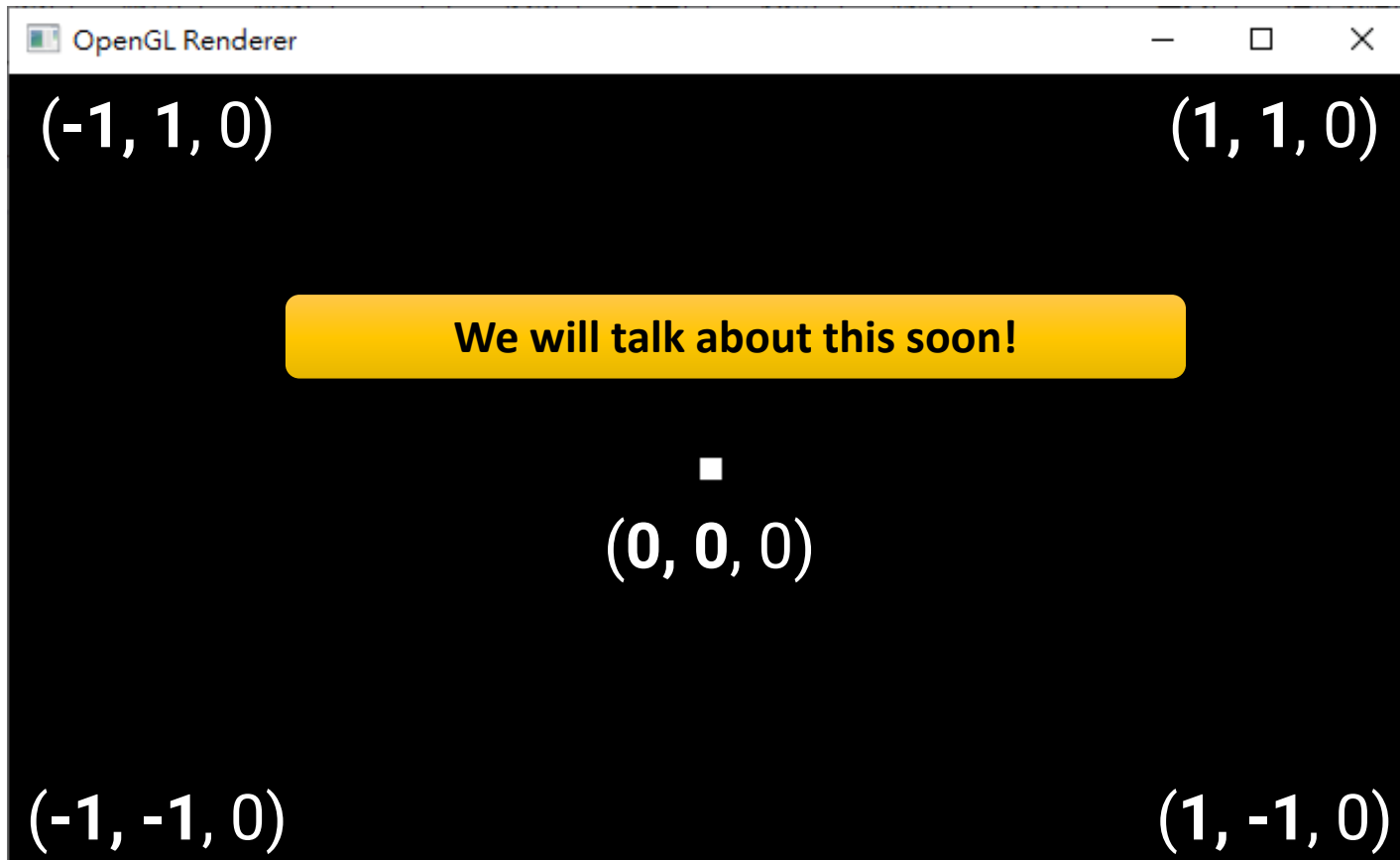


```
void SetupRenderState()  
{  
    // Default.  
    glPointSize(1);  
}
```



```
void SetupRenderState()  
{  
    glPointSize(10);  
}
```

# Insight: Coordinate (Recall)



What about the z coordinate? You can find the point will only be visible if its z value is within  **$[-1, 1]$**

# Draw a Circle (Ellipse)

```

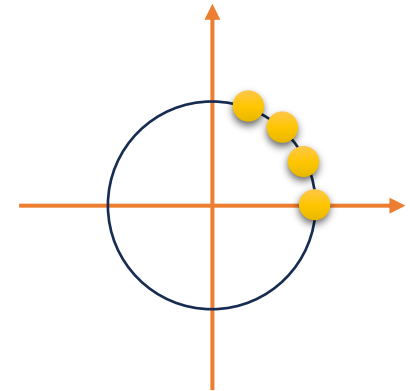
// C++ STL headers.
#include <iostream>
#include <vector>
#define _USE_MATH_DEFINES
#include <math.h>

// Global variables.
GLuint vbo;
const int numCircleSamples = 36;

void SetupScene()
{
    // Draw a circle.
    float VertexPosition[numCircleSamples * 3];
    const float thetaOffset = 2.0f * M_PI / (float)numCircleSamples;
    float startTheta = 0.0f;
    float r = 0.5f;
    for (int i = 0; i < numCircleSamples; ++i) {
        float theta = startTheta + i * thetaOffset;
        VertexPosition[3 * i + 0] = r * std::cos(theta); // x.
        VertexPosition[3 * i + 1] = r * std::sin(theta); // y.
        VertexPosition[3 * i + 2] = 0.0f; // z.
    }

    // Generate the vertex buffer.
    glGenBuffers(1, &vbo);
    glBindBuffer(GL_ARRAY_BUFFER, vbo);
    glBufferData(GL_ARRAY_BUFFER, sizeof(VertexPosition), VertexPosition, GL_STATIC_DRAW);
}

```



# Draw a Circle (Ellipse)

```

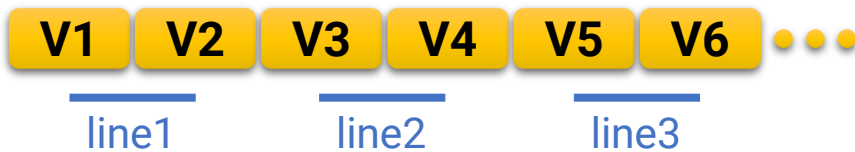
void RenderSceneCB()
{
    glClearColor(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);

    // Render a point on screen.
    glEnableVertexAttribArray(0);
    glBindBuffer(GL_ARRAY_BUFFER, vbo);
    glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, sizeof(float)*3, 0);
    glDrawArrays(GL_LINE_LOOP, 0, numCircleSamples);
    glDisableVertexAttribArray(0);

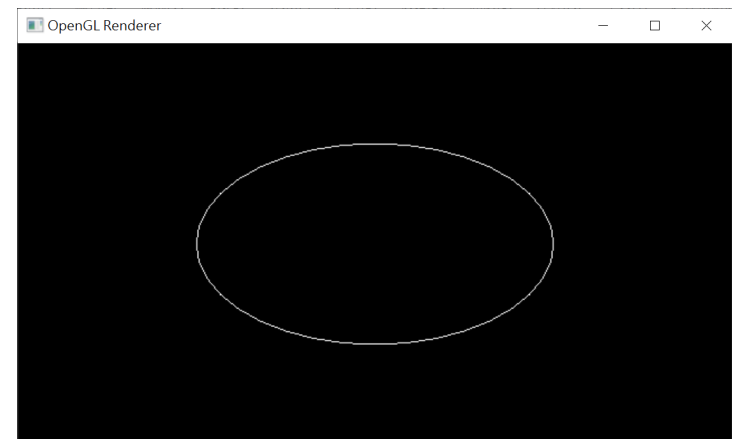
    glutSwapBuffers();
}

```

GL\_LINES

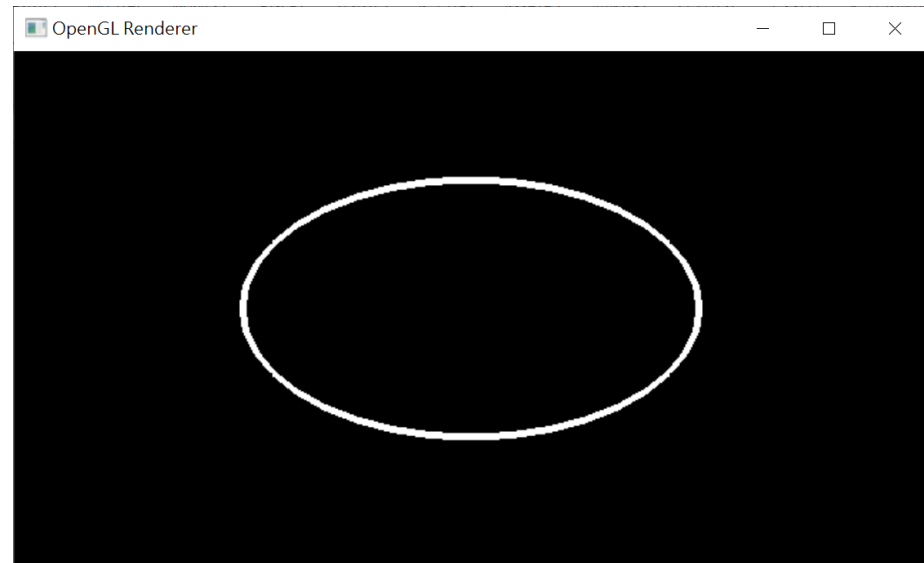
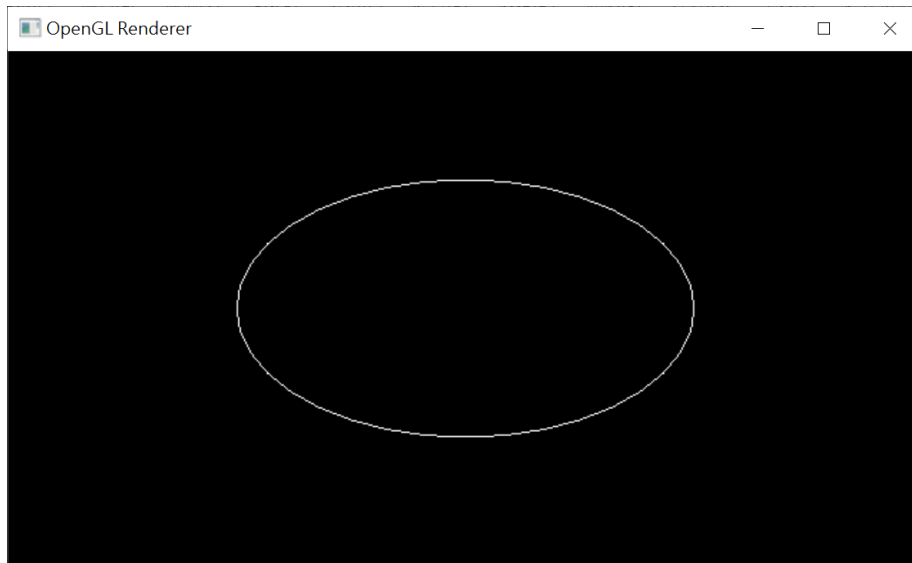


GL\_LINE\_LOOP



# Change the Line Width

- `void glLineWidth(GLfloat width)`



```
void SetupRenderState()  
{  
    ...  
    glLineWidth(5);  
}
```

