



Textures (Part I)

Computer Graphics

Yu-Ting Wu

Outline

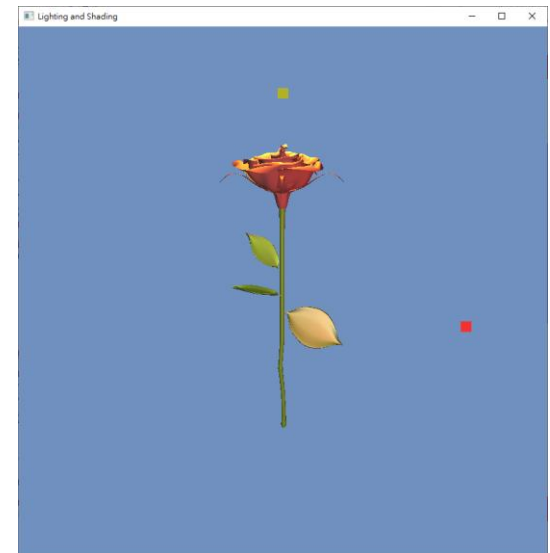
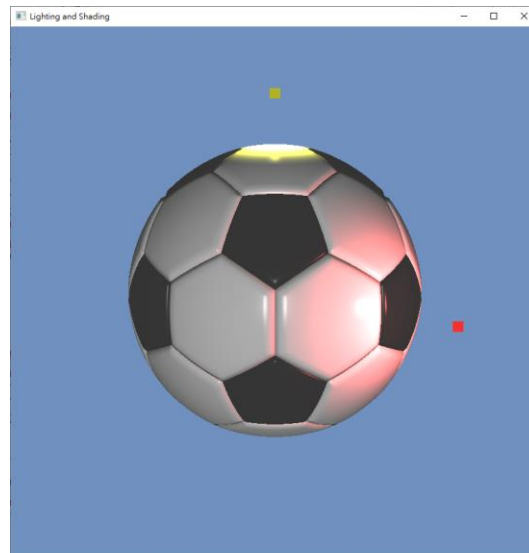
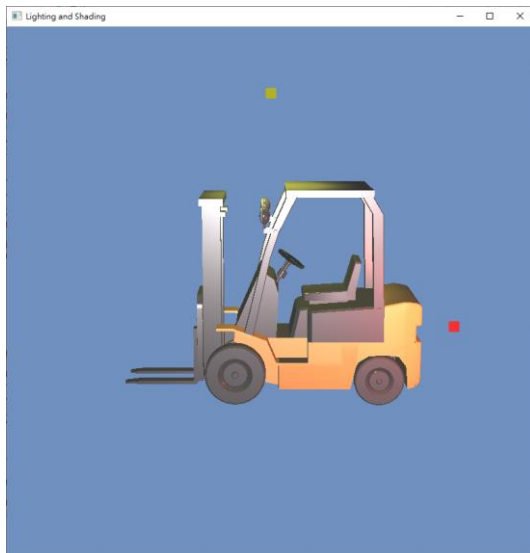
- [Overview](#)
 - [Texture data](#) (Part I)
 - [Texture filtering](#)
 - [Applications](#)
-
- OpenGL implementation (Part II)

Outline

- **Overview**
- Texture data
- Texture filtering
- Applications
- OpenGL implementation

Why Do We Need Textures

- So far, we have described object colors using their reflectance functions
 - Subdivide an object into several parts, each has its reflectance properties (e.g., different diffuse and specular colors)



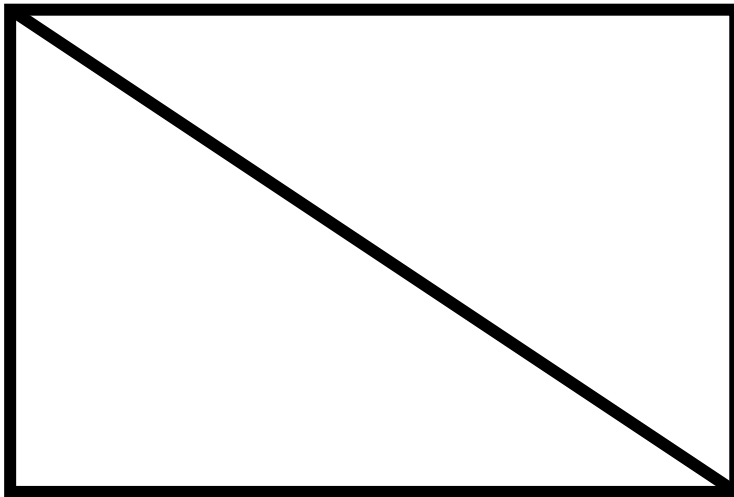
Why Do We Need Textures (cont.)

- Consider the following cases
 - Do we need (or can we) to finely subdivide the object?



Textures

- Can be used to represent **spatially-varying** data
- Can **decouple** materials from the geometry



Geometry: two triangles
Material: $K_d(1, 1, 1)$

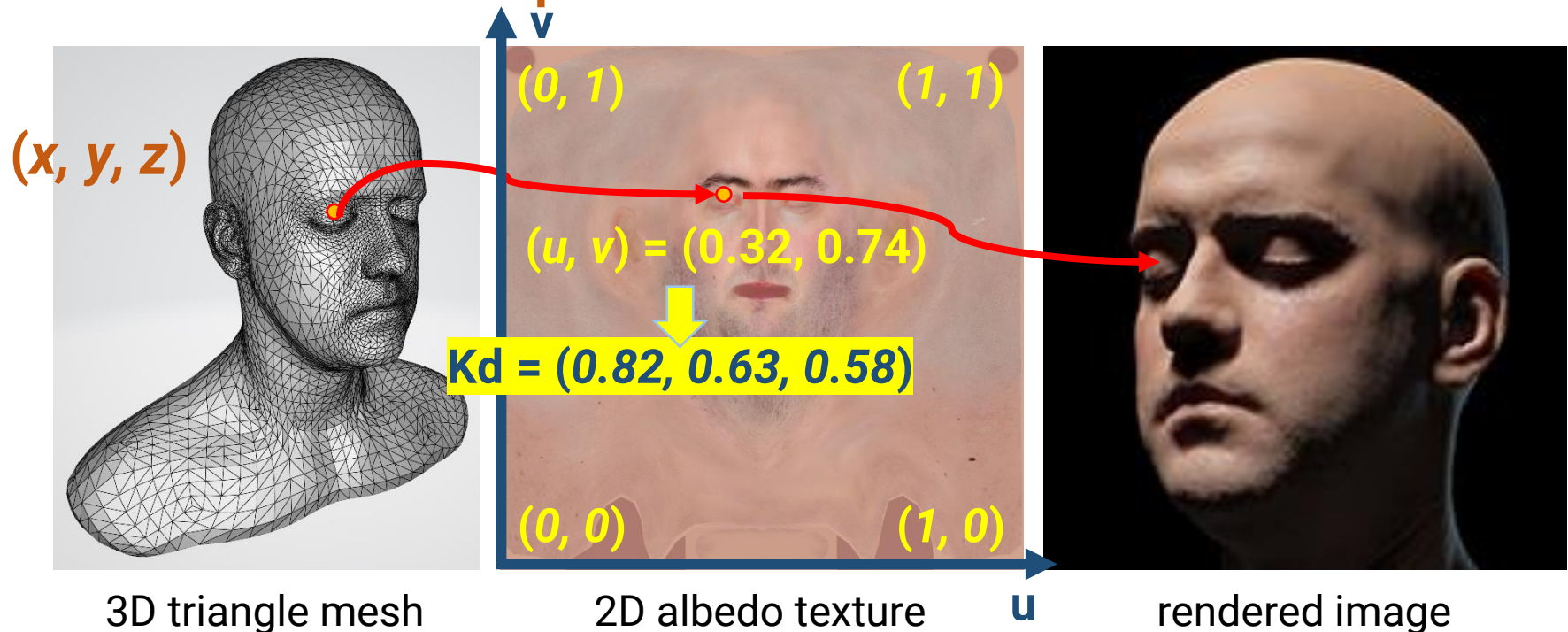


2D image texture

== complex appearance

Texture Coordinate

- A coordinate to look up the texture
- The way to map a point on an **arbitrary 3D surface** to a pixel (texel) on an **image** texture
 - Need **surface parameterization**



Texture Coordinate (cont.)

- A coordinate to look up the texture
- The way to map a point on an **arbitrary 3D surface** to a pixel (texel) on an **image** texture
 - Need **surface parameterization**
 - Usually produced by 3D artists

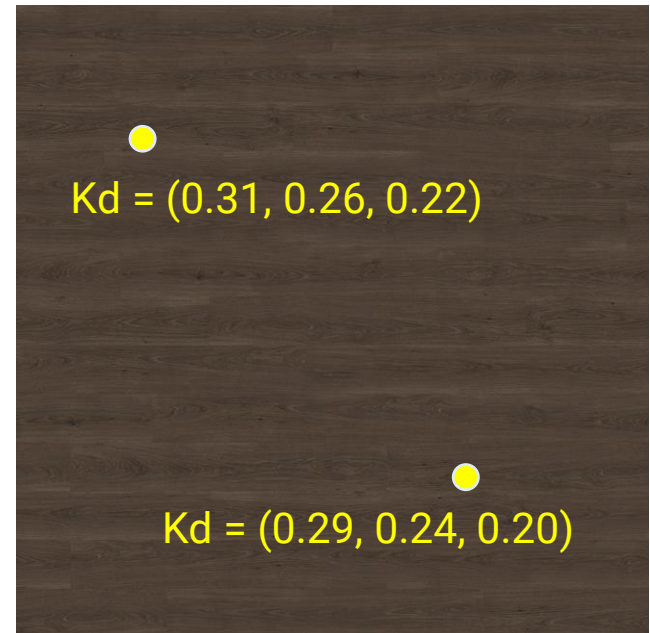


Types of Textures

- **2D image texture (most common)**
 - Material data (surface albedo, specularness, roughness)
 - Geometry data (surface bump, normals, height)
 - Lighting data (lightmap, ambient occlusion map)
- **3D volume texture**
 - Spatial data (participating media, collision detection)
- **Cubemap**
 - Spherical data (skybox, reflection probe)

Textures (cont.)

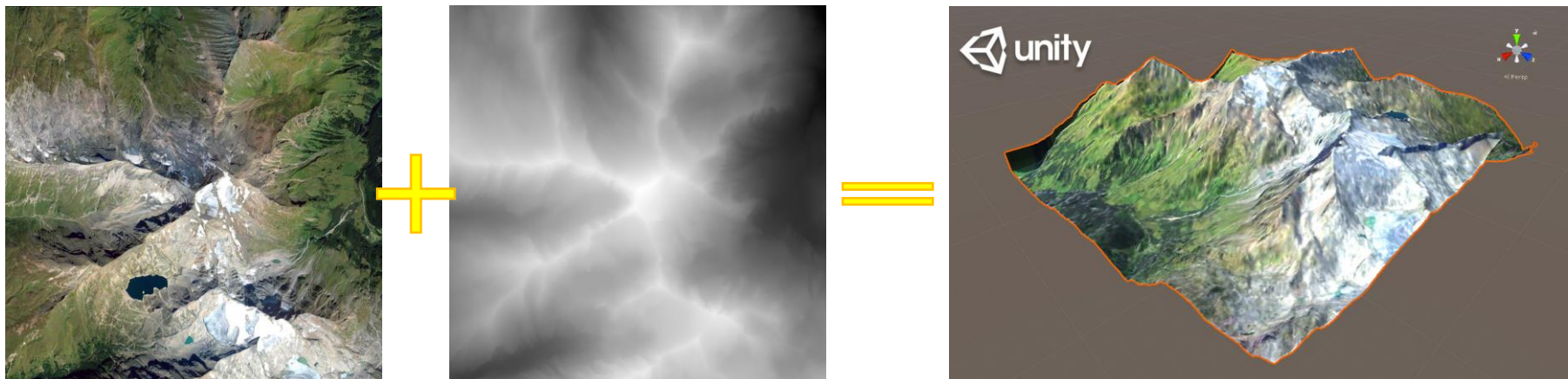
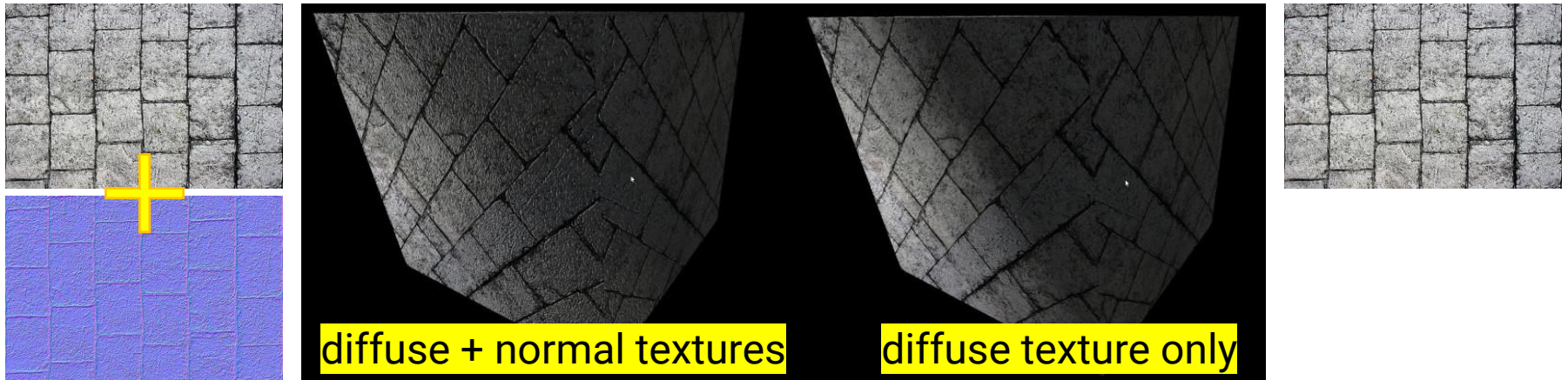
- 2D image texture for spatially-varying material



diffuse coefficient (K_d)

