

Advanced Materials

Computer Graphics

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(with some slides borrowed from Prof. Yung-Yu Chuang)

Outline

- <u>Overview</u>
- <u>Microfacet Models</u>
- <u>Materials beyond BRDFs</u>
- BRDFs for Production

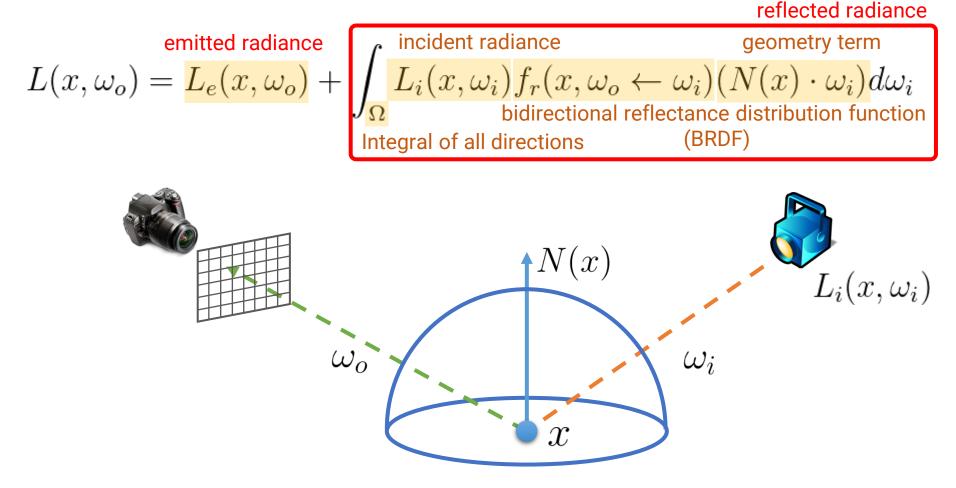
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The Rendering Equation

• Proposed by Kajiya [1986]



Formal Material Representation

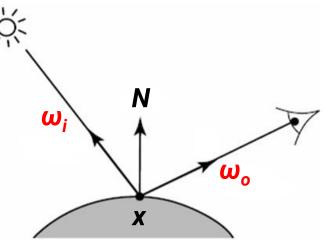
 In Physically-based Rendering (PBR), the characteristic of a material is usually defined by Bidirectional Reflectance Distribution Function (BRDF)

$$f_r(x, \omega_o \leftarrow \omega_i)$$

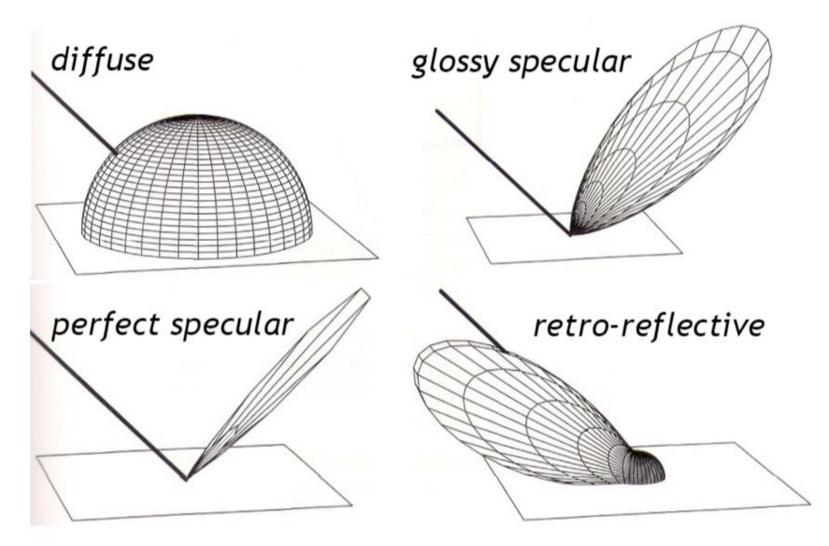
• Describe how much light (ratio) coming from ω_i will reflect toward ω_o at point **x**

A good representation should have

- Accuracy
- Expressiveness
- Speed



Reflection Categories



Classification of BRDF

Phenomenological models

- Qualitative approach
- Models with intuitive parameters
- Examples are Phong and Blinn-Phong lighting models