# The GLM Library

- In computer graphics, we need a data structure to store and manipulate **multi-dimensional data**, such as position, normal, texture coordinate, and color
- The GLM library provides an elegant way to process multi-dimensional data
  - Support **operator overloading**
  - Match the syntax of OpenGL shading language (GLSL)
  - Support **alias** of components
    - For position or normal, we used to use  $(x, y, z, w)$
    - For texture coordinate, we used to use  $(u, v, s, t)$
    - For color, we used to use  $(r, g, b, a)$

# The GLM Library Examples

- The most common data types are three/four-dimensional vectors and four-by-four matrices
- Example: compute the average direction of three vectors

```
glm::vec3 dir1 = glm::vec3(1.0f, 0.0f, 0.0f);  
glm::vec3 dir2 = glm::vec3(0.0f, 1.0f, 0.0f);  
glm::vec3 dir3 = glm::vec3(0.0f, 0.0f, 1.0f);  
glm::vec3 avgDir = (dir1 + dir2 + dir3) / 3.0f;
```

# Draw a Triangle

```
void SetupScene()
{
    // Draw a triangle.
    glm::vec3 VertexPosition[3];
    VertexPosition[0] = glm::vec3(-1.0f, -1.0f, 0.0f);
    VertexPosition[1] = glm::vec3( 0.0f,  1.0f, 0.0f);
    VertexPosition[2] = glm::vec3( 1.0f, -1.0f, 0.0f);

    // Generate the vertex buffer.
    glGenBuffers(1, &vbo);
    glBindBuffer(GL_ARRAY_BUFFER, vbo);
    glBufferData(GL_ARRAY_BUFFER, sizeof(VertexPosition), VertexPosition, GL_STATIC_DRAW);
}

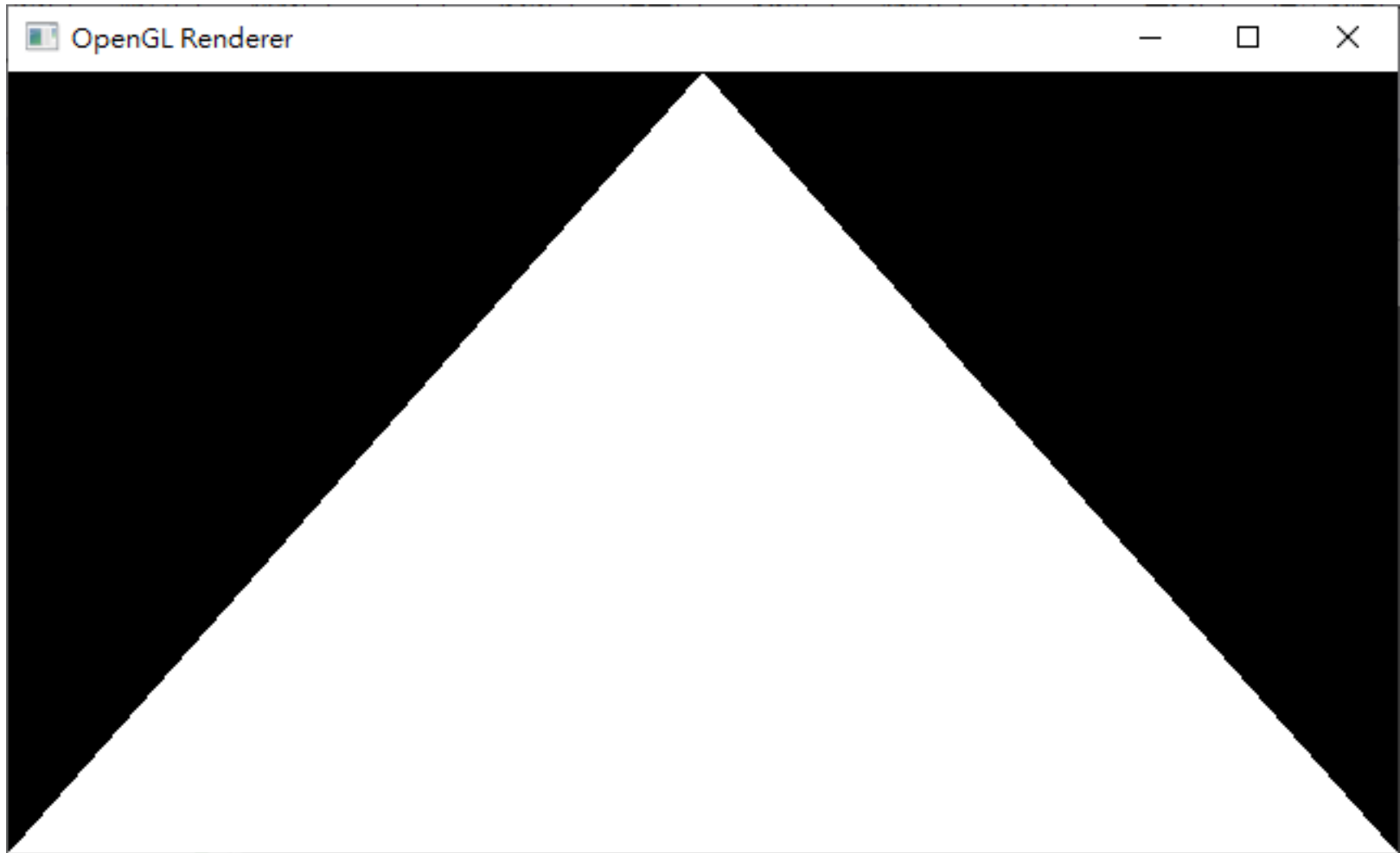
void RenderSceneCB()
{
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT);

    // Render a point on screen.
    glEnableVertexAttribArray(0);
    glBindBuffer(GL_ARRAY_BUFFER, vbo);
    glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, sizeof(glm::vec3), 0);
    glDrawArrays(GL_TRIANGLES, 0, 3);
    glDisableVertexAttribArray(0);

    glutSwapBuffers();
}
```



# Draw a Triangle (cont.)



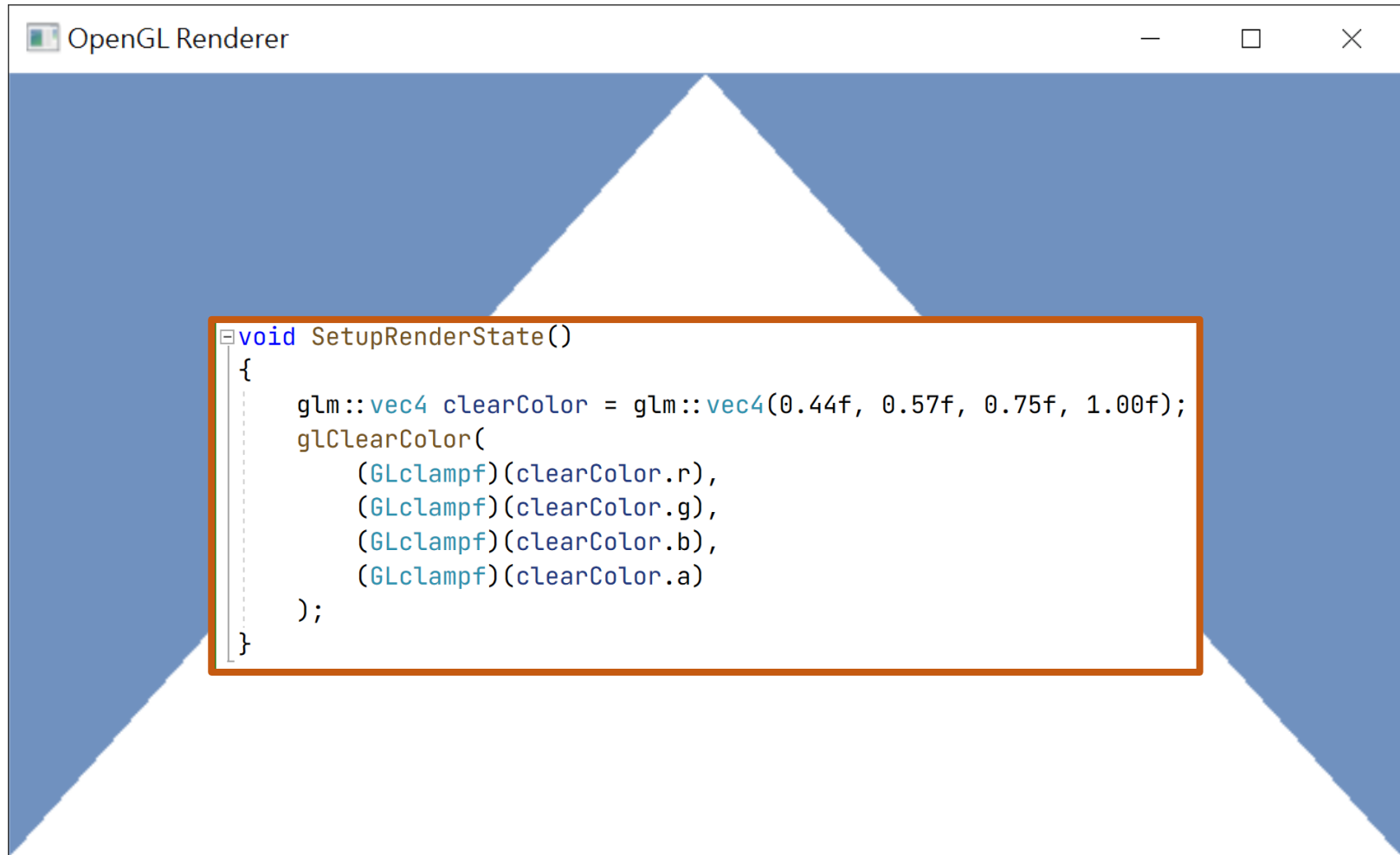
# Avoid Deprecated APIs

- You may find online tutorials that use the following APIs:

```
glBegin(GL_POINTS/GL_LINES/GL_TRIANGLES);  
    glVertex3f(...);  
    glVertex3f(...);  
    glVertex3f(...);  
glEnd();
```

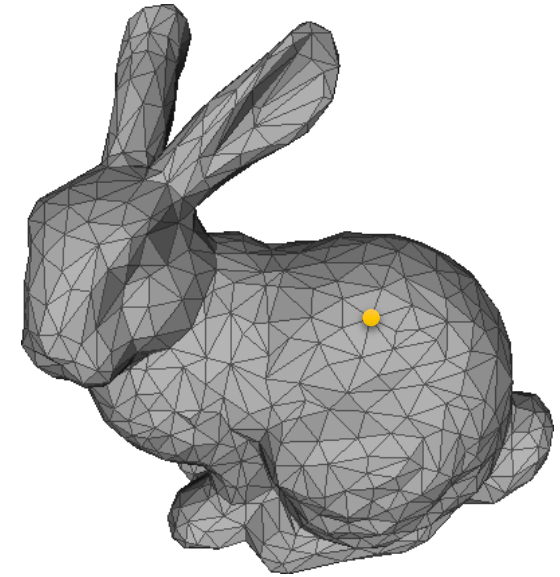
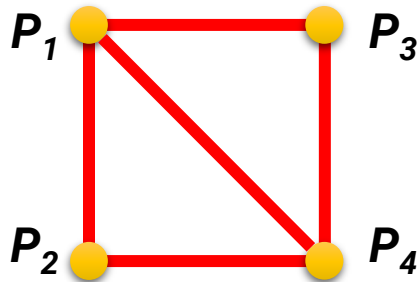
- Although it seems convenient, do **NOT** use it
- These APIs have been deprecated since OpenGL 3.2 due to the performance issue