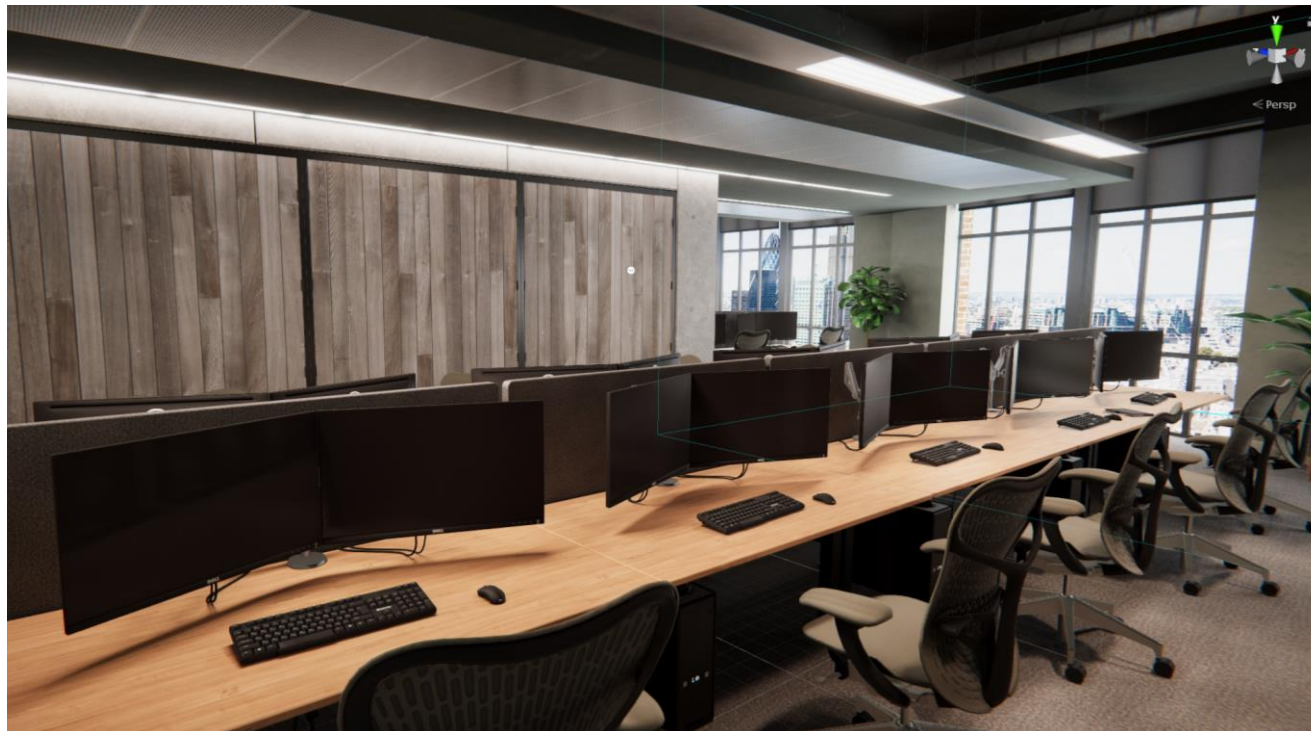
Types of Textures (cont.)

- 2D image texture for spatially-geometry data



Types of Textures (cont.)

- 2D image texture for precomputed lighting data



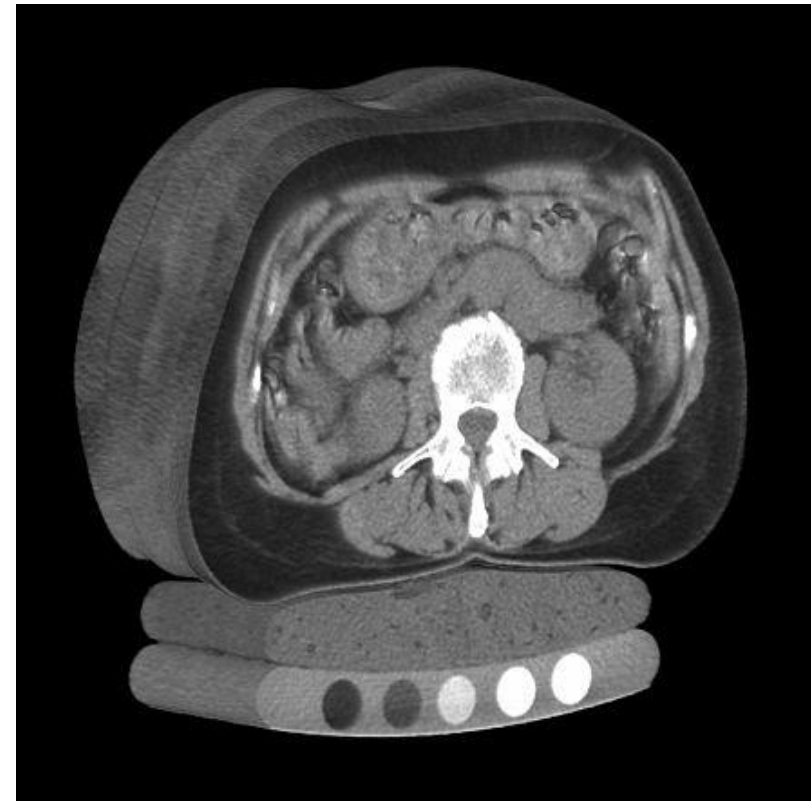
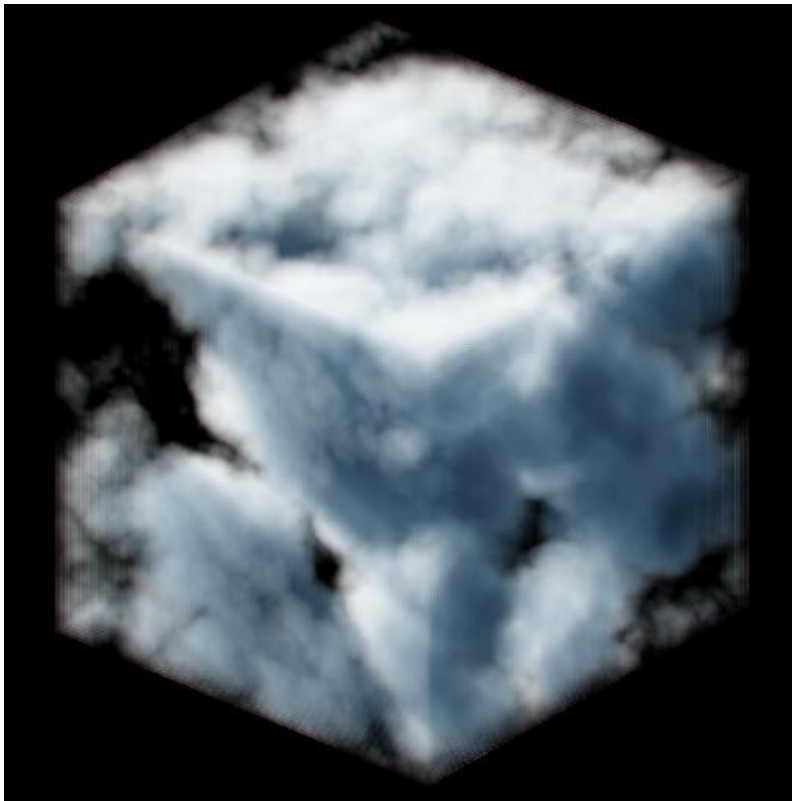
real-time rendered result



precomputed
lightmaps

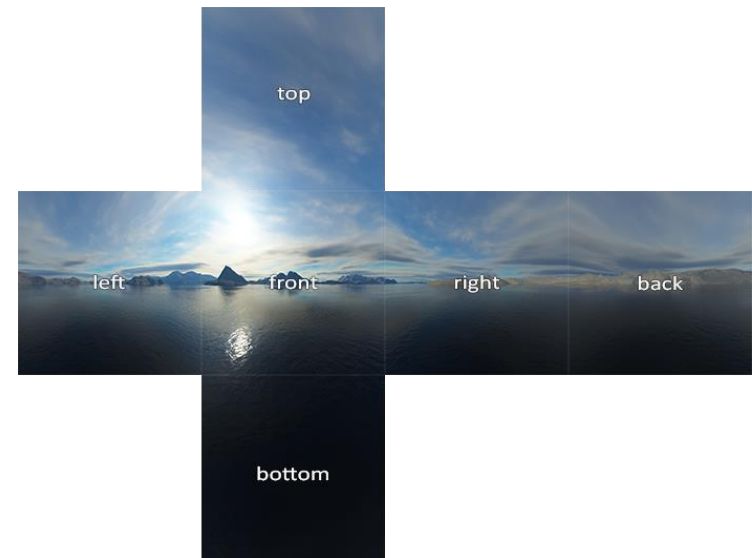
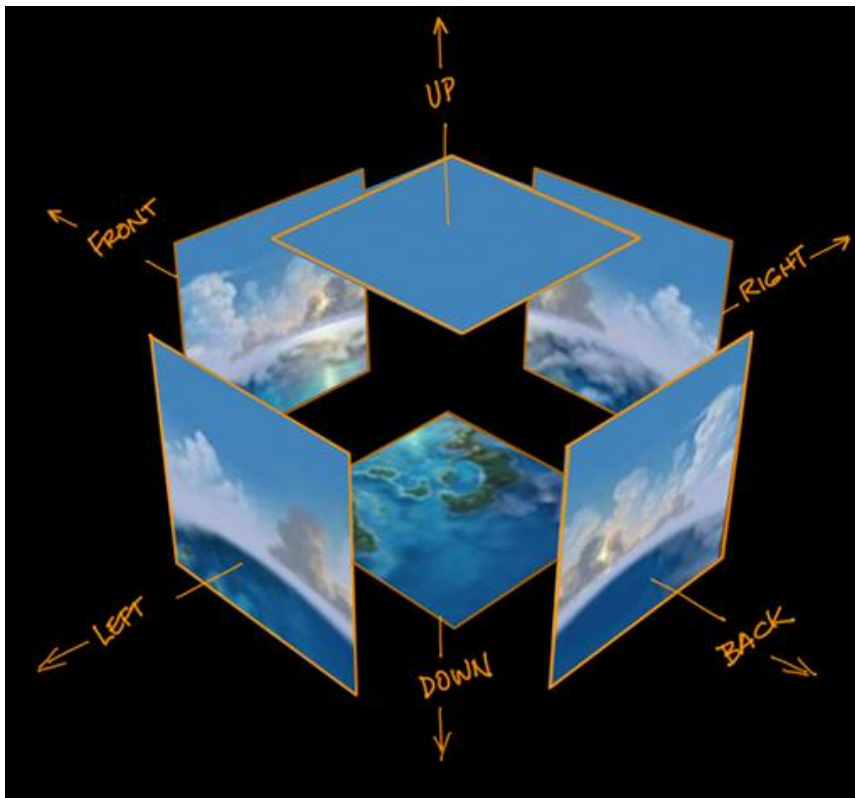
Types of Textures (cont.)