Geometric optics

- Microfacet models
- Measured data
 - Usually described in tabular form or coefficients of a set of basis functions

Outline

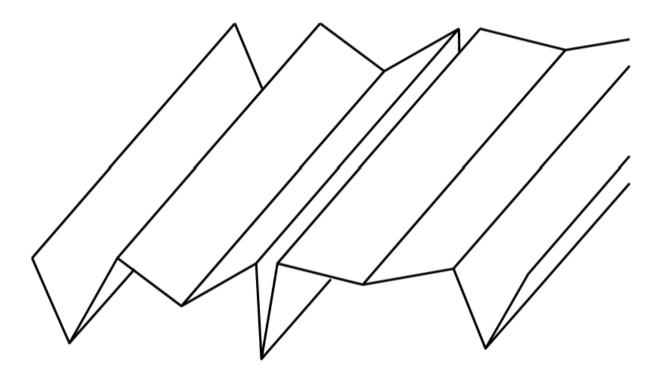
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Microfacet Model

- Rough surfaces can be modeled as a collection of small microfacets
- The **aggregate behavior** of the small microfacets determines the scattering
- Two components for deriving a closed-form BRDF expression
 - The distribution of microfacets
 - How light scatters from the individual microfacet

Ν

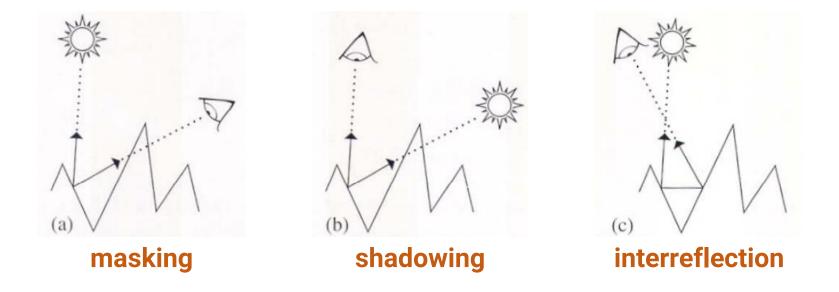
Microfacet Model (cont.)



Most microfacet models assume that all microfacets make up **symmetric V-shaped** grooves so that only neighboring microfacet needs to be considered

Microfacet Model (cont.)

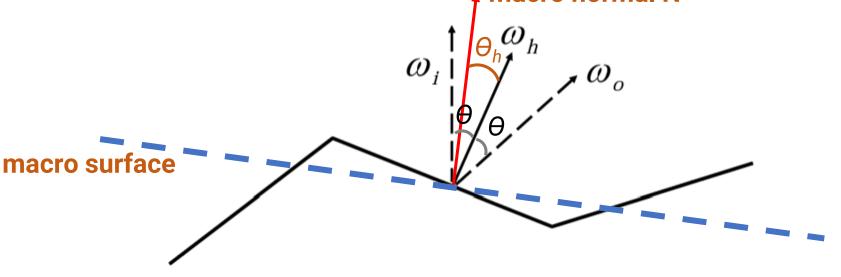
Important geometric effects to consider



 Particular models consider these effects with varying degrees of accuracy

Torrance-Sparrow Model

- One of the first microfacet model
- Designed to model metallic surfaces
- Assumption: a surface is composed of a collection of perfectly smooth mirrored microfacets with distribution D(ω_h)



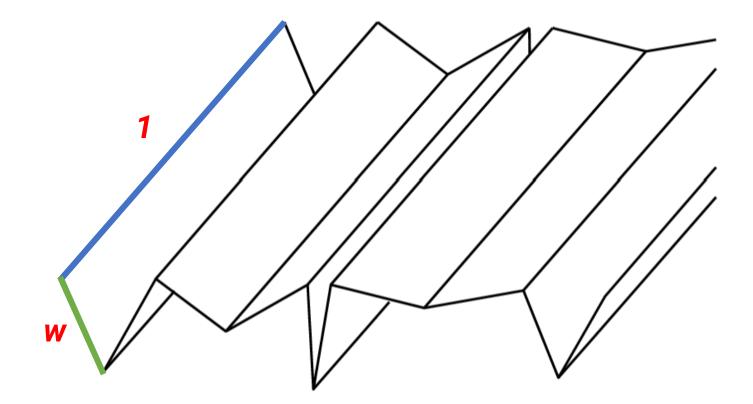
- Described by
 - Microfacet distribution D
 - Geometric attenuation G
 - Fresnel reflection F

$$f_r(\omega_o \leftarrow \omega_i) = \frac{D(\omega_h)G(\omega_i, \omega_o)F(\omega_i, \omega_h)}{4\cos\theta_i \cos\theta_o}$$