# GLM Vector for Representing Color

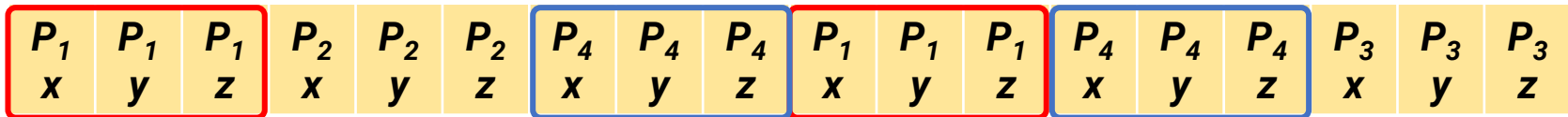


# Index Buffer

- Lots of the vertices are shared when drawing triangle mesh with multiple triangles
- E.g., a quad with 2 triangles



## Vertex Buffer



Using **glDrawArrays** will need 6 vertices in the vertex buffer

# Index Buffer (cont.)

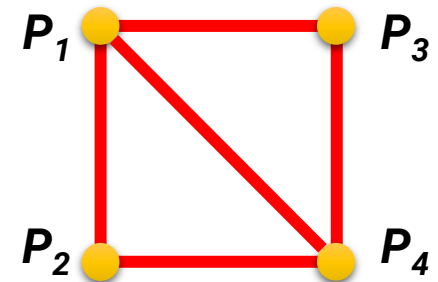
- Lots of the vertices are shared when drawing triangle mesh with multiple triangles
- **We can use an index buffer to identify the vertex defined in the vertex buffer**
- E.g., a quad with 2 triangles

## Vertex Buffer

$P_1$	$P_1$	$P_1$	$P_2$	$P_2$	$P_2$	$P_3$	$P_3$	$P_3$	$P_4$	$P_4$	$P_4$
$x$	$y$	$z$	$x$	$y$	$z$	$x$	$y$	$z$	$x$	$y$	$z$

## Index Buffer

1	2	4	1	4	3
---	---	---	---	---	---



**Now we need only 4 vertices and an integer array (save lots of memory when the vertex has many attributes)**

# Index Buffer

- **Generate a buffer and upload data**
  - Use the same functions as we create the vertex buffer, but with different parameters

```
// Draw a quad with indexed triangles.
glm::vec3 vertexPosition[4];
vertexPosition[0] = glm::vec3(-0.8f, 0.8f, 0.0f);
vertexPosition[1] = glm::vec3(-0.8f, -0.8f, 0.0f);
vertexPosition[2] = glm::vec3(0.8f, 0.8f, 0.0f);
vertexPosition[3] = glm::vec3(0.8f, -0.8f, 0.0f);
// Generate the vertex buffer.
glGenBuffers(1, &vbo);
glBindBuffer(GL_ARRAY_BUFFER, vbo);
glBufferData(GL_ARRAY_BUFFER, sizeof(vertexPosition), vertexPosition, GL_STATIC_DRAW);

unsigned int vertexIndices[6] = { 0, 1, 3, 0, 3, 2 };
// Generate the index buffer.
glGenBuffers(1, &ibo);
glBindBuffer(GL_ELEMENT_ARRAY_BUFFER, ibo);
glBufferData(GL_ELEMENT_ARRAY_BUFFER, sizeof(vertexIndices), vertexIndices, GL_STATIC_DRAW);
```

# Index Buffer (cont.)

- Render with the vertex buffer and index buffer

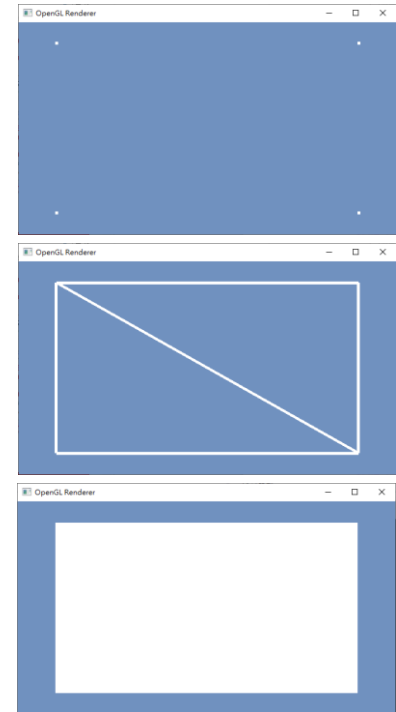
```
// Render a quad on screen.  
glEnableVertexAttribArray(0);  
glBindBuffer(GL_ARRAY_BUFFER, vbo);  
glVertexAttribPointer(0, 3, GL_FLOAT, GL_FALSE, sizeof(glm::vec3), 0);  
glBindBuffer(GL_ELEMENT_ARRAY_BUFFER, ibo);  
glDrawElements(GL_TRIANGLES, 6, GL_UNSIGNED_INT, 0);  
glDisableVertexAttribArray(0);
```



# Change Polygon Render Mode

- OpenGL provides API for changing polygon render mode
  - void **glPolygonMode**(GLenum face, GLenum mode);

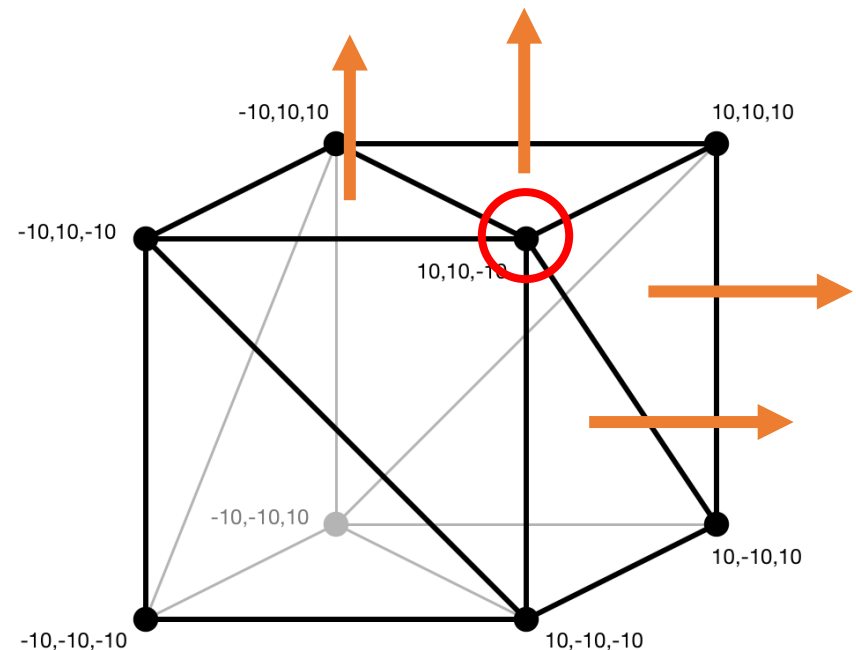
```
void ProcessSpecialKeysCB(int key, int x, int y)
{
    // Handle special (functional) keyboard inputs such as F1, spacebar, page up, etc.
    switch (key) {
    case GLUT_KEY_F1:
        // Render with point mode.
        glPointSize(5);
        glPolygonMode(GL_FRONT_AND_BACK, GL_POINT);
        break;
    case GLUT_KEY_F2:
        // Render with line mode.
        glLineWidth(5);
        glPolygonMode(GL_FRONT_AND_BACK, GL_LINE);
        break;
    case GLUT_KEY_F3:
        // Render with fill mode.
        glPolygonMode(GL_FRONT_AND_BACK, GL_FILL);
        break;
    default:
        break;
    }
}
```





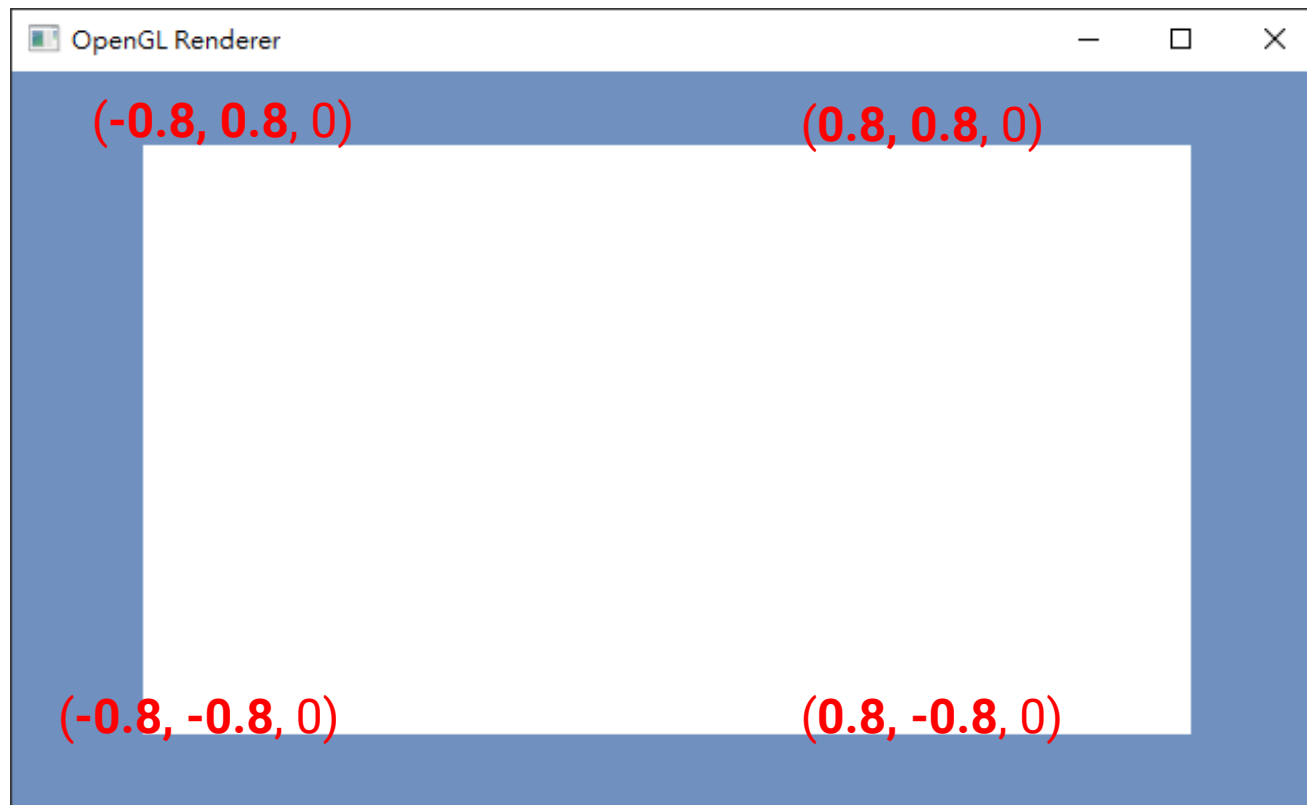
# Pitfalls of Using Index Buffer

- Sometimes vertices will share the same positions but different other attributes such as **vertex normal** and **texture coordinate**
- These vertices should be stored **individually**