- 3D volume texture
 - Lookup by a 3D texture coordinate (u, v, s)



Types of Textures (cont.)

- Cubemap



Outline

- Overview
- **Texture data**
- Texture filtering
- Applications
- OpenGL implementation

Texture Data in Wavefront OBJ File

- TexCube.obj

```

TexCube.obj - 記事本
檔案(F) 編輯(E) 格式(O) 檢視(V) 說明
# Blender v2.76 (sub 0) OBJ File: ''
# www.blender.org
mtllib TexCube.mtl
v 1.000000 -1.000000 -1.000000
v 1.000000 -1.000000 1.000000
v -1.000000 -1.000000 1.000000
v -1.000000 -1.000000 -1.000000
v 1.000000 1.000000 -1.000000
v 1.000000 1.000000 1.000001
v -1.000000 1.000000 1.000000
v -1.000000 1.000000 -1.000000

vt 0.0 0.0
vt 0.0 1.0
vt 1.0 0.0
vt 1.0 1.0

vn 0.000000 -1.000000 0.000000
vn 0.000000 1.000000 0.000000
vn 1.000000 0.000000 0.000000
vn -0.000000 0.000000 1.000000
vn -1.000000 -0.000000 -0.000000
vn 0.000000 0.000000 -1.000000
  
```

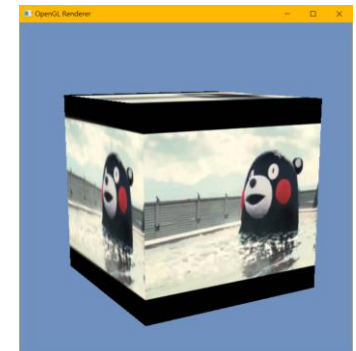
vertex texture coordinate declaration

f P/T/N P/T/N P/T/N

```

usemtl cubeMtl
f 8/2/2 7/1/2 6/3/2
f 5/4/2 8/2/2 6/3/2
f 2/4/1 3/2/1 4/1/1
f 1/3/1 2/4/1 4/1/1
f 2/3/4 6/4/4 3/1/4
f 6/4/4 7/2/4 3/1/4
f 5/4/3 6/2/3 2/1/3
f 1/3/3 5/4/3 2/1/3
f 3/3/5 7/4/5 8/2/5
f 4/1/5 3/3/5 8/2/5
f 5/2/6 1/1/6 8/4/6
f 1/1/6 4/3/6 8/4/6
  
```

face data
(adjacency, submesh)



Texture Data in Wavefront OBJ File (cont.)

```

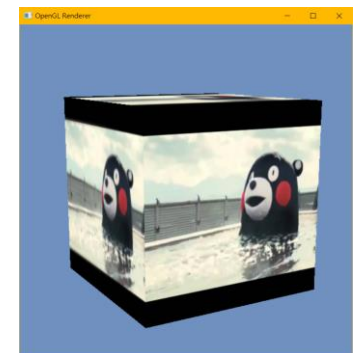
usemtl cubeMtl
f 8/2/2 7/1/2 6/3/2
f 5/4/2 8/2/2 6/3/2
f 2/4/1 3/2/1 4/1/1
f 1/3/1 2/4/1 4/1/1
f 2/3/4 6/4/4 3/1/4
f 6/4/4 7/2/4 3/1/4
f 5/4/3 6/2/3 2/1/3
f 1/3/3 5/4/3 2/1/3
f 3/3/5 7/4/5 8/2/5
f 4/1/5 3/3/5 8/2/5
f 5/2/6 1/1/6 8/4/6
f 1/1/6 4/3/6 8/4/6
  
```

```

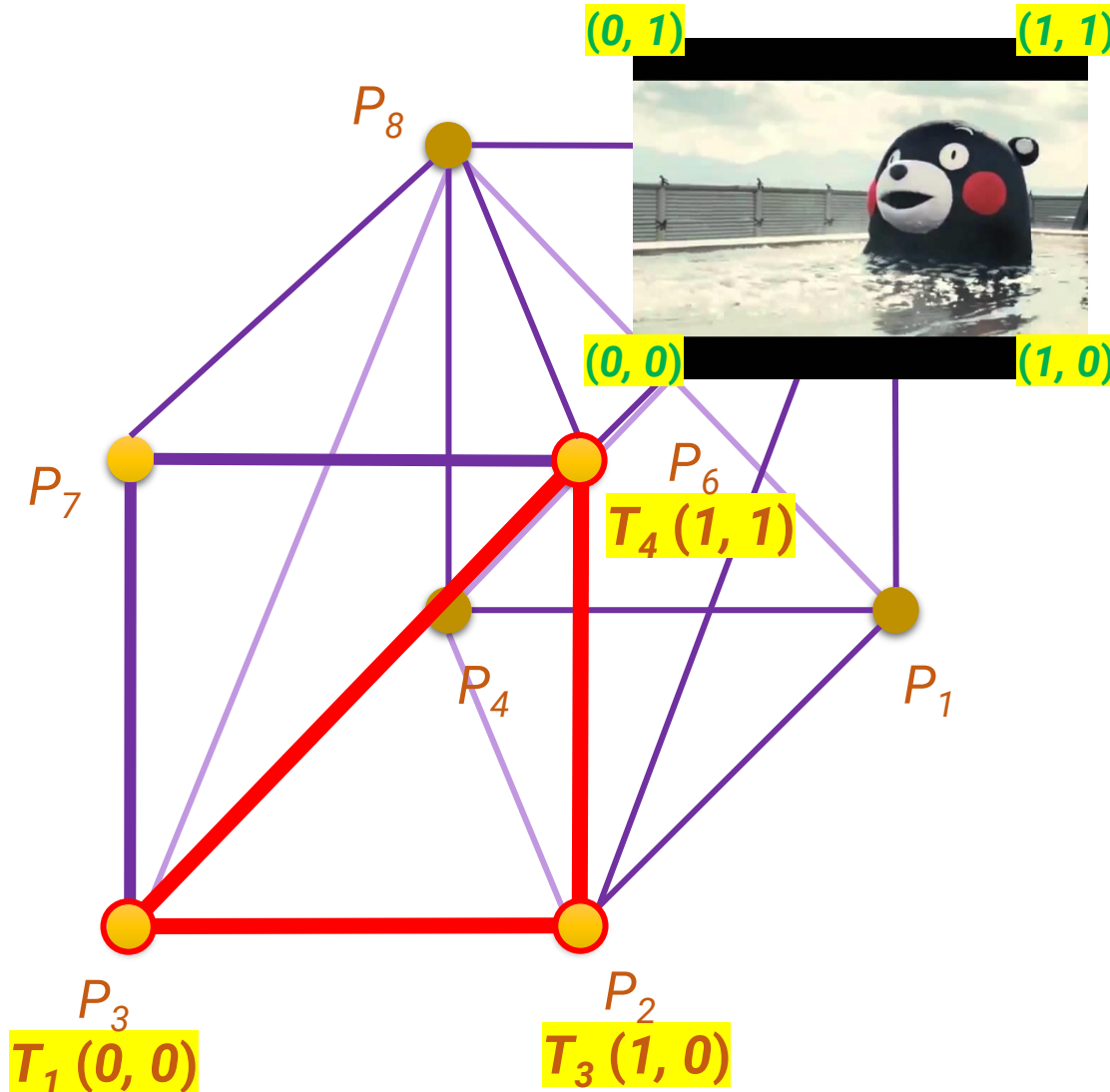
TexCube.mtl - 記事本
檔案(F) 編輯(E) 格式(O) 檢視
newmtl cubeMtl
Ns 30.0000
Ka 0.2 0.2 0.2
Kd 1 1 1
Ks 1 1 1
map_Kd kumamon.jpg
  
```



kumamon.jpg



Interpret the Texture Data



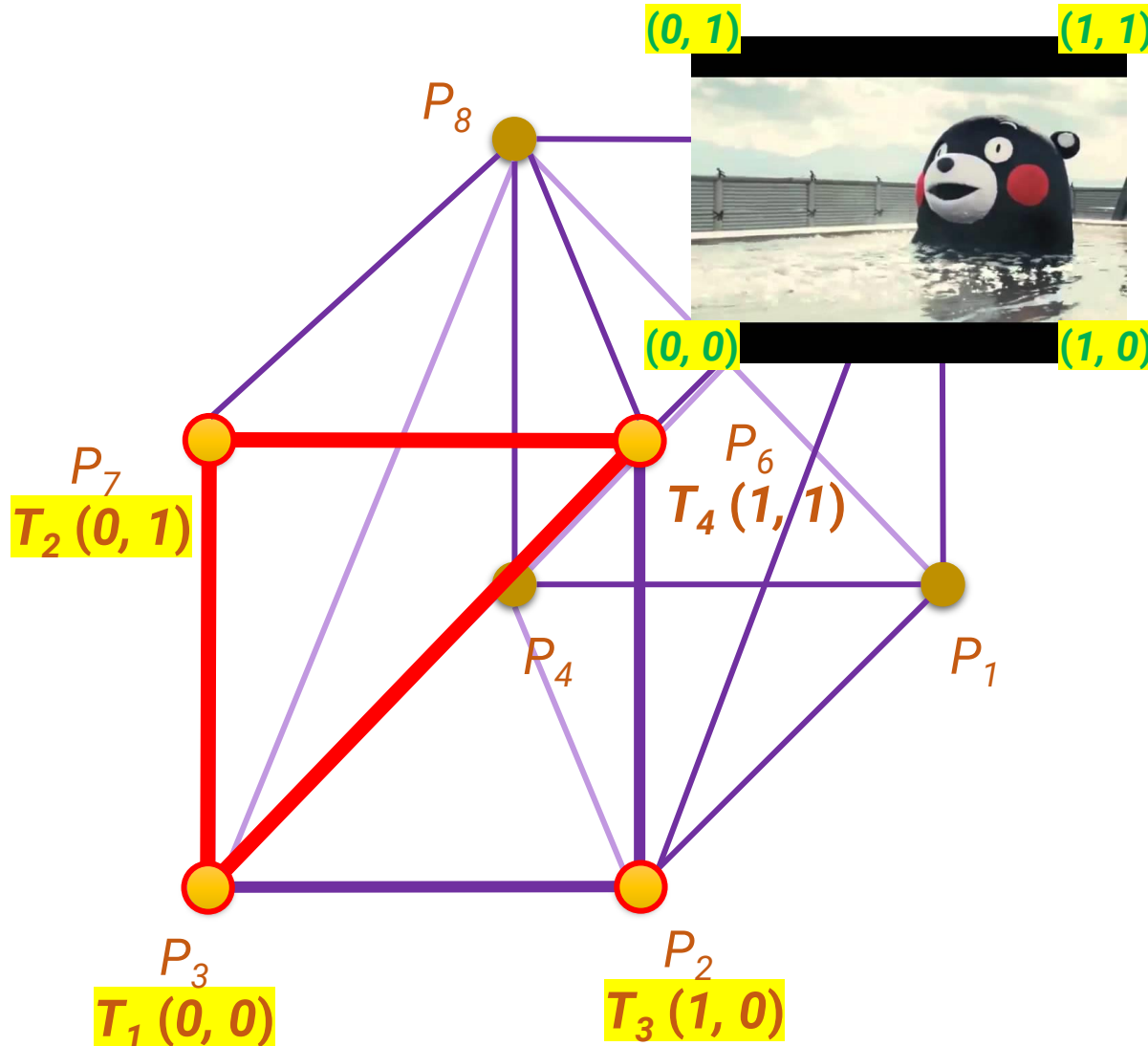
```
vt 0.0 0.0
vt 0.0 1.0
vt 1.0 0.0
vt 1.0 1.0
```

```
usemtl cubeMtl
f 8/2/2 7/1/2 6/3/2
f 5/4/2 8/2/2 6/3/2
f 2/4/1 3/2/1 4/1/1
f 1/3/1 2/4/1 4/1/1
f 2/3/4 6/4/4 3/1/4
f 6/4/4 7/2/4 3/1/4
f 5/4/3 6/2/3 2/1/3
f 1/3/3 5/4/3 2/1/3
f 3/3/5 7/4/5 8/2/5
f 4/1/5 3/3/5 8/2/5
f 5/2/6 1/1/6 8/4/6
f 1/1/6 4/3/6 8/4/6
```

vertex1 vertex2 vertex3
f P/T/N P/T/N P/T/N

P: index of vertex position
T: index of texture coordinate
N: index of vertex normal

