

Camera

Computer Graphics Yu-Ting Wu

(Some of this slides are borrowed from Prof. Yung-Yu Chuang)

Outline

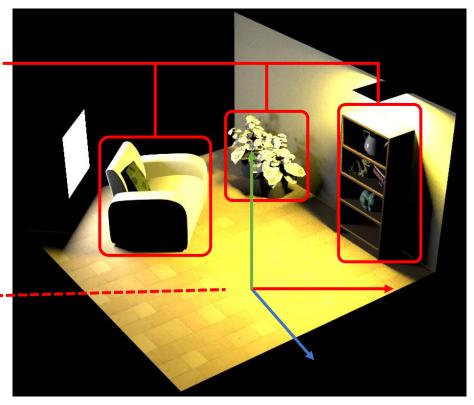
- Introduction to real-world cameras
- Introduction to computer graphics cameras
- Camera space and camera transformation
- Projective cameras
- OpenGL Implementation

Recap: 3D Scene Representation

 So far, we have introduced how to represent a virtual 3D world

Sofa, plant, bookshelf, and the room vertex data → (vertex buffer)
vertex adjacency → (index buffer)
defined in **Object Space**

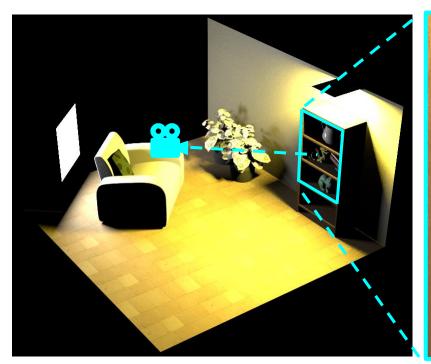
Objects are put into a shared World Space ------by transformation (translation, scaling, rotation)



3D virtual world

Recap: Virtual Camera and Rendering

 In computer graphics, we generate an image from a virtual 3D world using a virtual camera



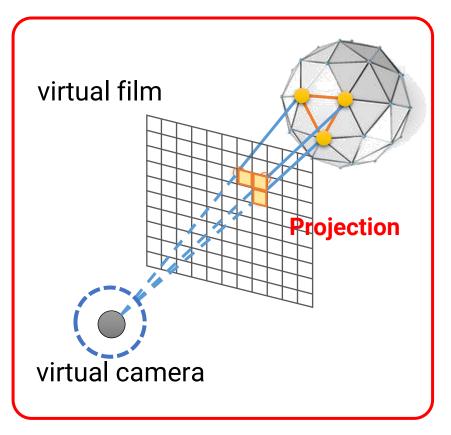
3D virtual world



rendered image

Recap: Rasterization and Projection

 OpenGL uses Rasterization to bring 3D shapes to the 2D screen

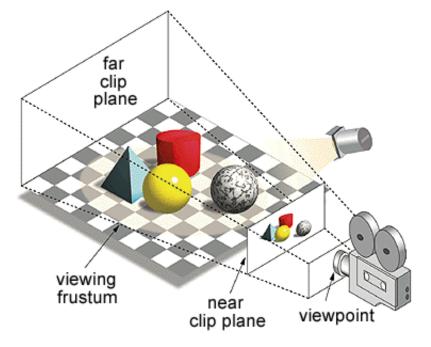


Where is the Camera and Projection?

 The typical flow of bringing a 3D point to the 2D screen involves the camera projection

 For now, we specify neither the camera nor the projection, so you can consider that we set the "projected" positions

of the vertices directly



Spoiler

- There are other spaces
- We will introduce camera space, clip space, and NDC today