# Question

- A rectangle? Why not a square? (we will answer later)



# Take Home Assignments

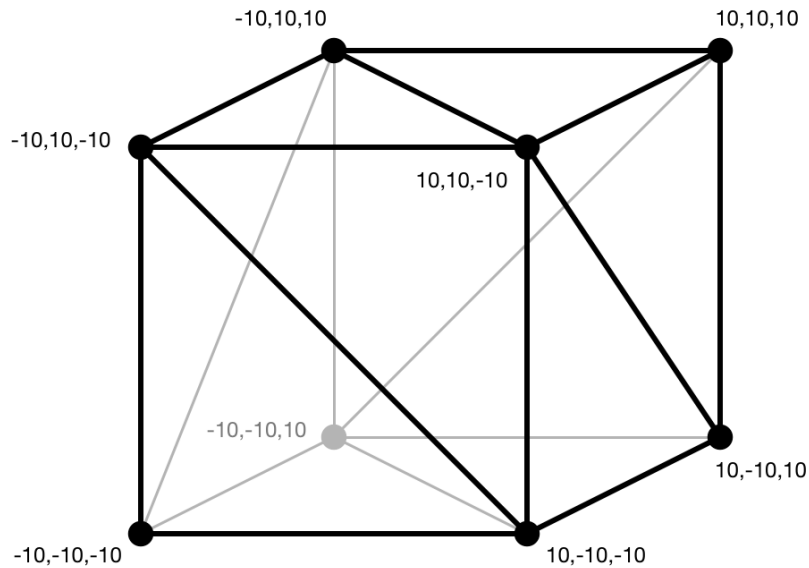
- Try to create some 3D shapes, e.g., cube, sphere ...
  - Practice to create the vertex data
  - Practice to create a vertex buffer
  - Practice to render with a vertex buffer
  - Practice to render with a vertex and index buffer

# Outline

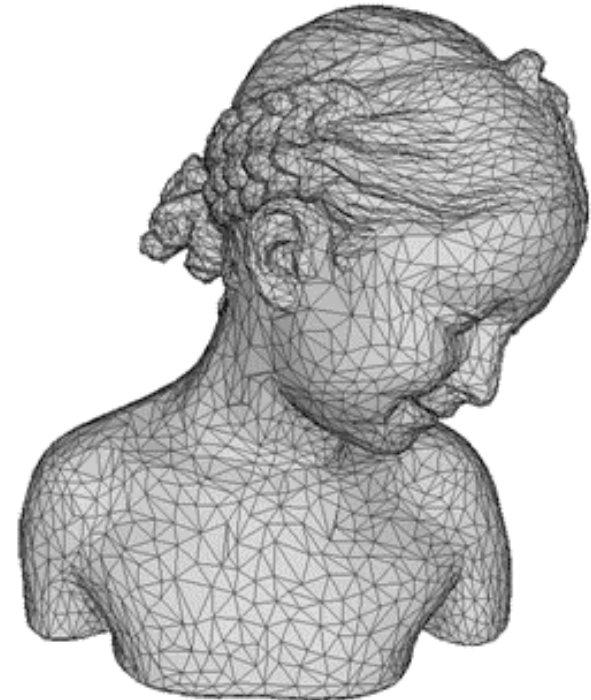
- Geometric properties and coordinate systems
- Draw shapes with OpenGL
- **Triangle meshes**

# Triangle Mesh

- We can define the geometry of an object by specifying the coordinates of the **vertices** and **their adjacencies**



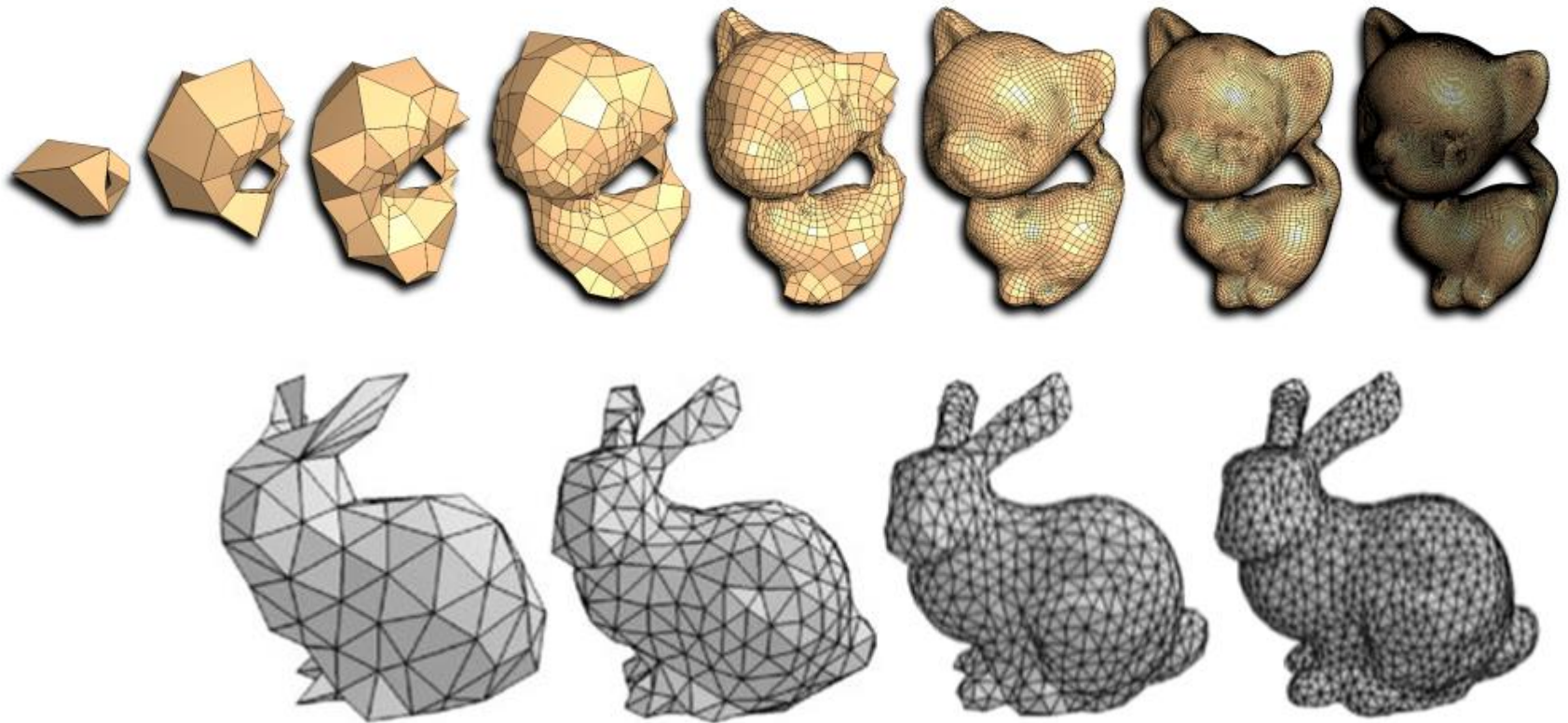
12 triangles



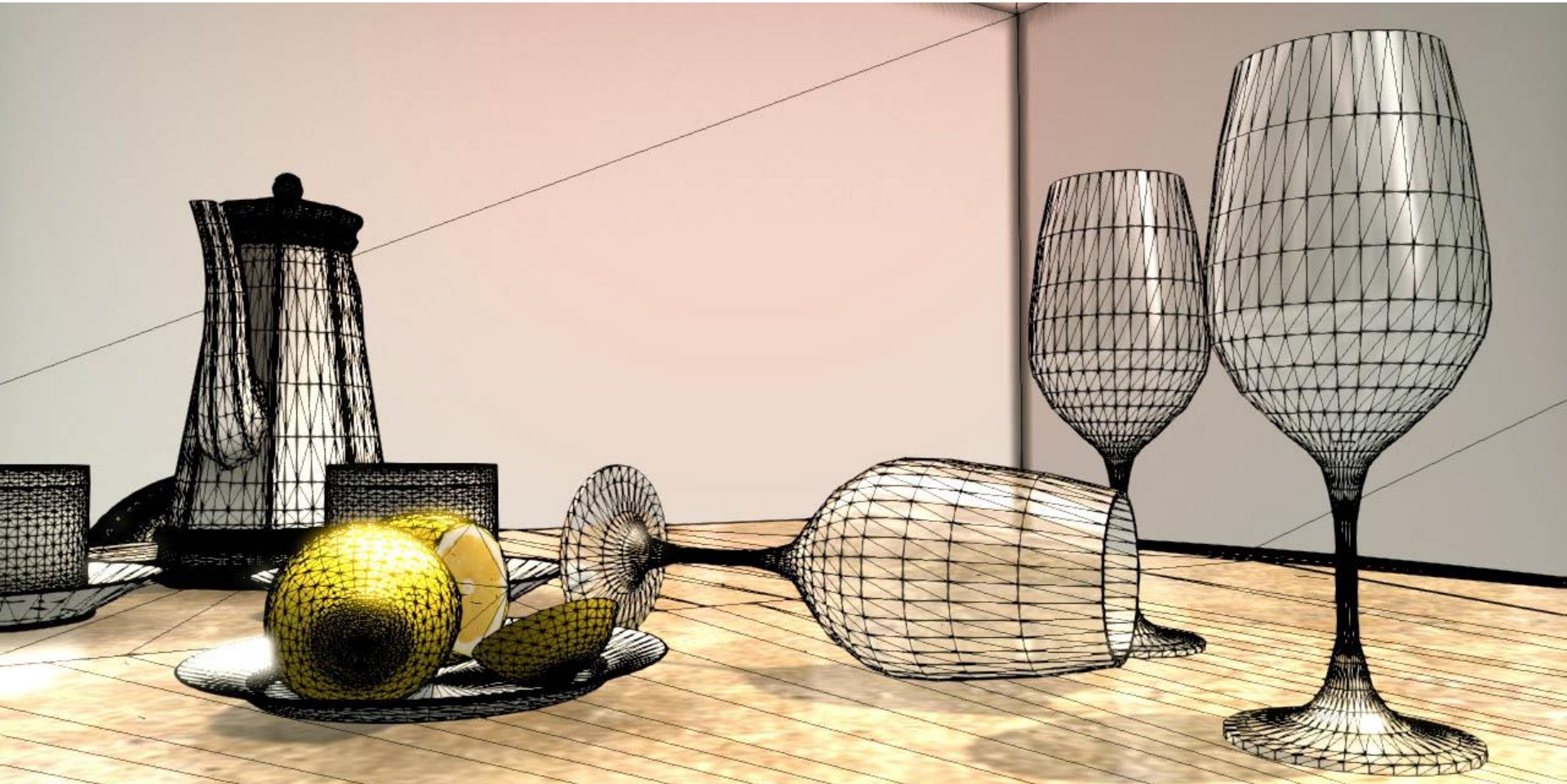
10K triangles

# Triangle Mesh (cont.)

- Using more triangles can lead to higher-quality meshes
  - However, takes more time to render