Interpret the Texture Data (cont.)



```
vt 0.0 0.0
vt 0.0 1.0
vt 1.0 0.0
vt 1.0 1.0
```

```
usemtl cubeMtl
f 8/2/2 7/1/2 6/3/2
f 5/4/2 8/2/2 6/3/2
f 2/4/1 3/2/1 4/1/1
f 1/3/1 2/4/1 4/1/1
f 2/3/4 6/4/4 3/1/4
f 6/4/4 7/2/4 3/1/4
f 5/4/3 6/2/3 2/1/3
f 1/3/3 5/4/3 2/1/3
f 3/3/5 7/4/5 8/2/5
f 4/1/5 3/3/5 8/2/5
f 5/2/6 1/1/6 8/4/6
f 1/1/6 4/3/6 8/4/6
```

vertex1 vertex2 vertex3
f P/T/N P/T/N P/T/N

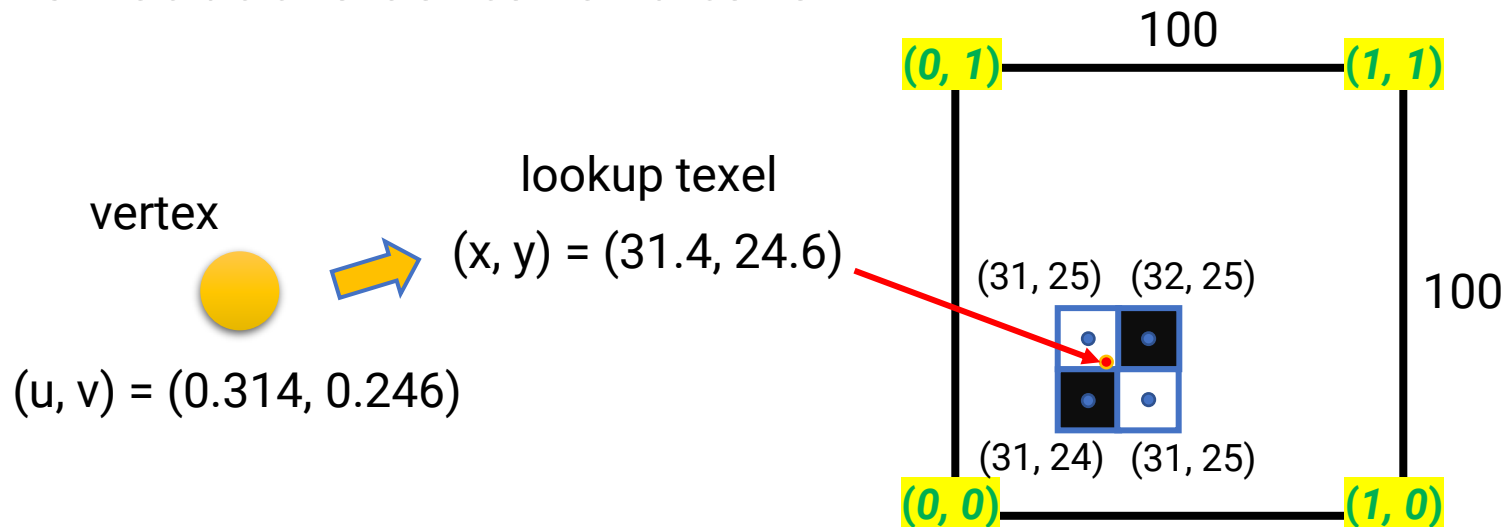
P: index of vertex position
T: index of texture coordinate
N: index of vertex normal

Outline

- Overview
- Texture data
- **Texture filtering**
- Applications
- OpenGL implementation

Texture Filtering

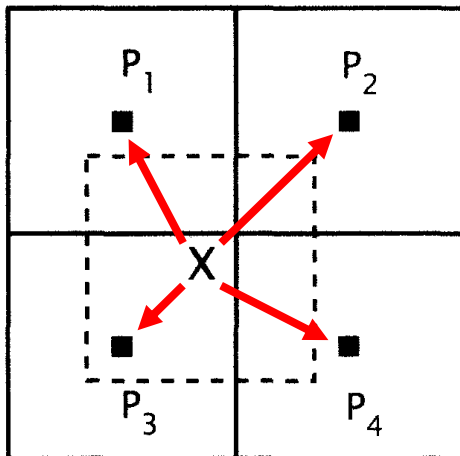
- Like an image, the content in a 2D texture is **discretely** represented by texels
- The texture coordinates can be **continuous** (especially after interpolation by the rasterization)
- How to determine the texture value if the lookup point is not at the center of a texel?



Texture Filtering (cont.)

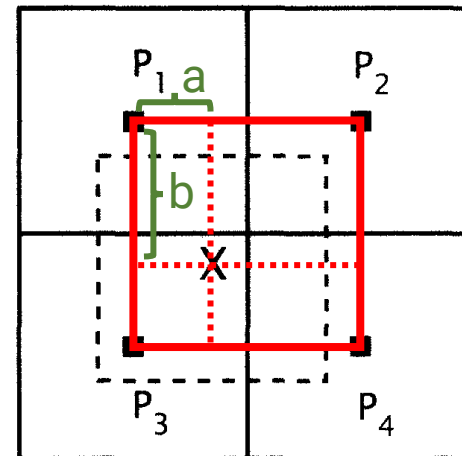
- **Strategies**

- **Nearest neighbor**
- **Bilinear interpolation**



nearest neighbor

P_3 is closest
Use P_3 's pixel value

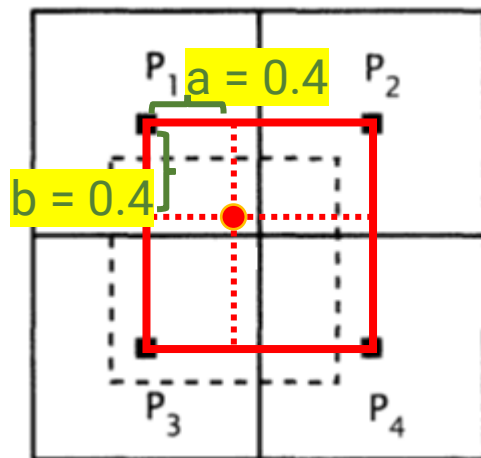


bilinear interpolation

$$(1-a)(1-b)P_1 + (a)(1-b)P_2 + (1-a)(b)P_3 + (a)(b)P_4$$

Texture Filtering (cont.)

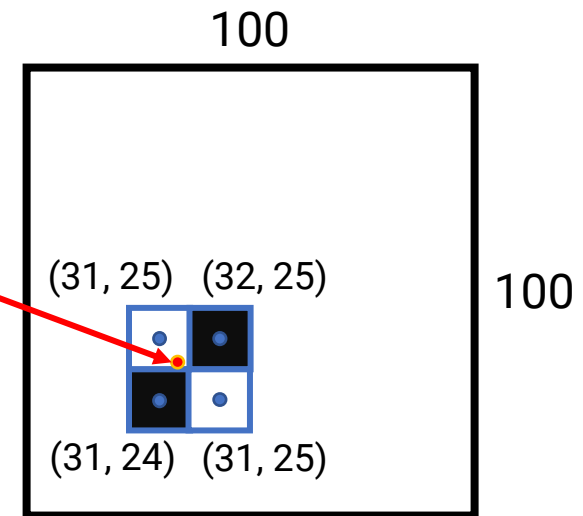
- Example



bilinear interpolation

$$(1-a)(1-b)P_1 + (a)(1-b)P_2 + (1-a)(b)P_3 + (a)(b)P_4$$

lookup texel
(x, y) = (31.4, 24.6)



nearest neighbor: use color of (31,25)

bilinear: compute

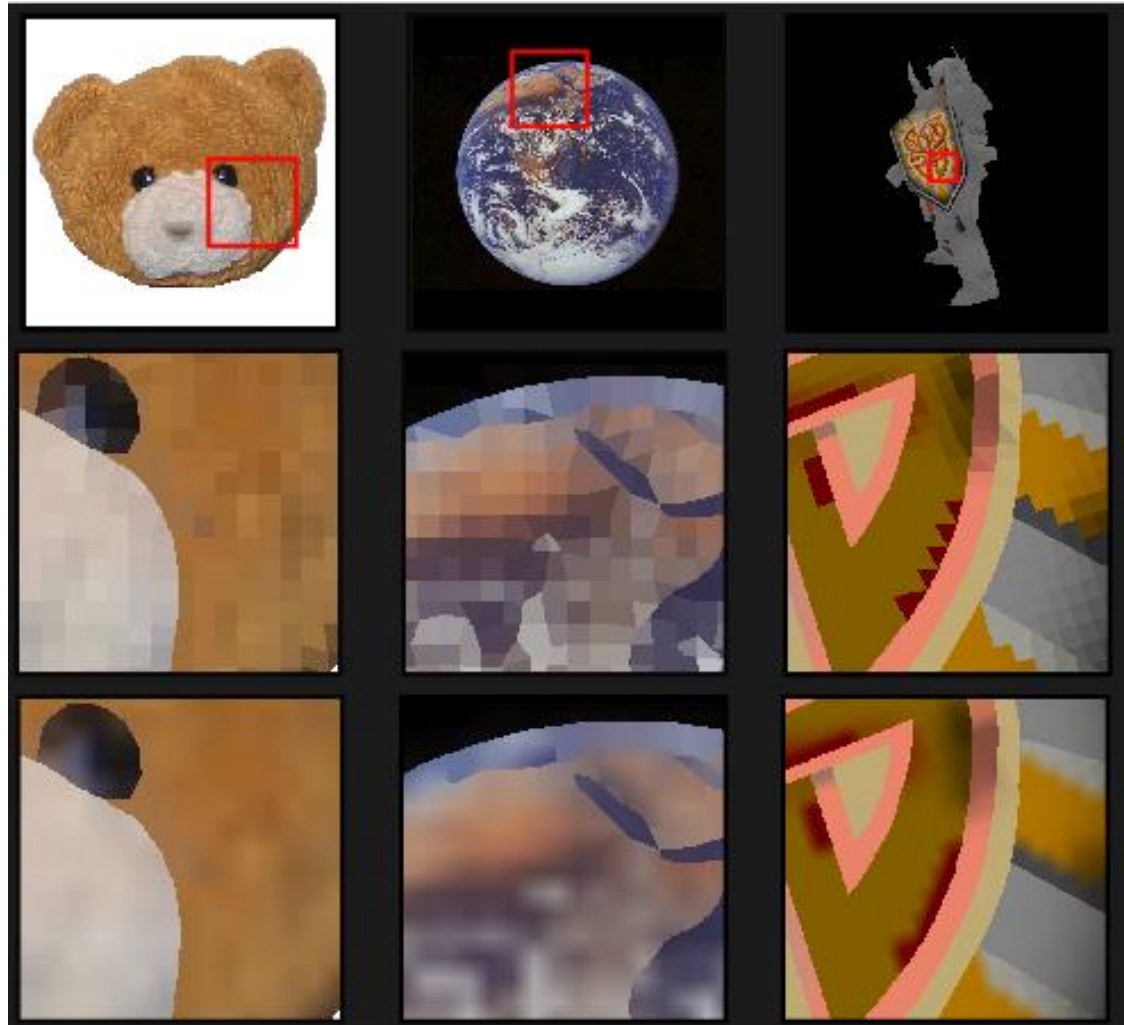
$$(1-a)(1-b)P_1 + (a)(1-b)P_2 + (1-a)(b)P_3 + (a)(b)P_4$$

0.36
0.24
0.24
0.16

Texture Filtering (cont.)