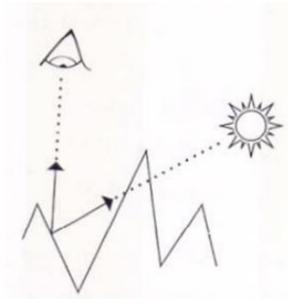
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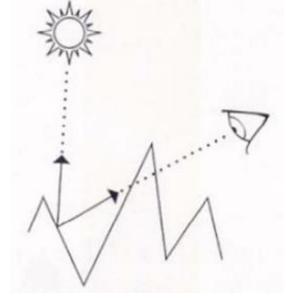
$$f_r(\omega_o \leftarrow \omega_i) = \frac{D(\omega_h)G(\omega_i, \omega_o)F(\omega_i, \omega_h)}{4\cos\theta_i \cos\theta_o}$$

• Configuration



• Geometry attenuation factor





shadowing

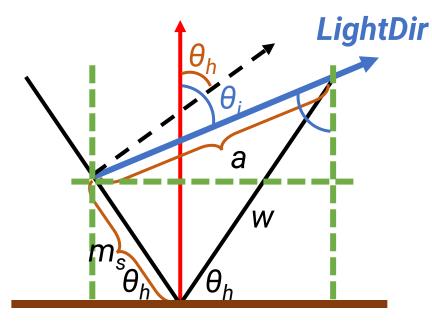
masking

G = <u>facet area that is both visible and illuminated</u> total facet area

• Shadowing term

1		m_s	
T		\overline{w}	

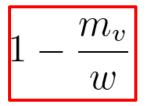
$$a \sin \theta_i = w \cos \theta_h + m_s \cos \theta_h \qquad \times \cos \theta_i a \cos \theta_i = w \sin \theta_h - m_s \sin \theta_h \qquad \times -\sin \theta_i$$



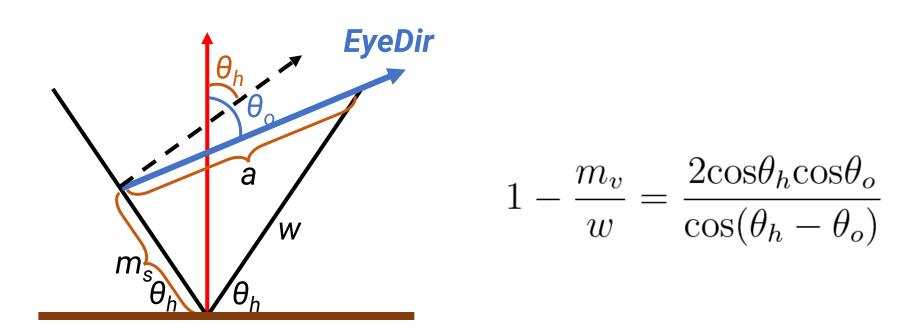
$$\frac{m_s}{w} = -\frac{\cos(\theta_h + \theta_i)}{\cos(\theta_h - \theta_i)}$$

$$1 - \frac{m_s}{w} = \frac{2\cos\theta_h \cos\theta_i}{\cos(\theta_h - \theta_i)}$$

Masking term



$$a\sin\theta_o = w\cos\theta_h + m_s\cos\theta_h \quad \times\cos\theta_o$$
$$a\cos\theta_o = w\sin\theta_h + m_s\sin\theta_h \times -\sin\theta_o$$



Geometry attenuation factor

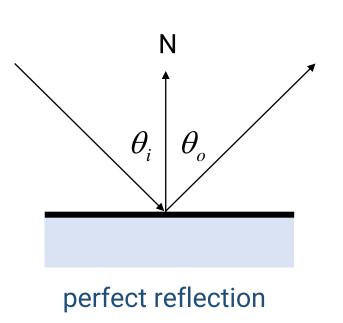
 $G = \frac{facet area that is both visible and illuminated}{total facet area}$