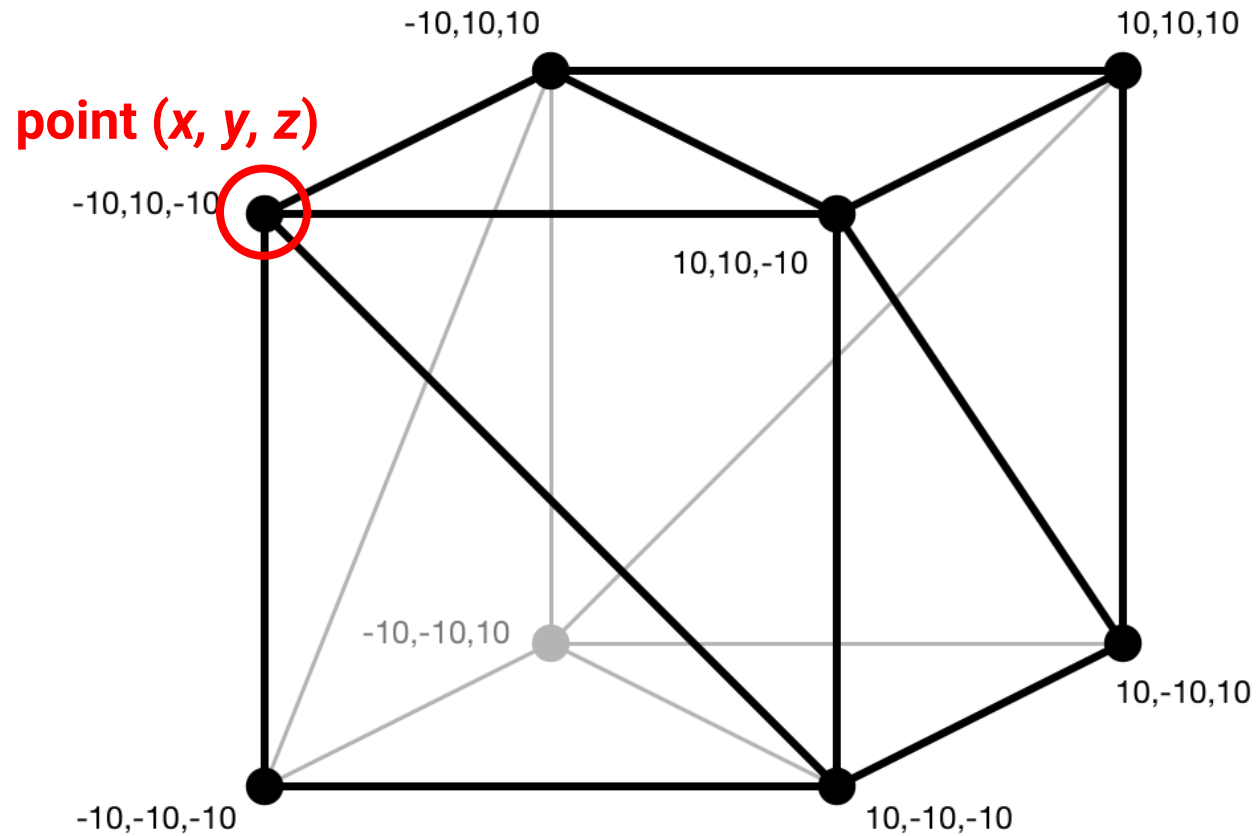


# Scene Built with Triangle Mesh



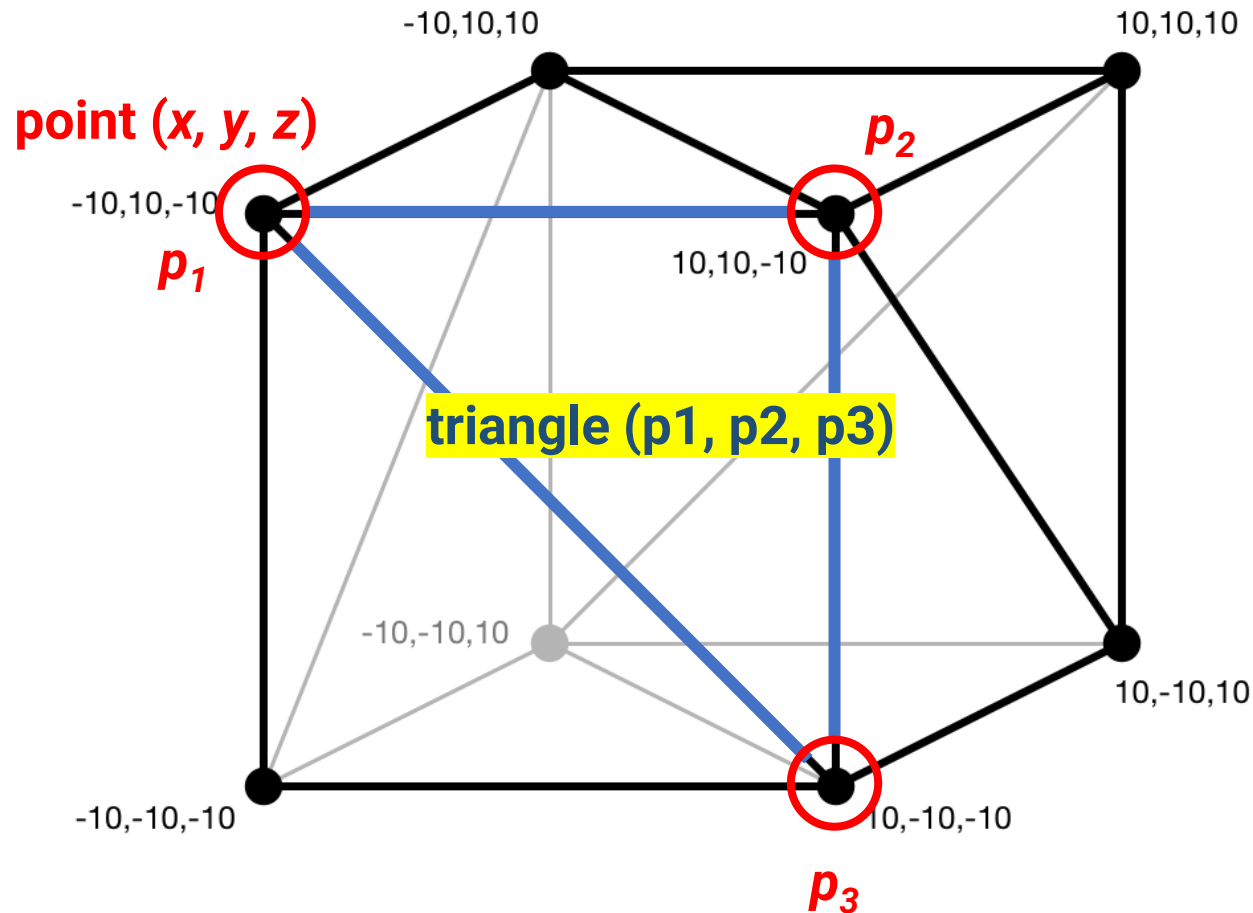


# Point, Triangle, and Surface Normal

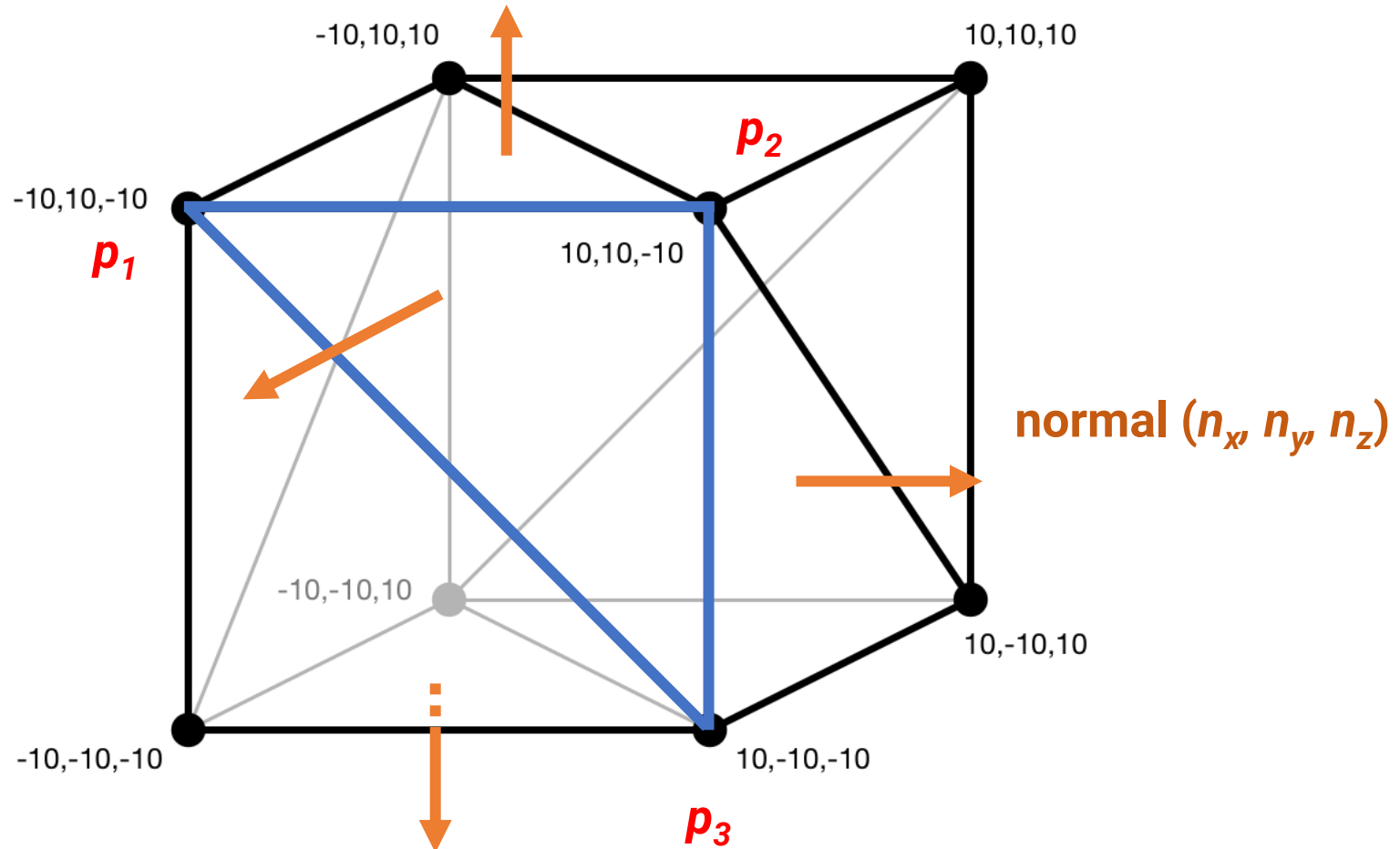




# Point, Triangle, and Surface Normal

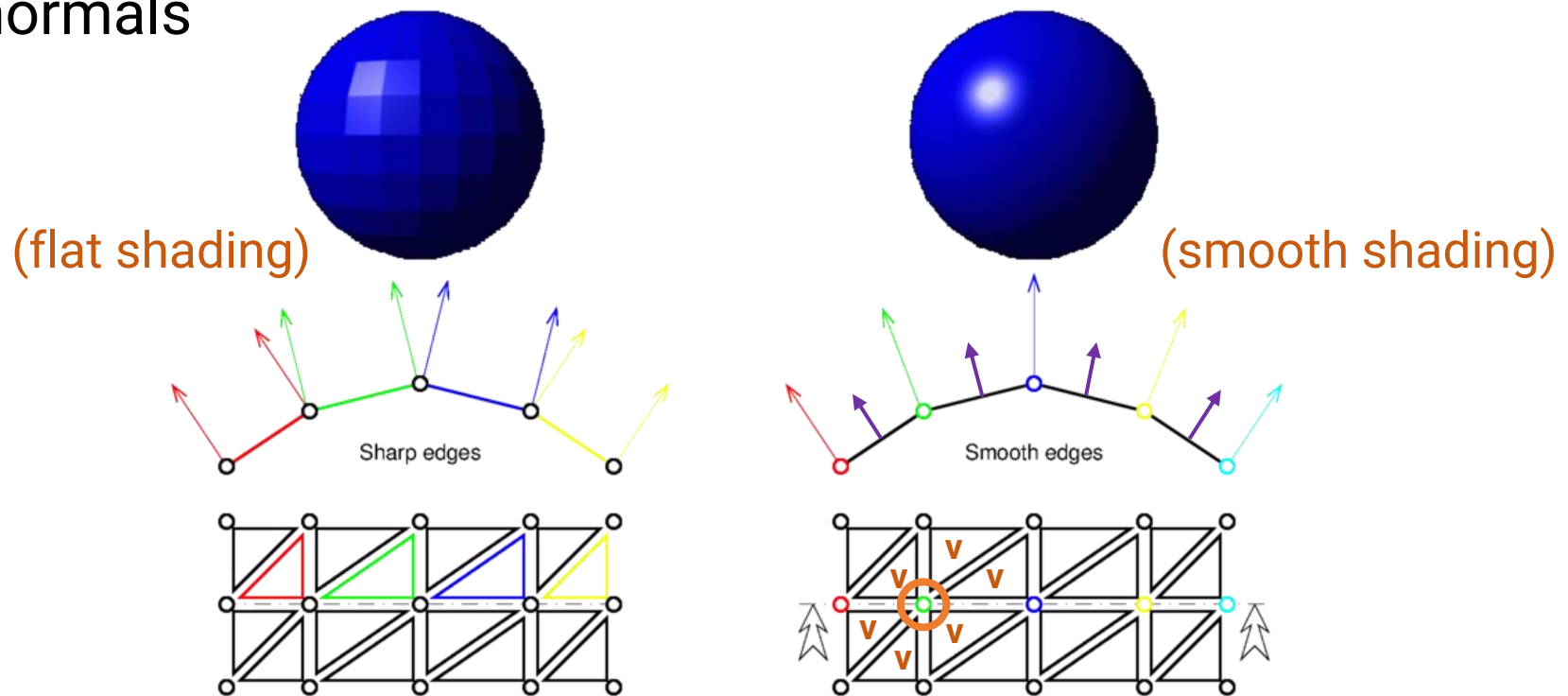


# Point, Triangle, and Surface Normal



# Vertex Normal

- Compute by **averaging** the surface normals of the faces that contain that vertex
- Can achieve much **smooth** shading than using triangle normals



# 3D Model Format

- A model is often stored in a file
- Common file format includes
  - **Wavefront (\*.obj)**
  - Polygon file format (\*.ply)
  - **Filmbox (\*.fbx)**
  - MAX (\*.max)
  - Digital Asset Exchange File (\*.dae)
  - STereoLithography (\*.stl)

# Example: Wavefront OBJ File Format

- cube.obj

TexCube.obj - 記事本

檔案(E) 編輯(E) 格式(O) 檢視(V) 說明

```