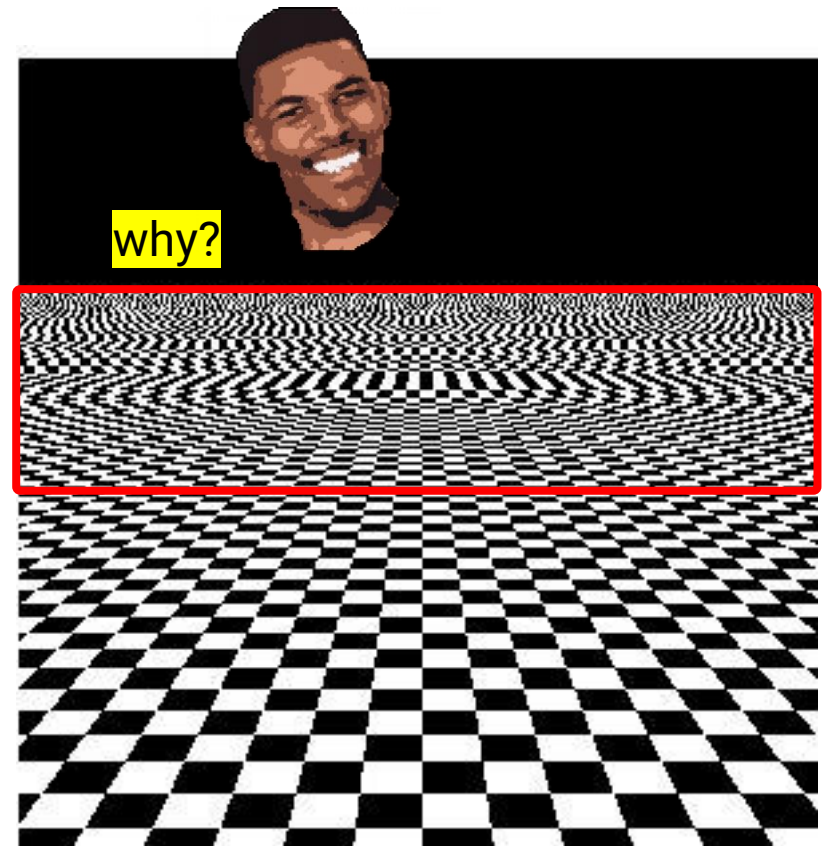
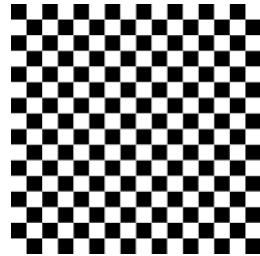
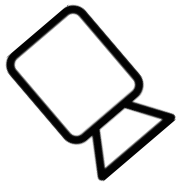
nearest
neighbor

bilinear
interpolation



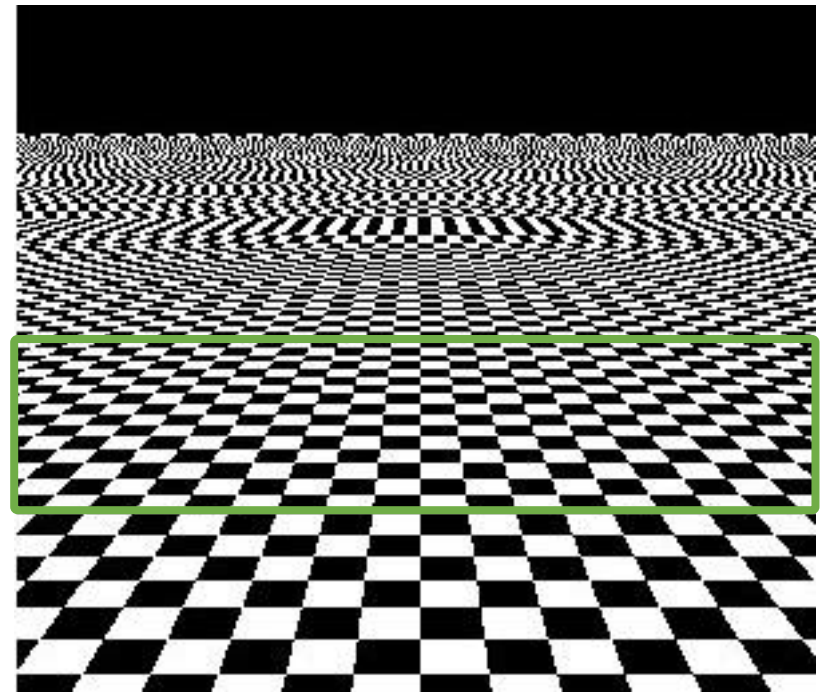
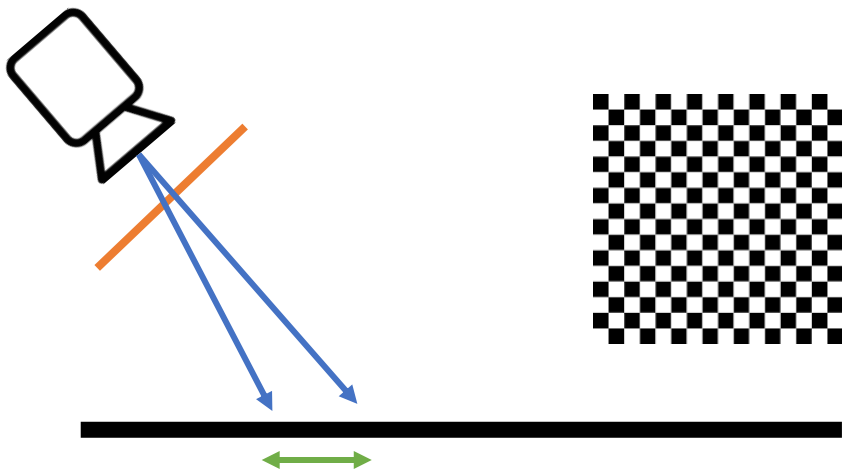
Problems with Texture Mapping

- Consider the following plane with a check-board pattern texture



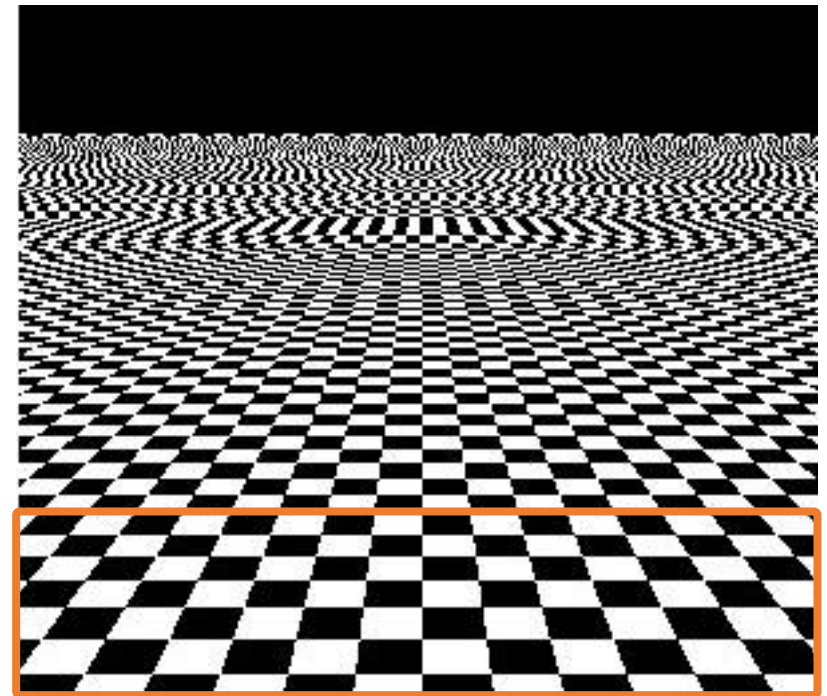
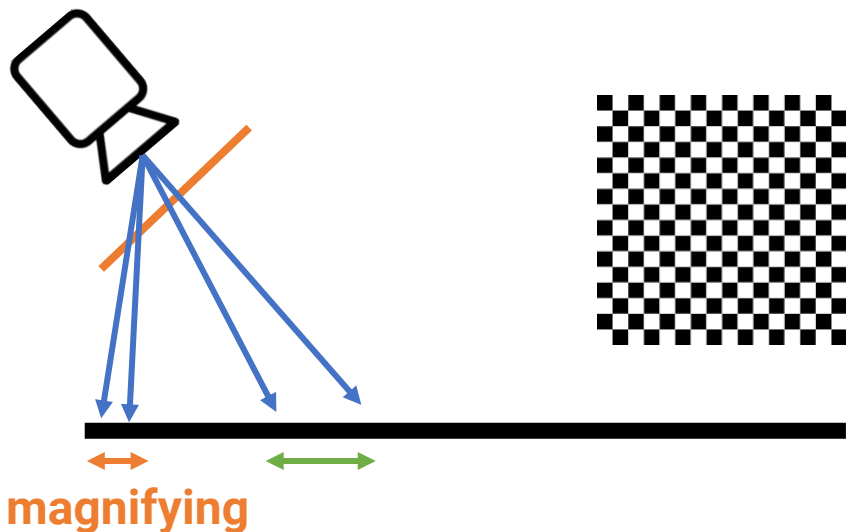
Texture Aliasing (cont.)

- Example
 - For the **green** area, one pixel covers a surface that is roughly one texel in the texture



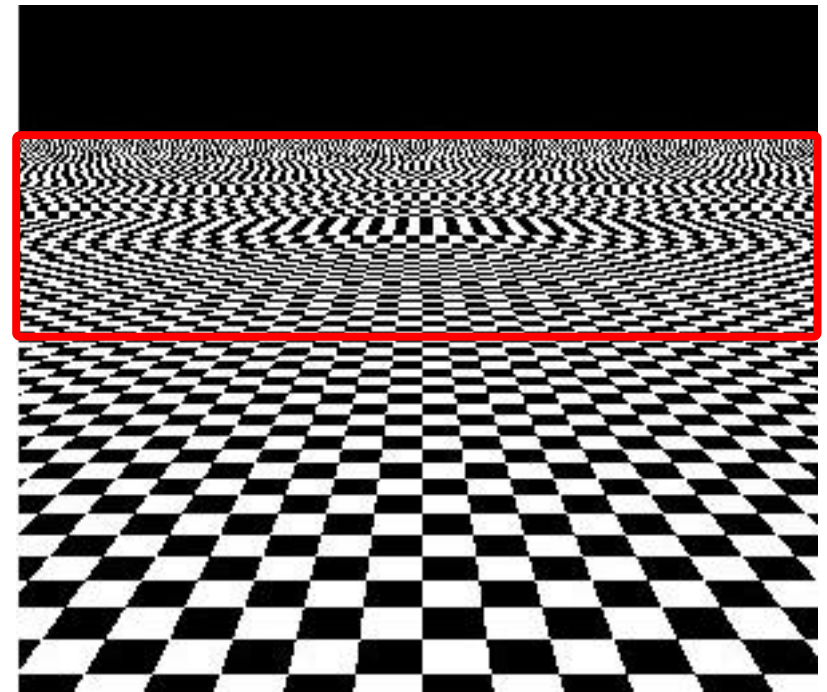
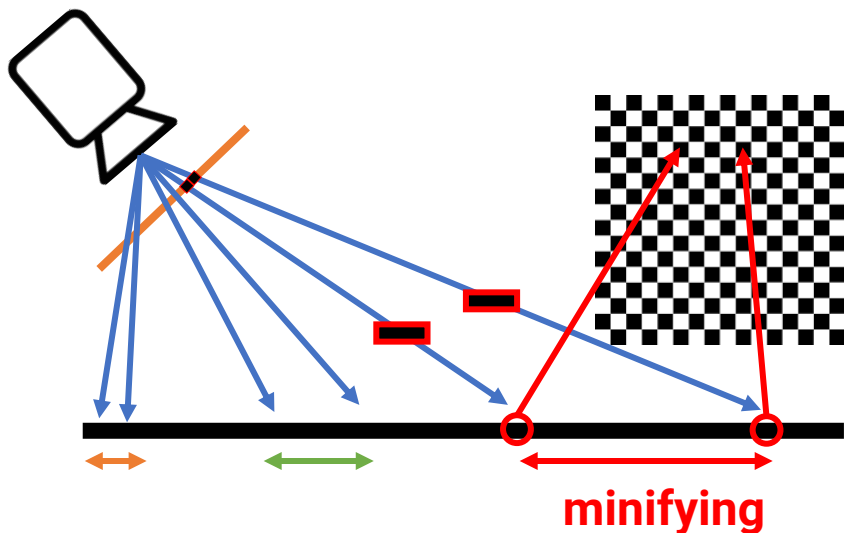
Texture Aliasing (cont.)

- Example
 - For the **orange** area, one pixel covers a surface that is **smaller** than one texel in the texture
 - Called **magnification**



Texture Aliasing (cont.)