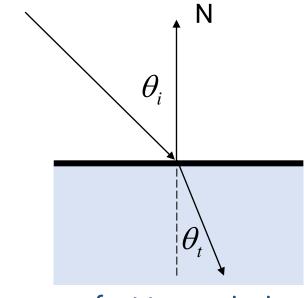
$$G = \min\left(1 - \frac{m_s}{w}, 1 - \frac{m_v}{w}\right) = \min\left(\frac{2\cos\theta_h\cos\theta_i}{\cos(\theta_h - \theta_i)}, \frac{2\cos\theta_h\cos\theta_o}{\cos(\theta_h - \theta_o)}\right)$$

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$$f_r(\omega_o \leftarrow \omega_i) = \frac{D(\omega_h)G(\omega_i, \omega_o)F(\omega_i, \omega_h)}{4\cos\theta_i \cos\theta_o}$$

- Real-world surface has both reflection and transmission
 - Perfect specular reflection: $\theta_i = \theta_o$
 - Perfect specular transmission: $\underline{\eta}_i \sin \theta_i = \underline{\eta}_t \sin \theta_t$ (Snell's law)





perfect transmission

index of refraction

- Reflectivity and transmissiveness: fraction of incoming light that is reflected or transmitted
 - Usually view dependent
 - Hence, the reflectivity is not a constant and should be corrected by the **Fresnel equation**
- Fresnel equation
 - Related to the wave's electric field
 - S polarization and P polarization https://en.wikipedia.org/wiki/Fresnel_equations

Different properties for dielectrics and conductors

$$r_{\parallel} = \frac{\eta_t \cos \theta_i - \eta_i \cos \theta_t}{\eta_t \cos \theta_i + \eta_i \cos \theta_t}$$
$$r_{\perp} = \frac{\eta_i \cos \theta_i - \eta_t \cos \theta_t}{\eta_i \cos \theta_i + \eta_t \cos \theta_t}$$

Fresnel reflectance for **dielectrics**

 $r_{\perp}^{2} = \frac{\left(\eta^{2} + k^{2}\right) - 2\eta\cos\theta_{i} + \cos^{2}\theta_{i}}{\left(\eta^{2} + k^{2}\right) + 2\eta\cos\theta_{i} + \cos^{2}\theta_{i}}$ Freshel reflectance for conductors

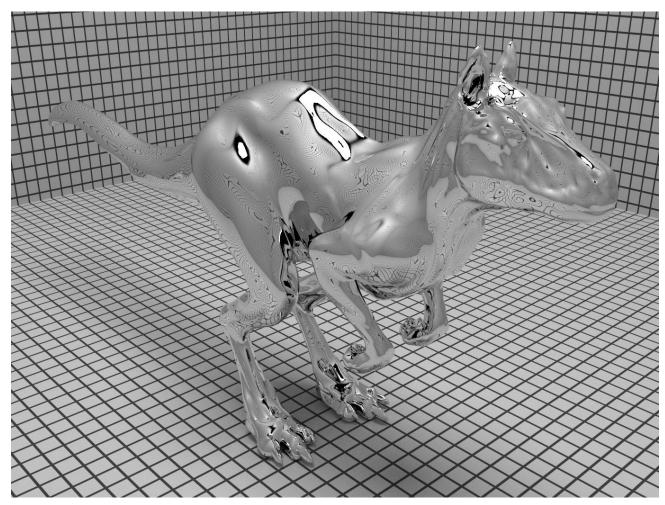
 $r_{\parallel}^{2} = \frac{\left(\eta^{2} + k^{2}\right)\cos^{2}\theta_{i} - 2\eta\cos\theta_{i} + 1}{\left(\eta^{2} + k^{2}\right)\cos^{2}\theta_{i} + 2\eta\cos\theta_{i} + 1}$