# Blender v2.76 (sub 0) OBJ File: ''
# www.blender.org
```

comments

```
mtllib TexCube.mtl
```

specify material file

```
v 1.0 -1.0 -1.0
v 1.0 -1.0 1.0
v -1.0 -1.0 1.0
v -1.0 -1.0 -1.0
v 1.0 1.0 -1.0
v 1.0 1.0 1.0
v -1.0 1.0 1.0
v -1.0 1.0 -1.0
```

vertex position declaration

```
vt 0.0 0.0
vt 0.0 1.0
vt 1.0 0.0
vt 1.0 1.0
```

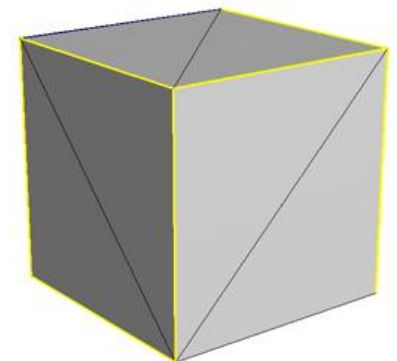
vertex texture coordinate declaration

```
vn 0.0 -1.0 0.0
vn 0.0 1.0 0.0
vn 1.0 0.0 0.0
vn -0.0 0.0 1.0
vn -1.0 -0.0 -0.0
vn 0.0 0.0 -1.0
```

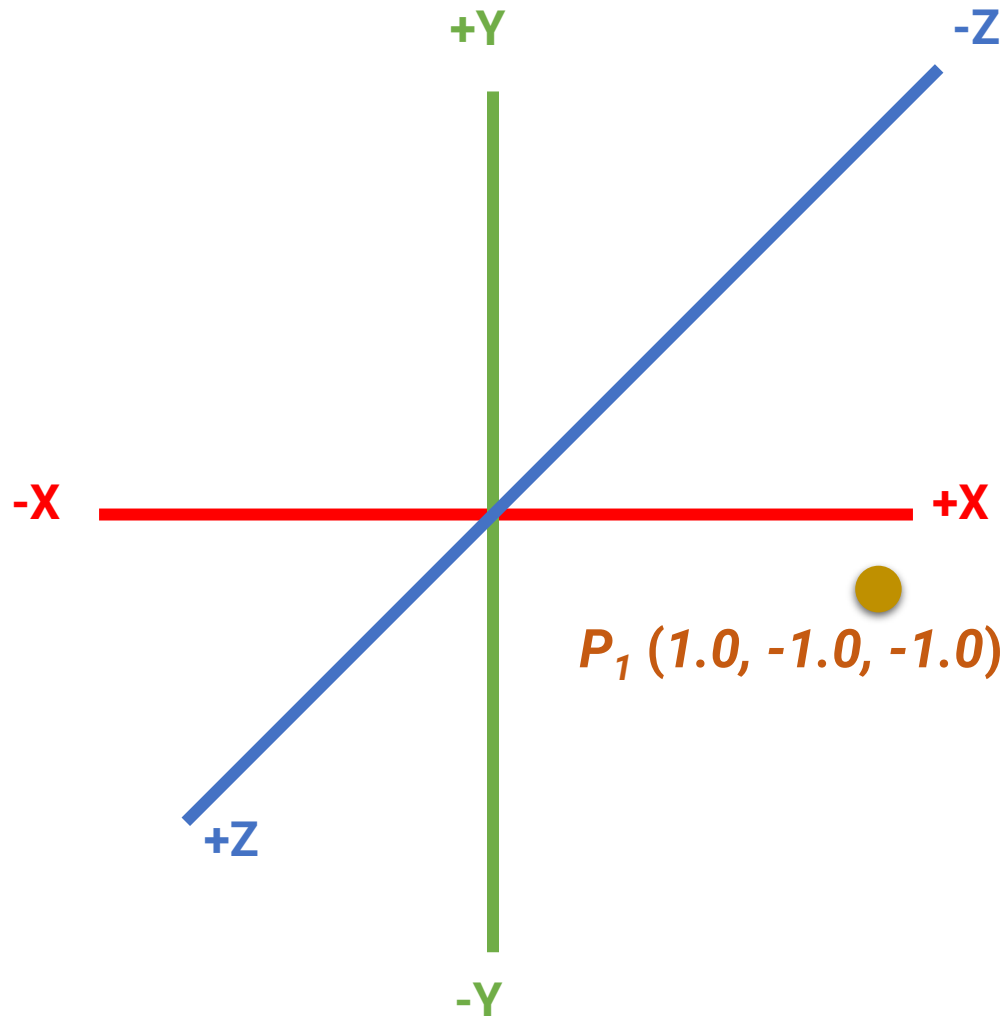
vertex normal declaration

```
usemtl cubeMtl
f 8/2/2 7/1/2 6/3/2
f 5/4/2 8/2/2 6/3/2
f 2/4/1 3/2/1 4/1/1
f 1/3/1 2/4/1 4/1/1
f 2/3/4 6/4/4 3/1/4
f 6/4/4 7/2/4 3/1/4
f 5/4/3 6/2/3 2/1/3
f 1/3/3 5/4/3 2/1/3
f 3/3/5 7/4/5 8/2/5
f 4/1/5 3/3/5 8/2/5
f 5/2/6 1/1/6 8/4/6
f 1/1/6 4/3/6 8/4/6
```

face data  
(adjacency, submesh)