- Example
 - For the **red** area, one pixel covers a surface that is **larger** than one texel in the texture
 - Called **minification**



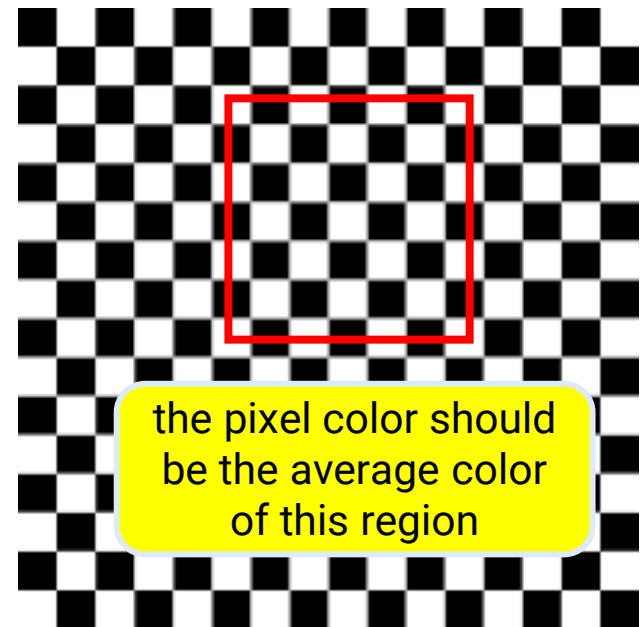
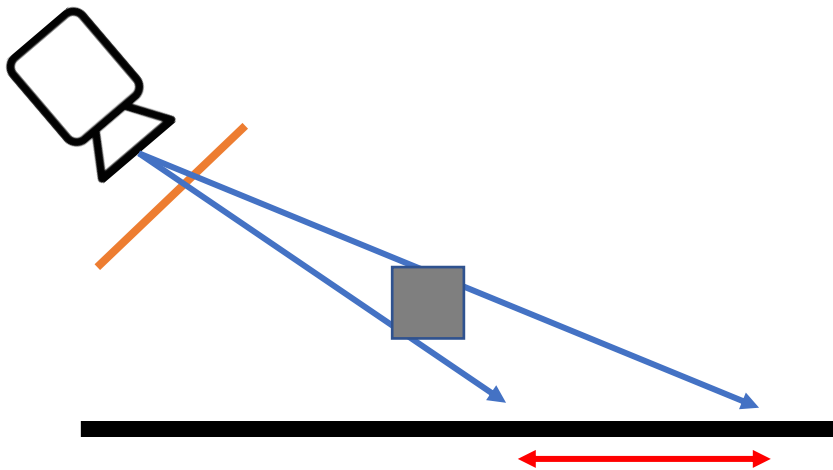
Texture Aliasing (cont.)

- Example
 - For the **red** area, one pixel covers a surface that is **larger** than one texel in the texture
 - Called **minification**
 - Might produce **flickering** for distant objects



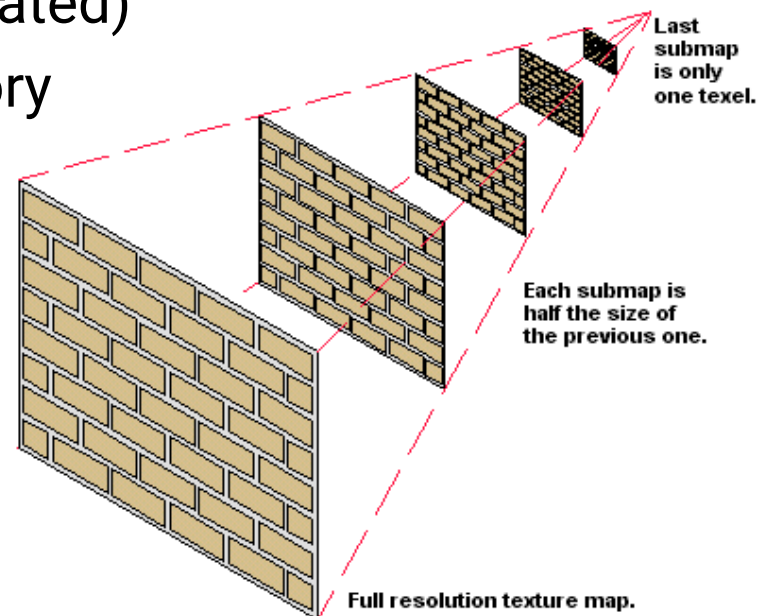
Mipmap

- To avoid aliasing, we should determine the regions a pixel covers (footprint) and average all the texture values inside the regions
- Time-consuming to do this in the run time!



Mipmap (cont.)

- Mipmap provides a clever way to solve this problem
- **Pre-process**
 - Build a **hierarchical representation** of the texture image
 - Each level has a half resolution of its previous level (generated by linearly interpolated)
 - Take at most **1/3** more memory



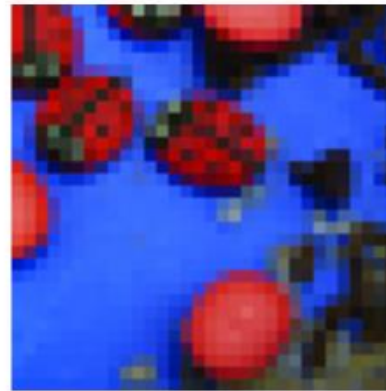
Mipmap (cont.)



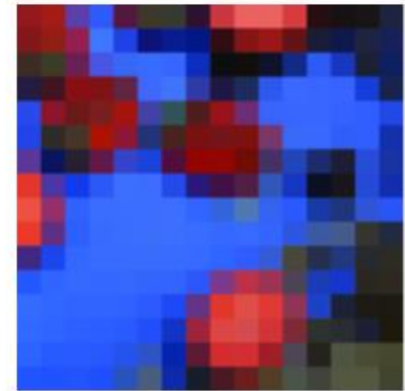
Level 0 = 128x128



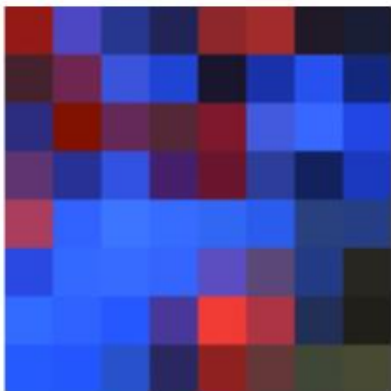
Level 1 = 64x64



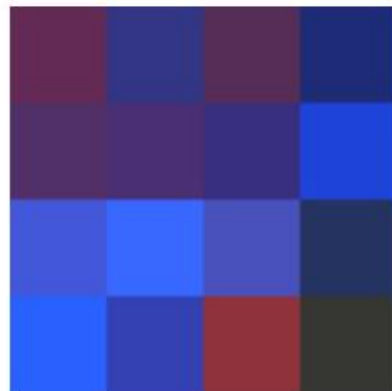
Level 2 = 32x32



Level 3 = 16x16



Level 4 = 8x8



Level 5 = 4x4



Level 6 = 2x2



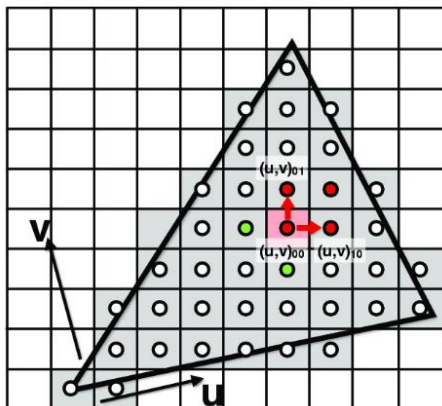
Level 7 = 1x1

Mipmap (cont.)

• Run-time lookup

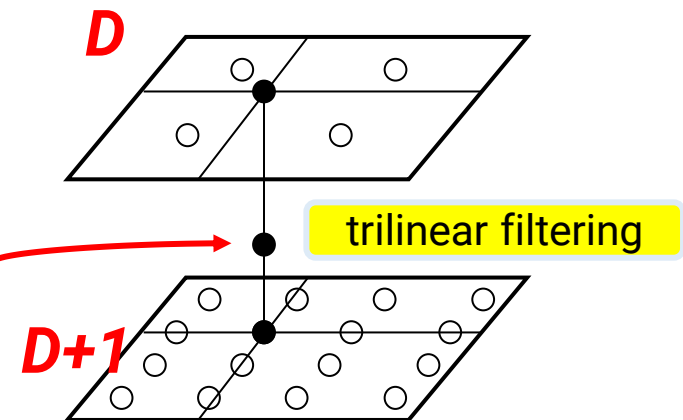
- Use **screen-space texture coordinate** to estimate its footprint in the texture space
- Choose two levels D and $D+1$ based on the footprint
- Perform linear interpolation at level D to obtain a value V_D
- Perform linear interpolation at level $D+1$ to obtain V_{D+1}
- Perform linear interpolation between V_D and V_{D+1}

trilinear

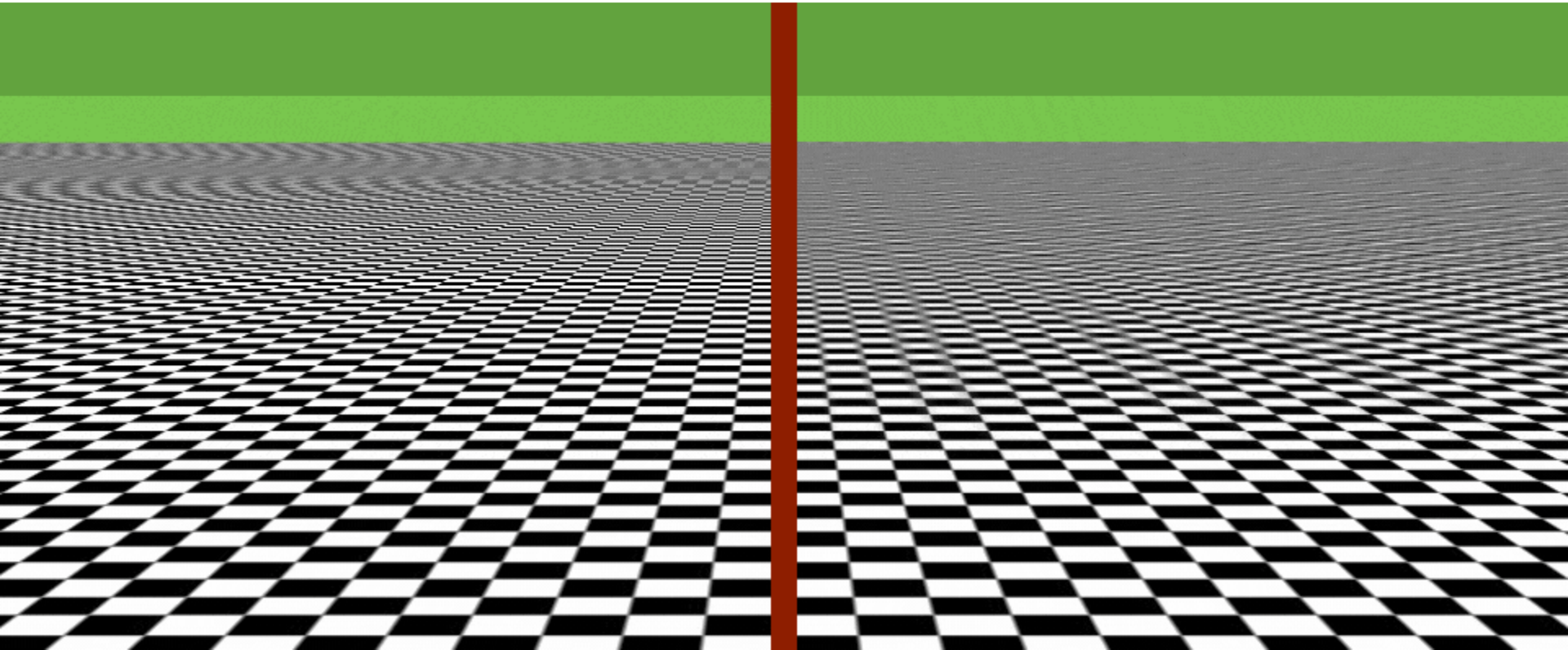


$$\frac{1}{W} = 2^{n-1-l}$$

$$l = n - 1 + \log w$$



Mipmap (cont.)



without mipmap

with mipmap

Mipmap (cont.)