$$F_r(\omega_i) = \frac{1}{2} \left(r_{\parallel}^2 + r_{\perp}^2 \right)$$

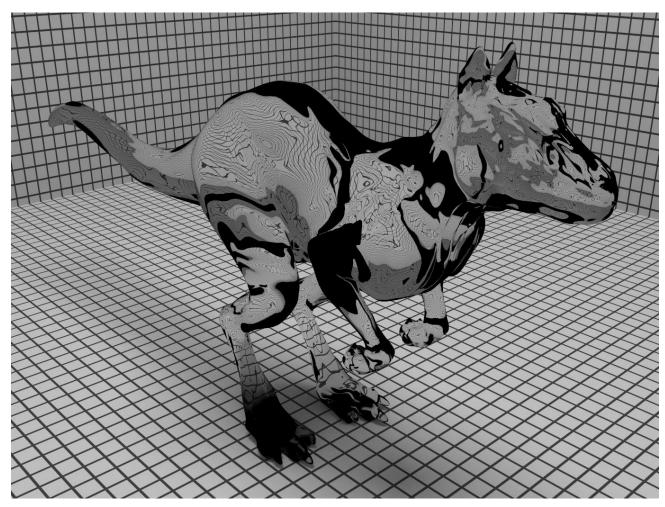
assume light is unpolarized

Indices of refraction

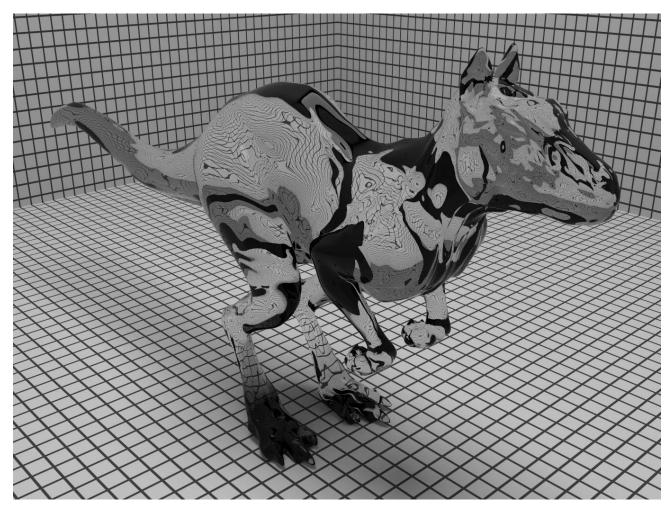
medium	Index of refraction	
Vaccum	1.0	
Air at sea level	1.00029	
lce	1.31	
Water (20°C)	1.333	
Fused quartz	1.46	
Glass	1.5~1.6	
Sapphire	1.77	
Diamond	2.42	



perfect specular refraction



perfect specular transmission (refraction)



Fresnel modulation

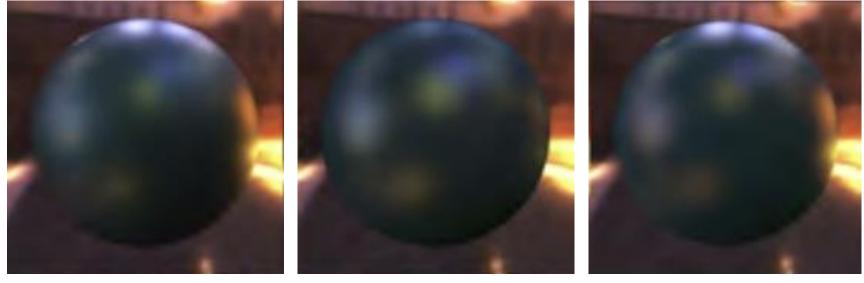
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$$f_r(\omega_o \leftarrow \omega_i) = \frac{D(\omega_h)G(\omega_i, \omega_o)F(\omega_i, \omega_h)}{4\cos\theta_i \cos\theta_o}$$

How many micro surfaces have this orientation Commonly used distributions: Beckmann, GGX

$$D\left(\omega_{h}
ight)=rac{lpha^{2}}{\pi \Big(\left(\mathbf{n}\cdotoldsymbol{\omega}_{h}
ight)^{2}\left(lpha^{2}-1
ight)+1\Big)^{2}}$$

• Put it all together



measured

Blinn-Phong

Cook-Torrance (microfacet)

Oren-Nayar Model

- Many real-world materials such as concrete, sand and cloth are not real Lambertian
 - Specifically, rough surfaces generally appear brighter as the illumination direction approaches the viewing direction