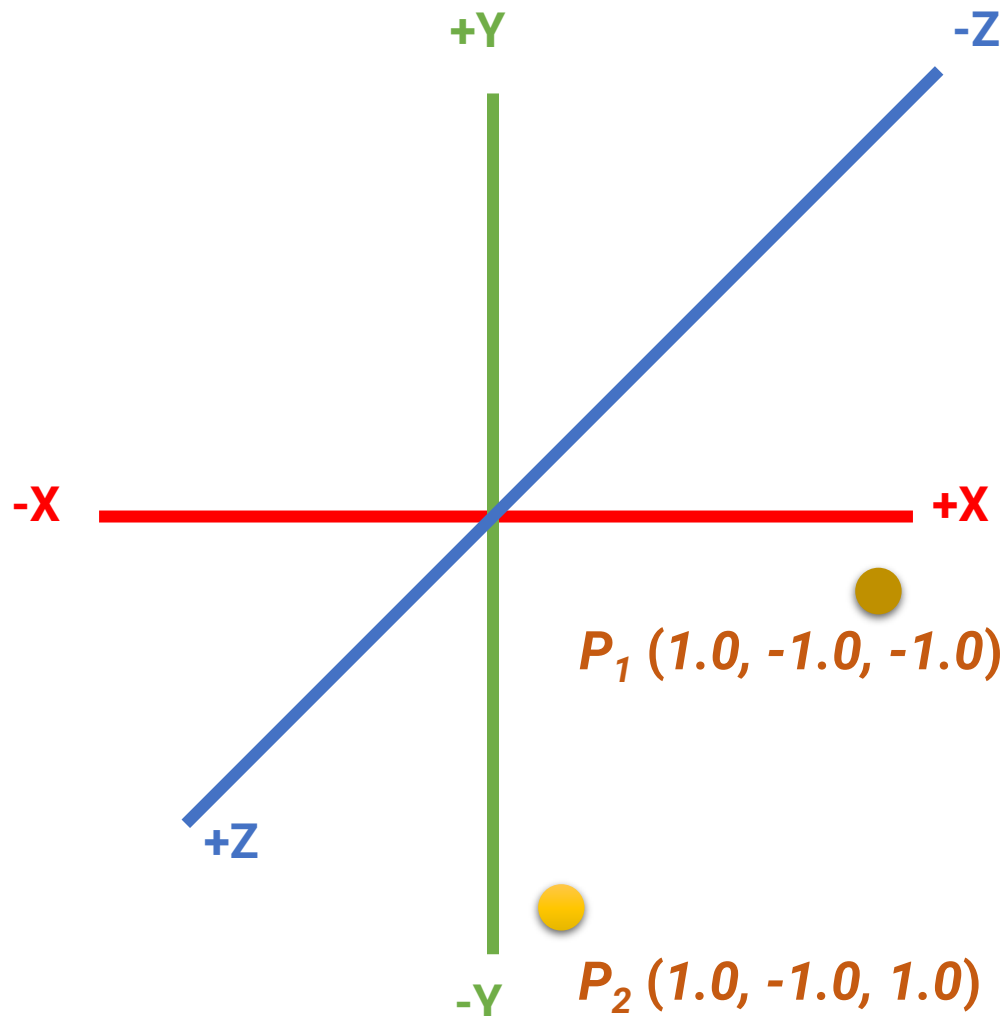


# Example: Wavefront OBJ File Format (cont.)



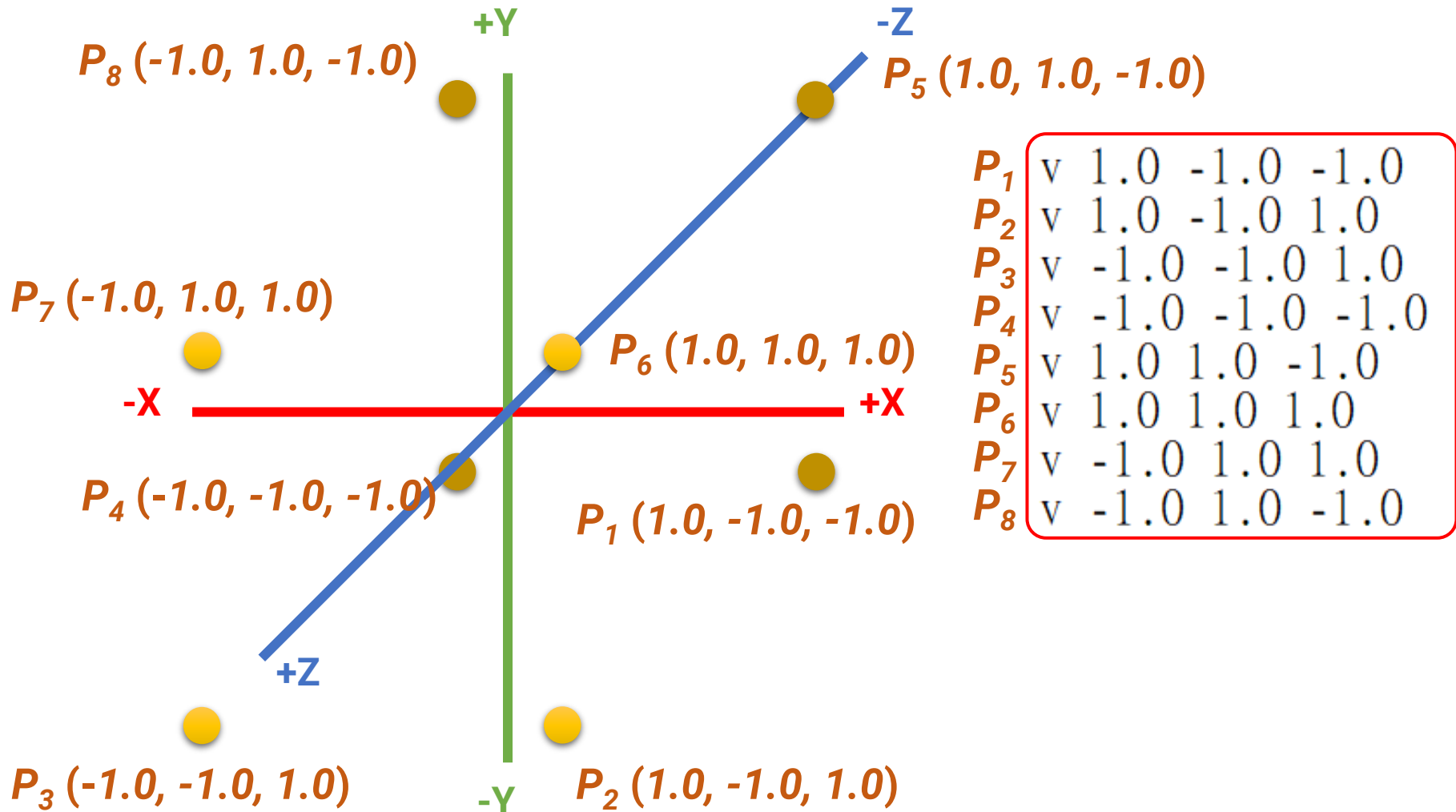
$P_1$	v	1.0	-1.0	-1.0
$P_2$	v	1.0	-1.0	1.0
$P_3$	v	-1.0	-1.0	1.0
$P_4$	v	-1.0	-1.0	-1.0
$P_5$	v	1.0	1.0	-1.0
$P_6$	v	1.0	1.0	1.0
$P_7$	v	-1.0	1.0	1.0
$P_8$	v	-1.0	1.0	-1.0

# Example: Wavefront OBJ File Format (cont.)



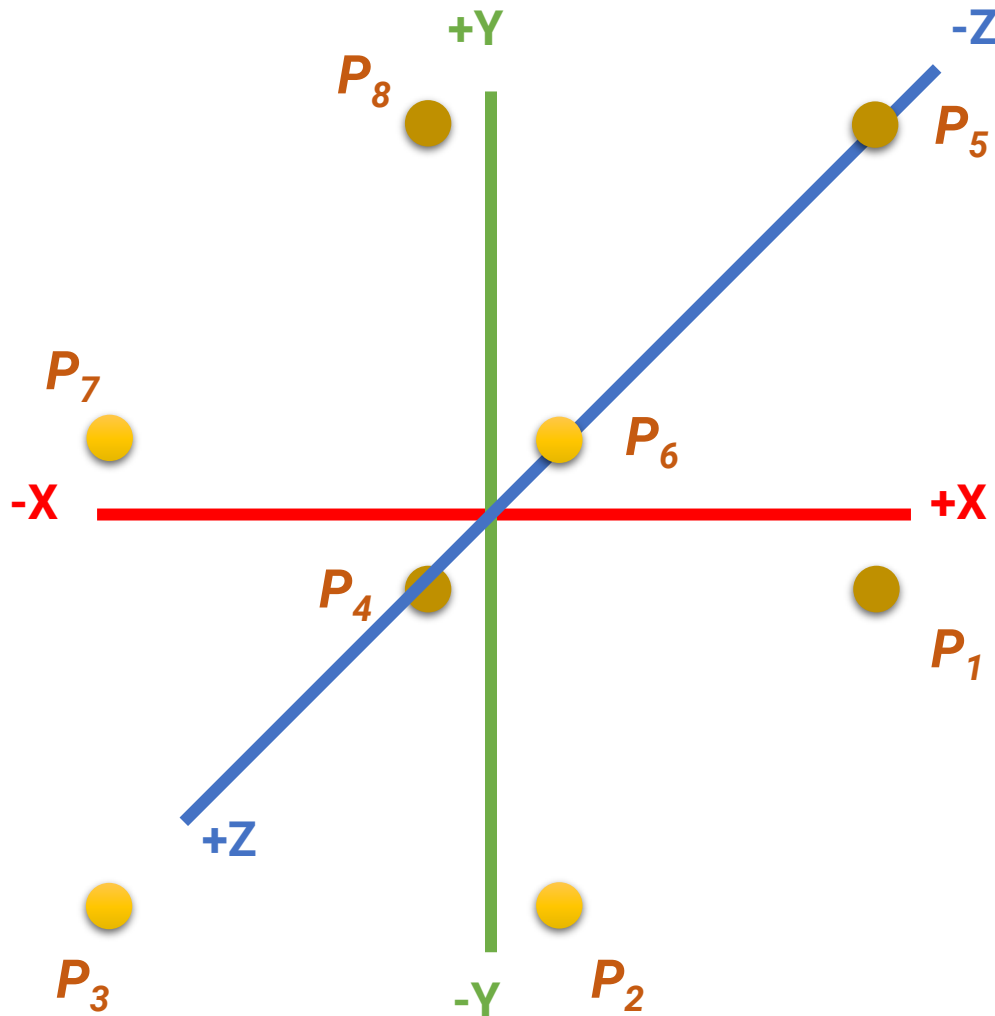
$P_1$	v	1.0	-1.0	-1.0
$P_2$	v	1.0	-1.0	1.0
$P_3$	v	-1.0	-1.0	1.0
$P_4$	v	-1.0	-1.0	-1.0
$P_5$	v	1.0	1.0	-1.0
$P_6$	v	1.0	1.0	1.0
$P_7$	v	-1.0	1.0	1.0
$P_8$	v	-1.0	1.0	-1.0

# Example: Wavefront OBJ File Format (cont.)





# Example: Wavefront OBJ File Format (cont.)



$F_1$	f	8/2/2	7/1/2	6/3/2
$F_2$	f	5/4/2	8/2/2	6/3/2
$F_3$	f	2/4/1	3/2/1	4/1/1
$F_4$	f	1/3/1	2/4/1	4/1/1
$F_5$	f	2/3/4	6/4/4	3/1/4
$F_6$	f	6/4/4	7/2/4	3/1/4
$F_7$	f	5/4/3	6/2/3	2/1/3
$F_8$	f	1/3/3	5/4/3	2/1/3
$F_9$	f	3/3/5	7/4/5	8/2/5
$F_{10}$	f	4/1/5	3/3/5	8/2/5
$F_{11}$	f	5/2/6	1/1/6	8/4/6
$F_{12}$	f	1/1/6	4/3/6	8/4/6