Outline

- Overview
- Texture data
- Texture filtering
- **Applications**
- OpenGL implementation

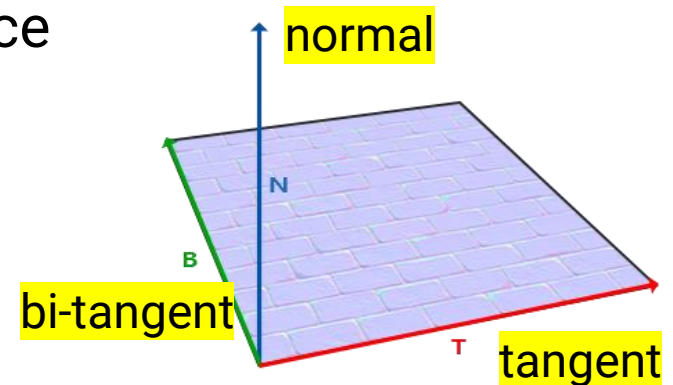
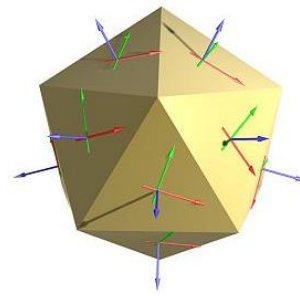
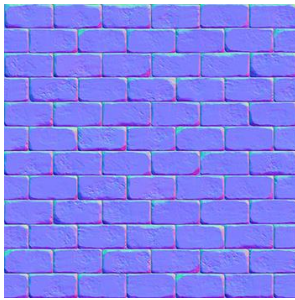
Normal Mapping

- Improve geometry details without adding vertices and triangles
 - Reduce the time of geometry processing
 - Only increase shading cost
 - Can also shorten the efforts of producing assets

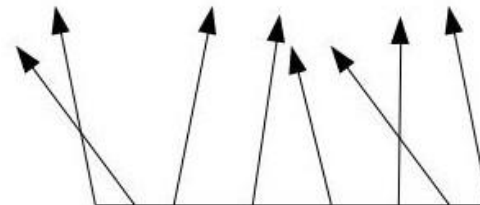
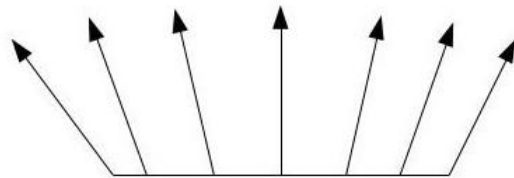


Normal Mapping (cont.)

- Encode normal as texture color
 - $(n_x, n_y, n_z) = \text{normalize}(2 * \text{TexColorRGB} - 1)$
 - The normal is defined in **TBN** space



- During rendering, use shading normal instead of geometry normal



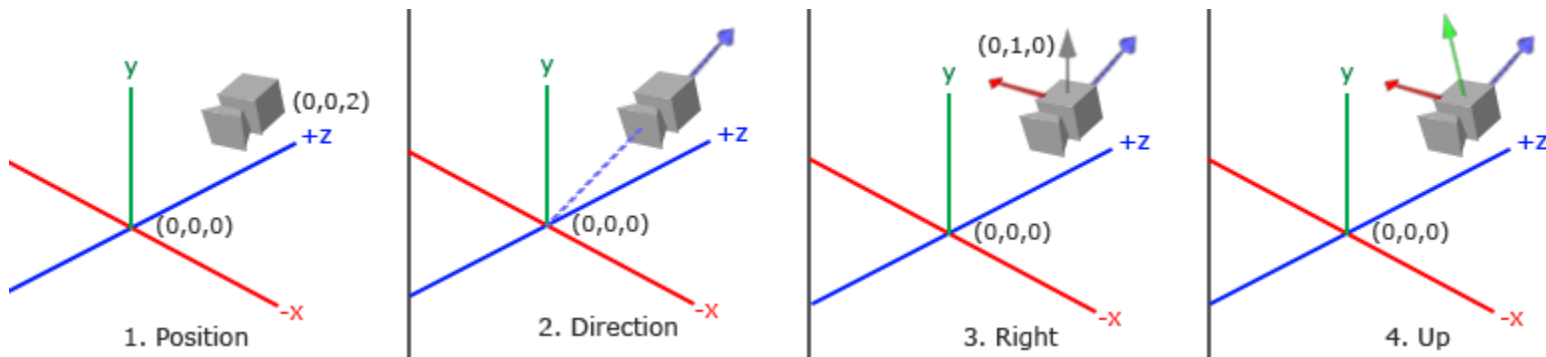
Normal Mapping (cont.)

- Recap: build camera matrix with viewing direction, right vector, and up vector

right vector	R_x	R_y	R_z	0	$\left[\begin{array}{cccc} 1 & 0 & 0 & -P_x \\ 0 & 1 & 0 & -P_y \\ 0 & 0 & 1 & -P_z \\ 0 & 0 & 0 & 1 \end{array} \right]$
up vector	U_x	U_y	U_z	0	
viewing vector	D_x	D_y	D_z	0	
	0	0	0	1	

rotation matrix

translation matrix



Normal Mapping (cont.)

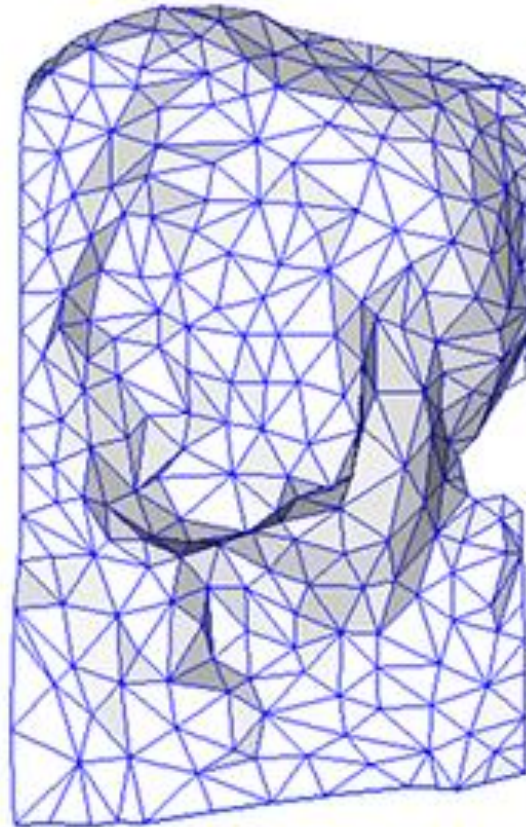
- Implementation
 - Calculate vertex tangent and bitangent as new vertex attributes
 - Calculate **per-face tangent** and **bi-tangent** and obtain **per-vertex tangent** and **bi-tangent** by averaging the face tangents of all adjacent faces
 - In the shader, build a **TBN** matrix and use it to transform the geometry normal

tangent vector	T_x	T_y	T_z
bi-tangent vector	B_x	B_y	B_z
normal vector	N_x	N_y	N_z

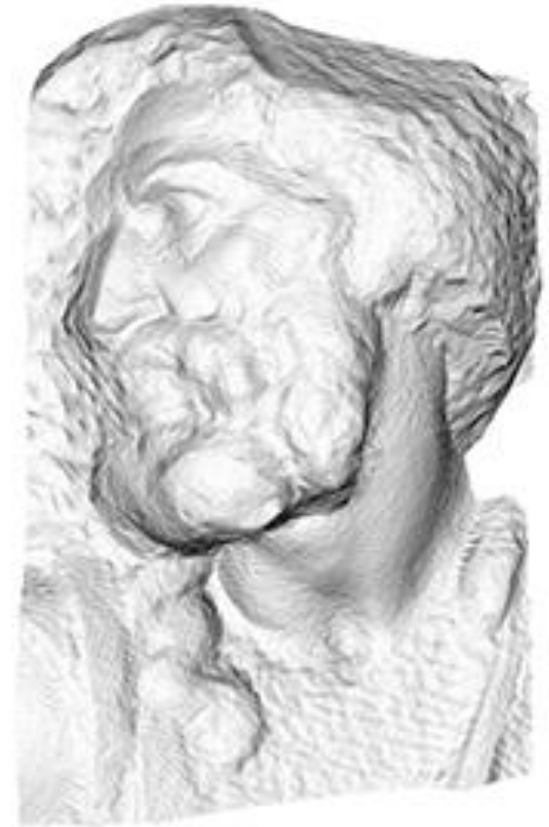
Normal Mapping (cont.)



original mesh
4M triangles



simplified mesh
500 triangles



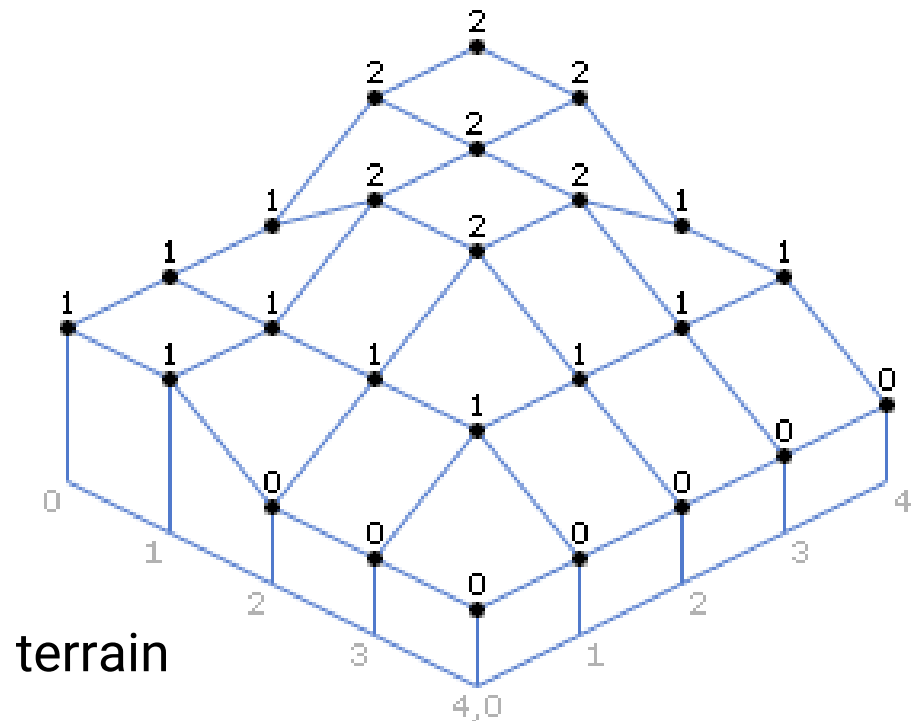
simplified mesh
and normal mapping
500 triangles

Height Map

- Use a scalar texture to represent the **vertex displacement** along the surface normal of a **base mesh**
- Widely used for **terrain** design

	0	1	2	3	4
0	1	1	1	2	2
1	1	1	2	2	2
2	0	1	2	2	1
3	0	1	1	1	1
4	0	0	0	0	0

heightmap

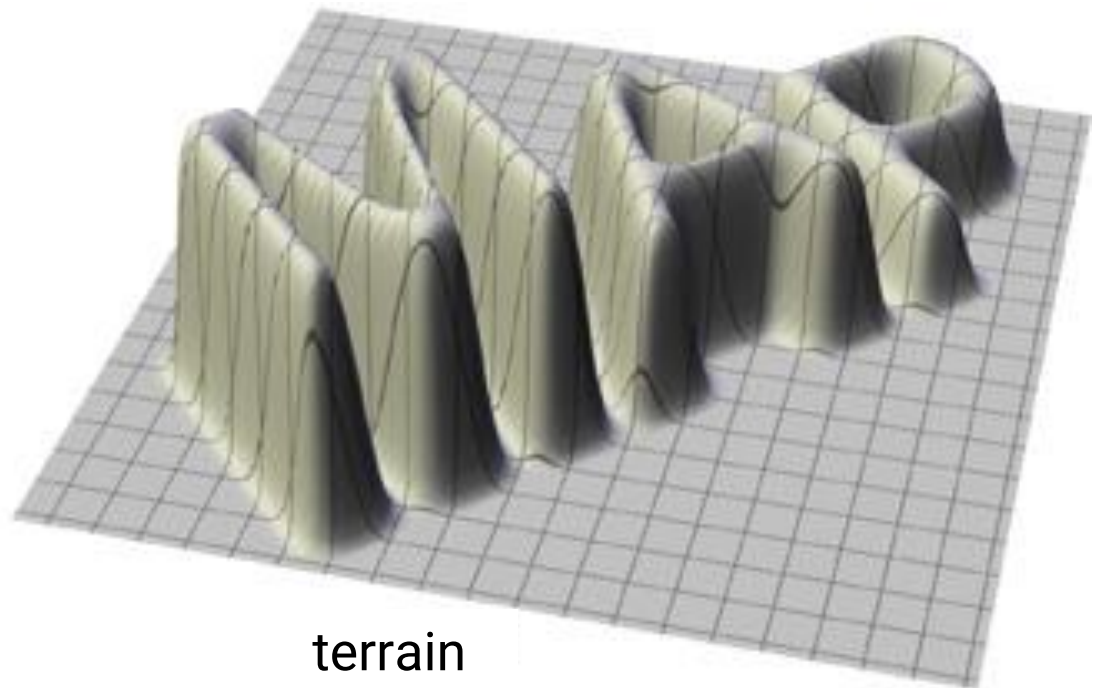


Height Map (cont.)