Lambertian model

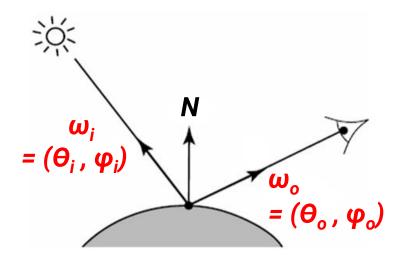
real image

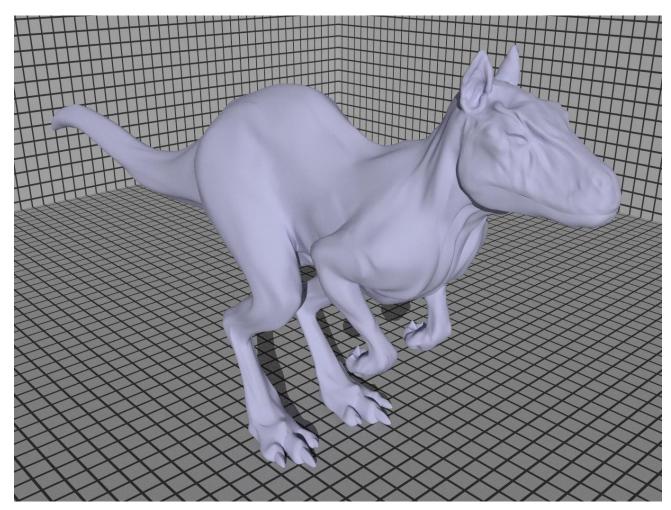
 Assumption: a surface is composed of a collection of perfectly Lambertian grooves whose orientation angles follow a Gaussian distribution

$$f_r(\omega_o \leftarrow \omega_i) = \frac{\rho}{\pi} (A + B\max(0, \cos(\phi_i - \phi_o))\sin\alpha \tan\beta)$$

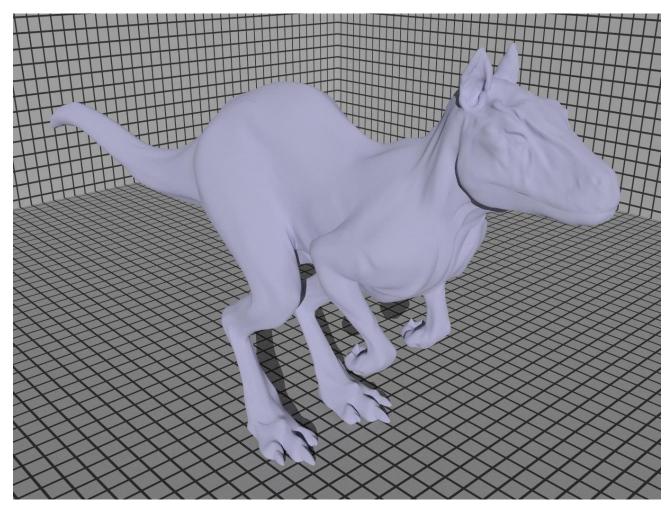
 $A=1-\frac{\ensuremath{\overline{\sigma}}^2}{2(\sigma^2+0.33)}$ the standard deviation of Gaussian

$$B = \frac{0.45\sigma^2}{\sigma^2 + 0.09}$$
$$\alpha = \max(\theta_i, \theta_o)$$
$$\beta = \min(\theta_i, \theta_o)$$



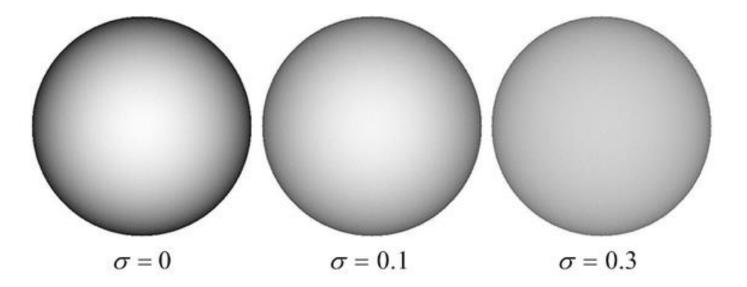


Lambertian model



Oren-Nayar model

- When the standard deviation σ becomes zero, Oren-Nayar model is reduced to Lambertian model