**vertex1 vertex2 vertex3**

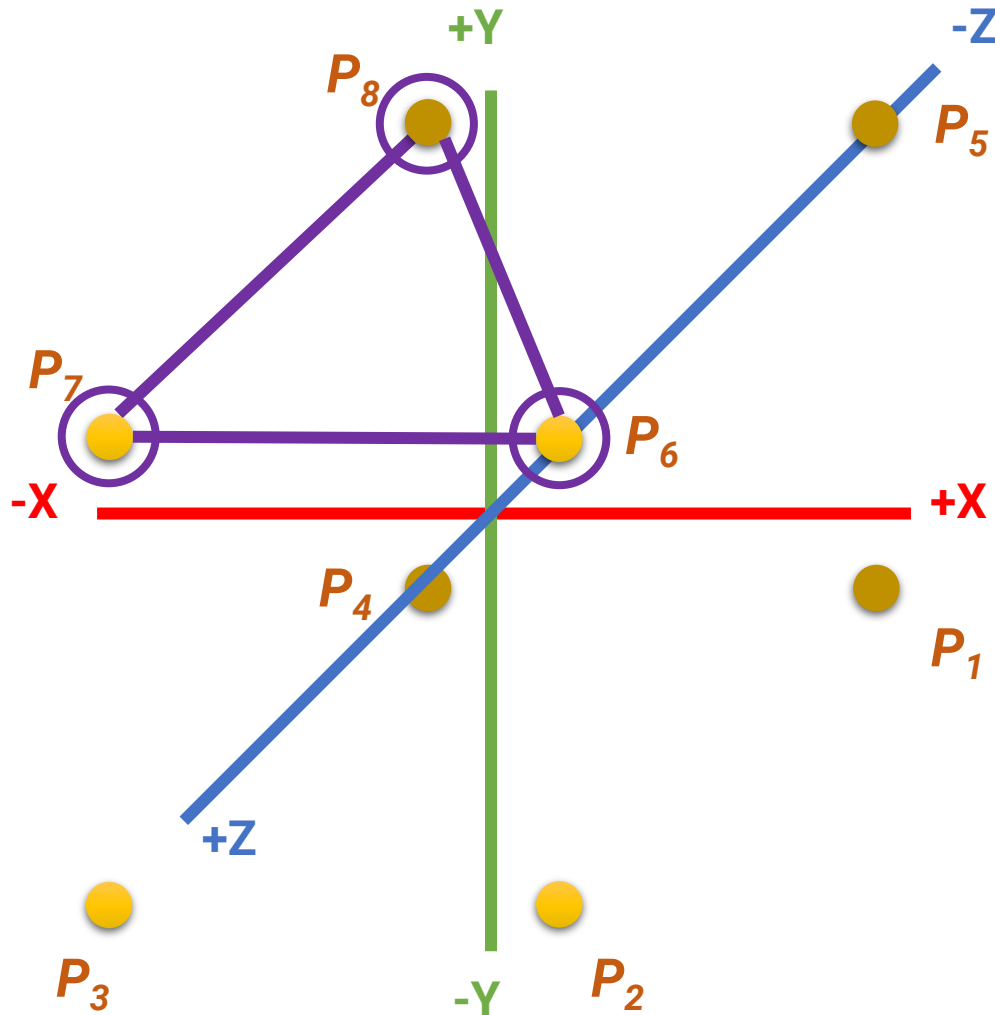
**f P/T/N P/T/N P/T/N**

**P: index of vertex position**

**T: index of texture coordinate**

**N: index of vertex normal**

# Example: Wavefront OBJ File Format (cont.)



$F_1$	f	<u>8/2/2</u>	<u>7/1/2</u>	<u>6/3/2</u>
$F_2$	f	5/4/2	8/2/2	6/3/2
$F_3$	f	2/4/1	3/2/1	4/1/1
$F_4$	f	1/3/1	2/4/1	4/1/1
$F_5$	f	2/3/4	6/4/4	3/1/4
$F_6$	f	6/4/4	7/2/4	3/1/4
$F_7$	f	5/4/3	6/2/3	2/1/3
$F_8$	f	1/3/3	5/4/3	2/1/3
$F_9$	f	3/3/5	7/4/5	8/2/5
$F_{10}$	f	4/1/5	3/3/5	8/2/5
$F_{11}$	f	5/2/6	1/1/6	8/4/6
$F_{12}$	f	1/1/6	4/3/6	8/4/6

**vertex1 vertex2 vertex3**

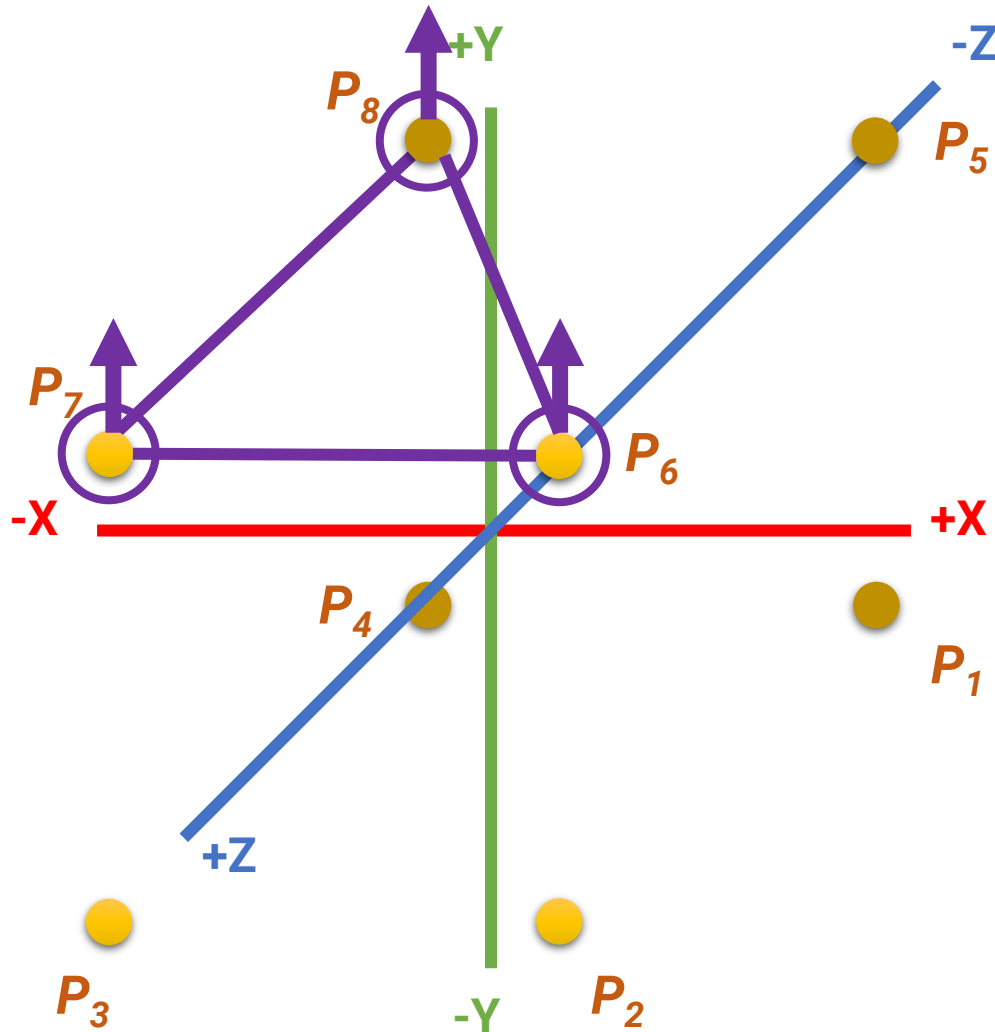
**f P/T/N P/T/N P/T/N**

**P: index of vertex position**

**T: index of texture coordinate**

**N: index of vertex normal**

# Example: Wavefront OBJ File Format (cont.)



$F_1$  f 8/2/2 7/1/2 6/3/2

$N_1$  vn 0.0 -1.0 0.0

$N_2$  vn 0.0 1.0 0.0

$N_3$  vn 1.0 0.0 0.0

$N_4$  vn -0.0 0.0 1.0

$N_5$  vn -1.0 -0.0 -0.0

$N_6$  vn 0.0 0.0 -1.0

**vertex1 vertex2 vertex3**

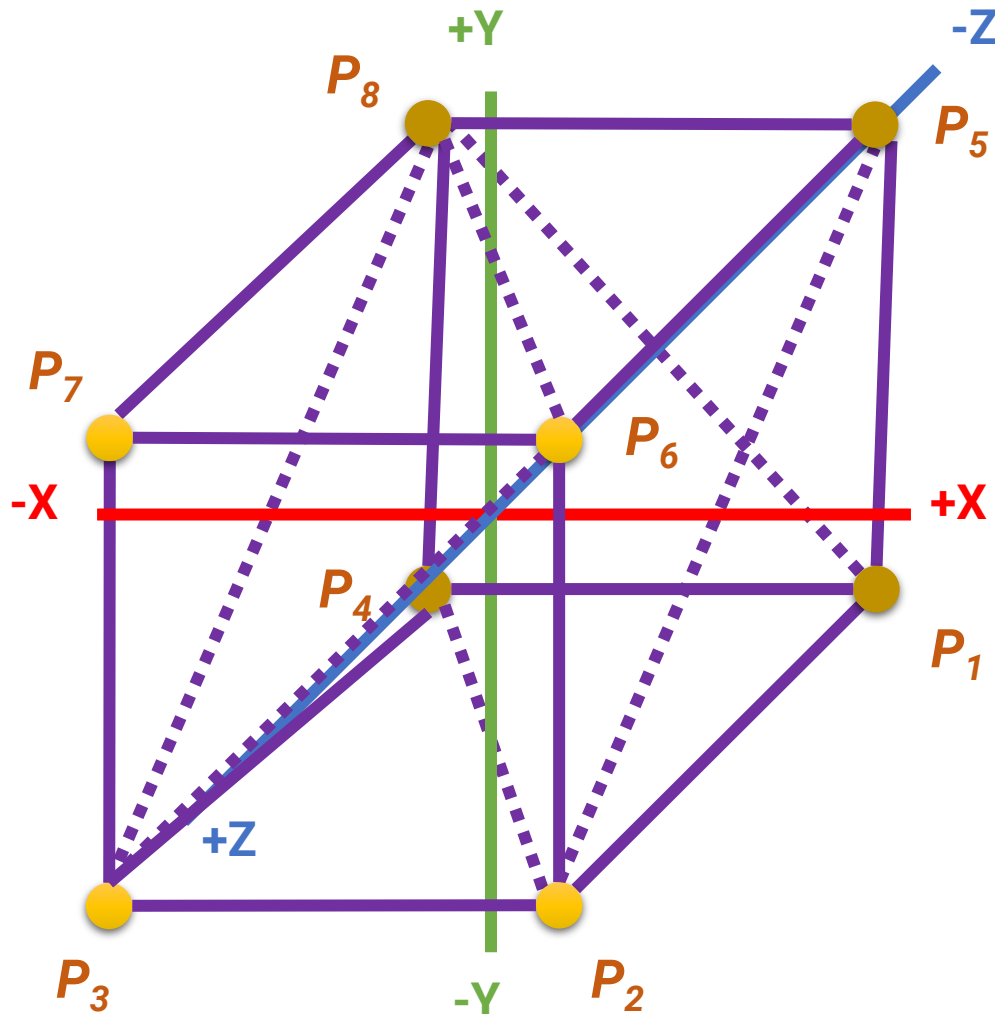
**f P/T/N P/T/N P/T/N**

**P: index of vertex position**

**T: index of texture coordinate**

**N: index of vertex normal**

# Example: Wavefront OBJ File Format (cont.)



$F_1$	f	8/2/2	7/1/2	6/3/2
$F_2$	f	5/4/2	8/2/2	6/3/2
$F_3$	f	2/4/1	3/2/1	4/1/1
$F_4$	f	1/3/1	2/4/1	4/1/1
$F_5$	f	2/3/4	6/4/4	3/1/4
$F_6$	f	6/4/4	7/2/4	3/1/4
$F_7$	f	5/4/3	6/2/3	2/1/3
$F_8$	f	1/3/3	5/4/3	2/1/3
$F_9$	f	3/3/5	7/4/5	8/2/5
$F_{10}$	f	4/1/5	3/3/5	8/2/5
$F_{11}$	f	5/2/6	1/1/6	8/4/6
$F_{12}$	f	1/1/6	4/3/6	8/4/6

**vertex1 vertex2 vertex3**  
**f P/T/N P/T/N P/T/N**

**P: index of vertex position**  
**T: index of texture coordinate**  
**N: index of vertex normal**

# Texture Coordinate

- A coordinate to look up the texture
  - The way to map a point on the 3D surface to a pixel (texel) on a 2D image texture
- We will introduce texture mapping in the near future