for assisting

rendering

1. LOCAL SPACE

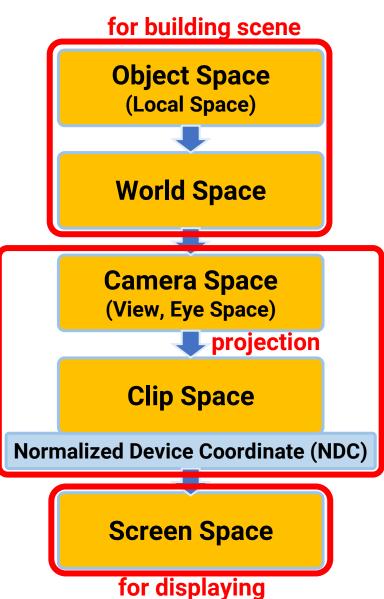
2. WORLD SPACE

VIEWPORT TRANSFORM

PROJECTION MATRIX

4. CLIP SPACE

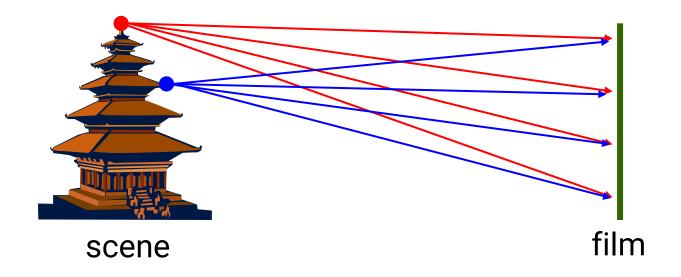
5. SCREEN SPACE



Outline

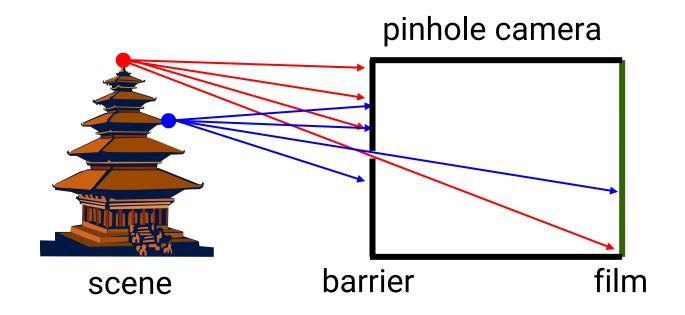
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Camera Trail



Put a piece of film in front of an object

Pinhole Camera

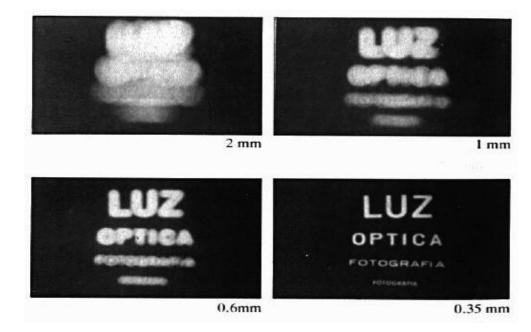


Add a barrier to block off most of the rays

- It reduces blurring
- The pinhole is known as the aperture
- The image is inverted

Pinhole Camera (cont.)

Shrink the aperture



Why not make the aperture as small as possible?

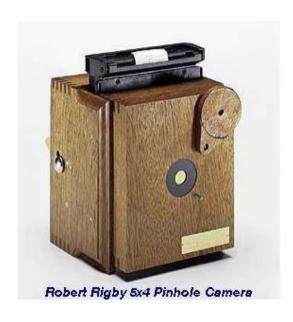
- Less light gets through
- Diffraction effect

Pinhole Camera (cont.)

Shrink the aperture



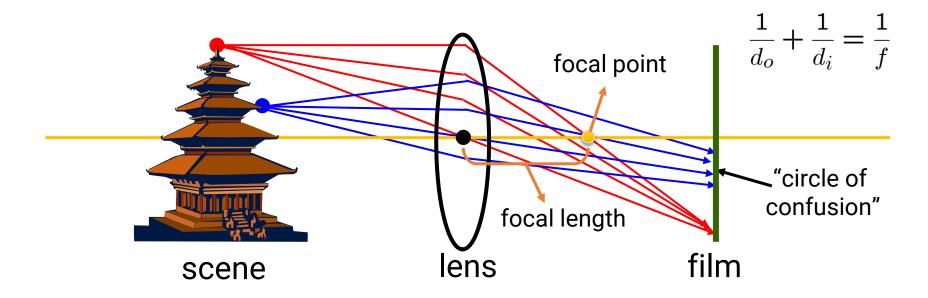
Pinhole Camera (cont.)



\$200~\$700



Camera with Lens



A lens focuses light onto the film

- There is a specific distance at which objects are "in focus"
- Other points project to a "circle of confusion" in the image Current digital cameras replace the film with a sensor array (CCD or CMOS)

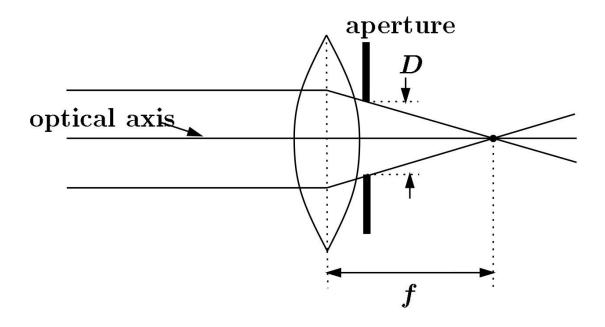
Camera with Lens



Depth of field due to circle of confusion

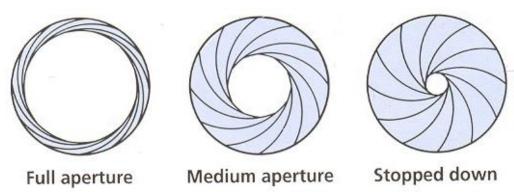
Exposure

- Exposure = aperture + shutter speed
 - Aperture of diameter **D** restricts the range of rays (aperture may be on either side of the lens)
 - Shutter speed is the amount of time that light is allowed to pass through the aperture