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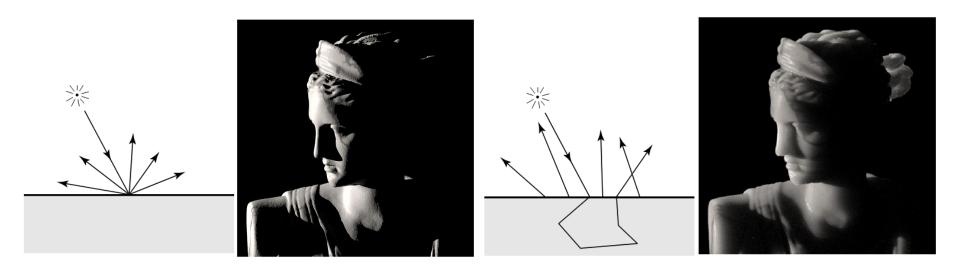
Subsurface Scattering

- Some materials interact with lights with a subsurface scattering process that allows lights to enter and scatter within a medium
- It gives objects a distinct soft look



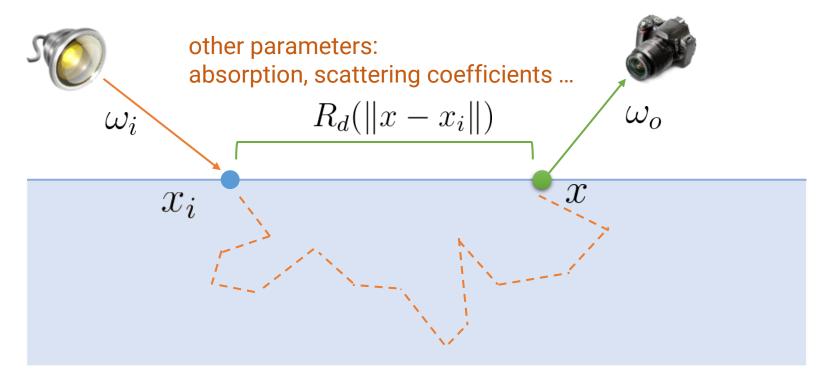
BSSRDF

• BRDF v.s. BSSRDF



Bidirectional Reflectance Distribution Function (BRDF) Bidirectional Subsurface Scattering Reflectance Distribution Function (BSSRDF)

Approximate BSSRDF with Dipole



$$S(x,\omega_o;x_i,\omega_i) = S^1(x,\omega_o;x_i,\omega_i) + S^d(x,\omega_o;x_i,\omega_i)$$
$$S^d(x,\omega_o;x_i,\omega_i) = \frac{1}{\pi}F_t(\eta,\omega_o)\frac{R_d(\|x-x_i\|)}{F_t(\eta,\omega_i)}F_t(\eta,\omega_i)$$

"A Practical Model for Subsurface Light Transport", Jensen et al. 2001

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Disney Principled BRDF

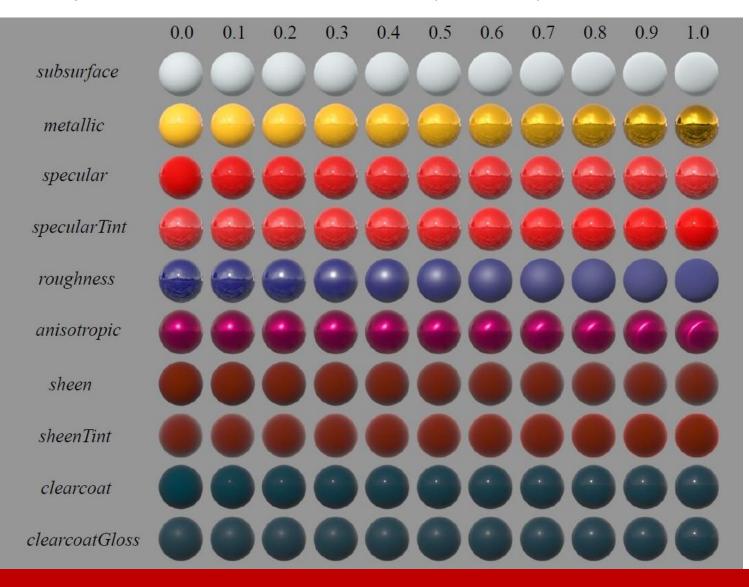
- Phenomenological models
 - More intuitive parameters; however, not accurate
- Geometric optics
 - More accurate but difficult to use by artists
- **Disney Principled BRDF** would like to combine the advantages of both models!
 - Represent a physically-based model (based on the Microfacet model) with few intuitive parameters
 - Each parameter has a range between [0, 1]
 - <u>https://disneyanimation.com/publications/physically-based-shading-at-disney/</u>