- Use a scalar texture to represent the **vertex displacement** along the surface normal of a **base mesh**
- Widely used for **terrain** design



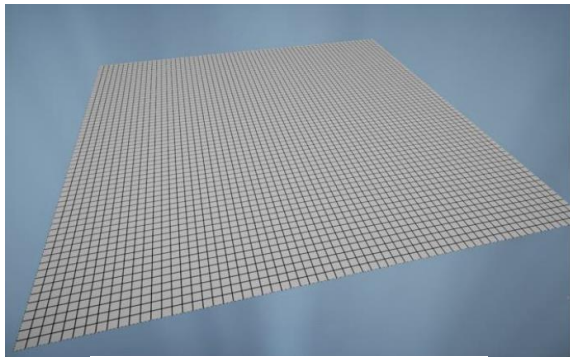
heightmap



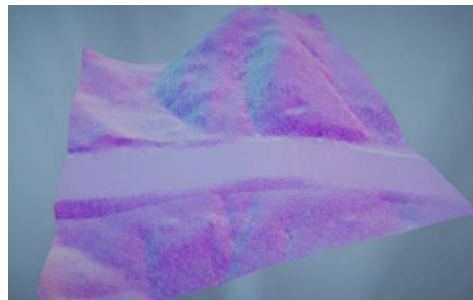
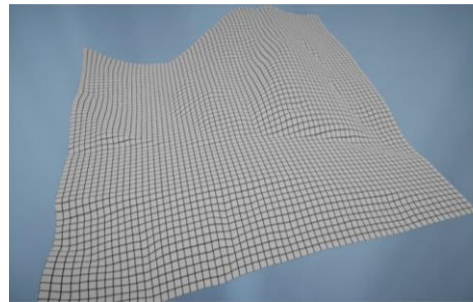
terrain

Height Map (cont.)

- Usually combined with an albedo texture and a normal map for shading



base mesh



rendered terrain

Height Map (cont.)

- Terrain management in *FarCry 5*



Height Map (cont.)

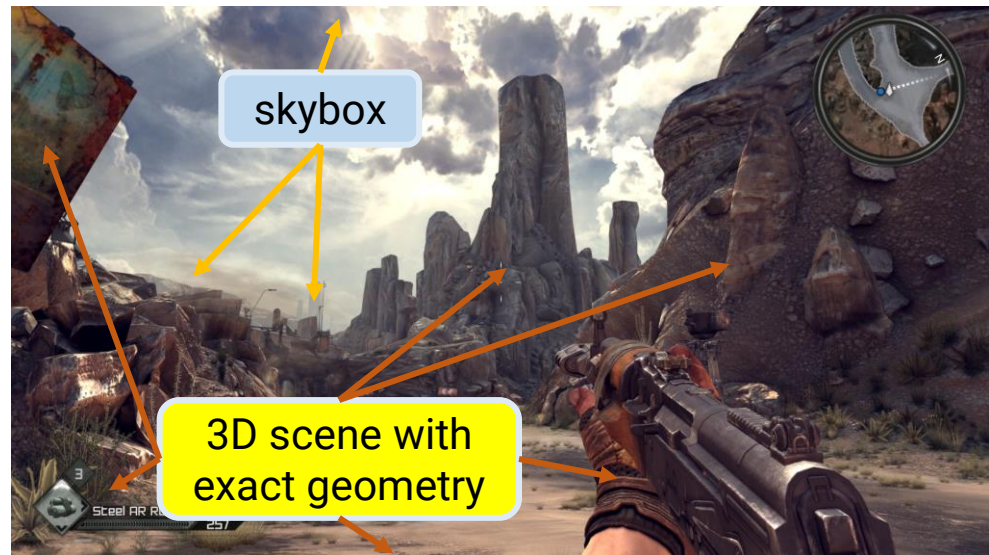
- Implementation
 - For each vertex in the base mesh, lookup the **height map** to displace the vertex (in the Vertex Shader)

*new vertex position = original vertex position + normal * height*

- For each fragment, lookup the **normal map** for the detailed shading normal and the **albedo texture** for the material property (in the Fragment Shader)

Skybox

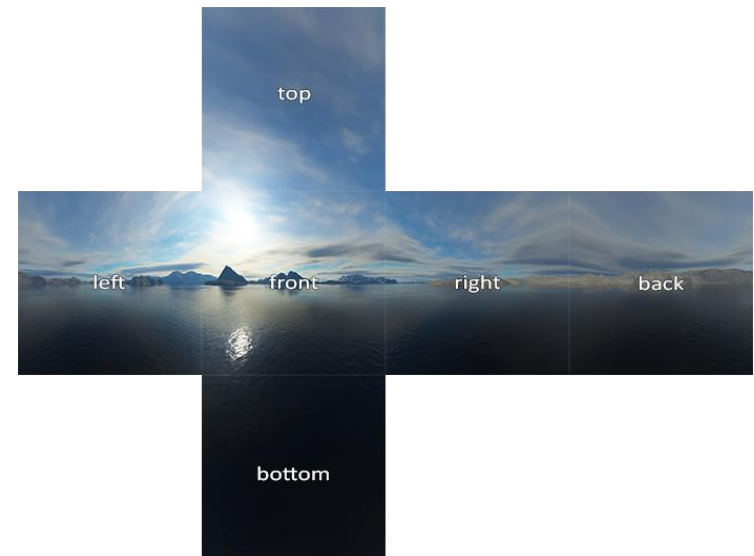
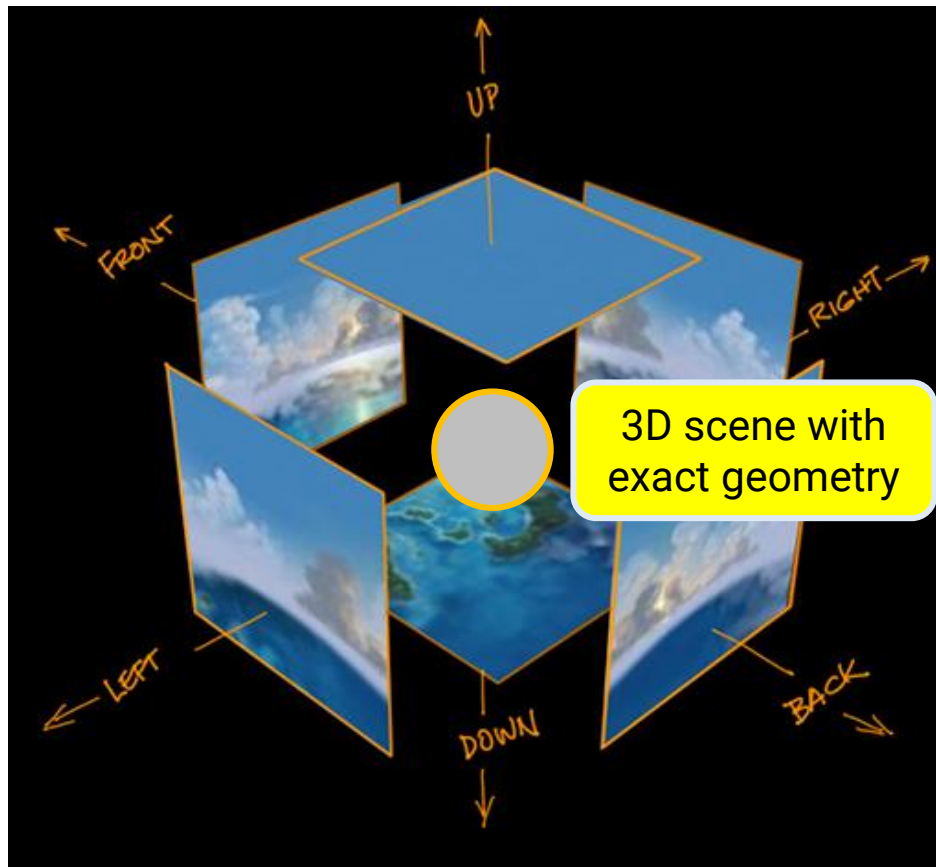
- Use a texture-mapped simple proxy geometry to represent far-away objects



- Two approaches
 - Cube + **cube map** texture
 - Sphere + **longitude-latitude** image

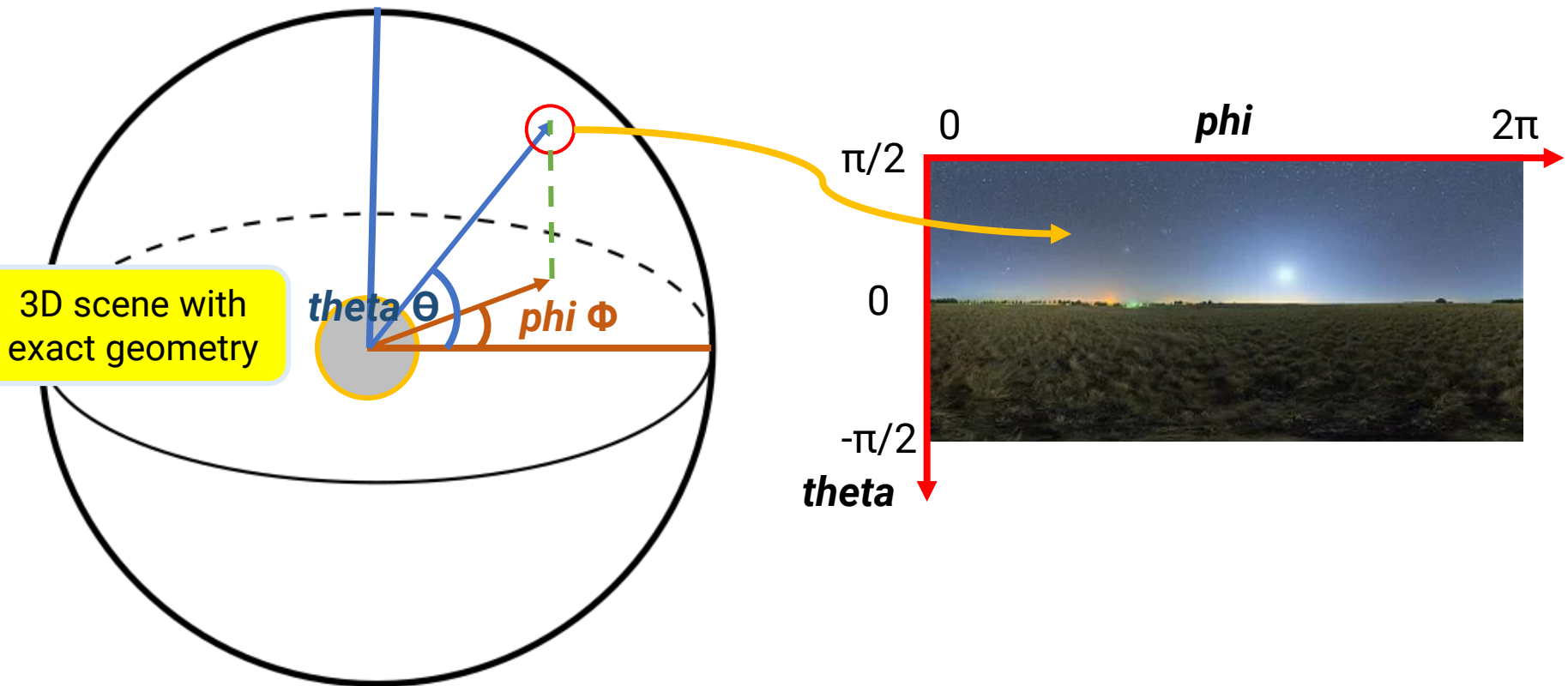
Skybox (cont.)

- Cube + **cube map** texture
 - Centered at world-space origin, with a significant long extent



Skybox (cont.)

- Sphere + **longitude-latitude** image
 - Centered at world-space origin, with a significant large radius



Reflection of the Skybox

- When rendering the scene, compute a reflected direction based on the viewing direction
- Use the reflected direction to lookup the skybox texture and obtain the reflected contribution
- Add the reflected contribution to the surface color



Reflection (cont.)



Ray Traced



Environment Map