Disney Principled BRDF (cont.)

- Proposed when producing the movie, Wreck-It Ralph (2012)
 - Also used by the Unity and Unreal engine



Disney Principled BRDF (cont.)



Disney Principled BRDF (cont.)

Code: https://github.com/wdas/brdf/blob/main/src/brdfs/disney.brdf

$$egin{aligned} f_{ ext{disney}}(oldsymbol{\omega}_i,oldsymbol{\omega}_o) &= (1-\sigma_m) \left(rac{C}{\pi} ext{mix}(rac{f_d(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}{f_{ss}(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}, rac{f_{ss}(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}{f_{ss}(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}, \sigma_{ss}) + rac{f_{sh}(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}{f_{sh}(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}, \sigma_{ss}) + rac{f_{sh}(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}{4\cos heta_i\cos heta_o}} & ext{specular} \ &+ rac{\sigma_c}{4} rac{F_c(heta_d)G_c(oldsymbol{\omega}_i,oldsymbol{\omega}_o)D_c(oldsymbol{\omega}_i,oldsymbol{\omega}_o)}{4\cos heta_i\cos heta_o}} & ext{clearcoat} \end{aligned}$$

$$egin{aligned} f_d(oldsymbol{\omega}_i,oldsymbol{\omega}_o) &= (1+(F_{D90}-1)(1-\cos heta_i)^5)(1+(F_{D90}-1)(1-\cos heta_o)^5)\ F_{D90} &= 0.5+2\cos^2 heta_d\sigma_r \end{aligned}$$

$$egin{aligned} f_{ss}(m{\omega}_i,m{\omega}_o) &= 1.25(F_{ss}(1/(\cos heta_i+\cos heta_o)-0.5)+0.5)\ F_{ss} &= (1+(F_{ss90}-1)(1-\cos heta_i)^5)(1+(F_{ss90}-1)(1-\cos heta_o)^5)\ F_{ss90} &= \cos^2 heta_d\sigma_r \end{aligned}$$

$$egin{aligned} f_{sh}(oldsymbol{\omega}_i,oldsymbol{\omega}_o) &= ext{mix}(ext{one}, C_{tint}, \sigma_{sht})\sigma_{sh}(1-\cos heta_d)^5 \ C_{tint} &= rac{C}{ ext{lum}(C)} \end{aligned}$$

$$egin{aligned} F_s(heta_d) &= C_s + (1-C_s)(1-\cos heta_d)^5\ C_s &= ext{mix}(0.08\sigma_s ext{mix}(ext{one},C_{tint},\sigma_{st}),C,\sigma_m)\ G_s(oldsymbol{\omega}_i,oldsymbol{\omega}_o) &= G_{s1}(oldsymbol{\omega}_i)G_{s1}(oldsymbol{\omega}_o)\ D_s(oldsymbol{\omega}_h) &= rac{1}{\pilpha_xlpha_yigg(\sin^2 heta_higg(rac{\cos^2\phi}{lpha_x^2}+rac{\sin^2\phi}{lpha_y^2}igg)+\cos^2 heta_higg)^2\ F_c(heta_d) &= 0.04+0.96(1-\cos heta_d)^5\ G_c(oldsymbol{\omega}_i,oldsymbol{\omega}_o) &= G_{c1}(oldsymbol{\omega}_i)G_{c1}(oldsymbol{\omega}_o)\ D_c(oldsymbol{\omega}_h) &= rac{lpha^2-1}{2\pi\lnlpha(lpha^2\cos^2 heta_h+\sin^2 heta_h)} \end{aligned}$$