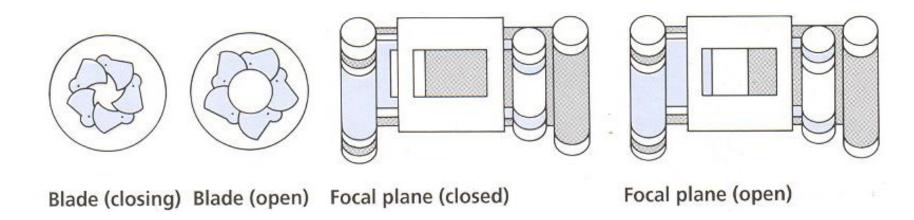


Exposure

Aperture (in f stop)

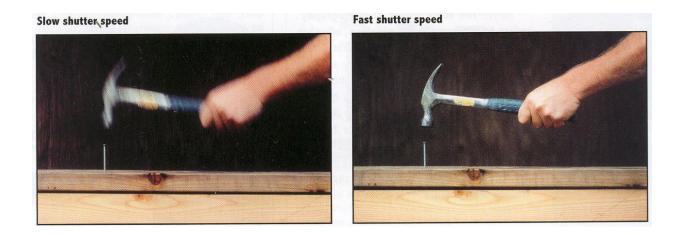


• Shutter speed (in fraction of a second)



Motion Blur and Depth of Field

Motion blur



Depth of field





1/2500 sec at f / 1.8

1/500 sec at f / 4.0

More About Real-World Cameras

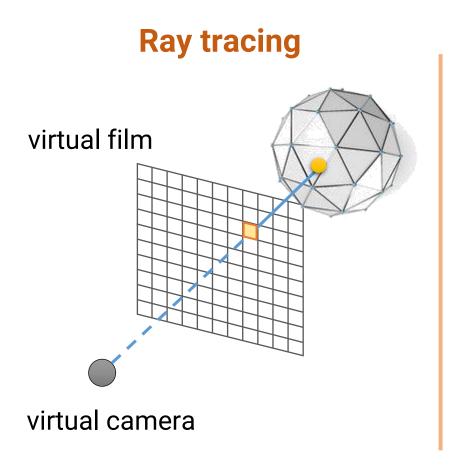
- For more details about real-world cameras, please refer to the recording of my course, "Multimedia Technology and Application"
 - Course material link:
 - Part 1: https://reurl.cc/GN1qNW
 - Part 2: https://reurl.cc/VW9Zm5
 - Part 3: https://reurl.cc/MzemM4

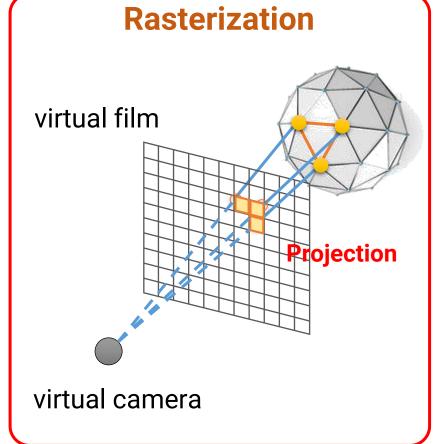
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Recap: Ways to Simulate Light Transport

Two ways for generating synthetic images



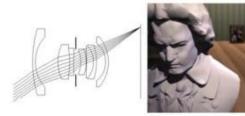


Computer Graphics Cameras

- Mimic the real-world functionalities of a real-world camera
- In offline (high-quality) graphics, we can simulate all the imaging processes of a camera using ray tracing







35 mm wide-angle



16 mm fisheye

Computer Graphics Cameras (cont.)

- Mimic the real-world functionalities of a real-world camera
- In offline (high-quality) graphics, we can simulate all the imaging processes of a camera using ray tracing
- · In interactive or real-time graphics, we usually use a pinhole camera for its simplicity of projection
- We can also dodge the drawbacks of real pinhole cameras

Avoid upside down images by putting the film in front of

the camera

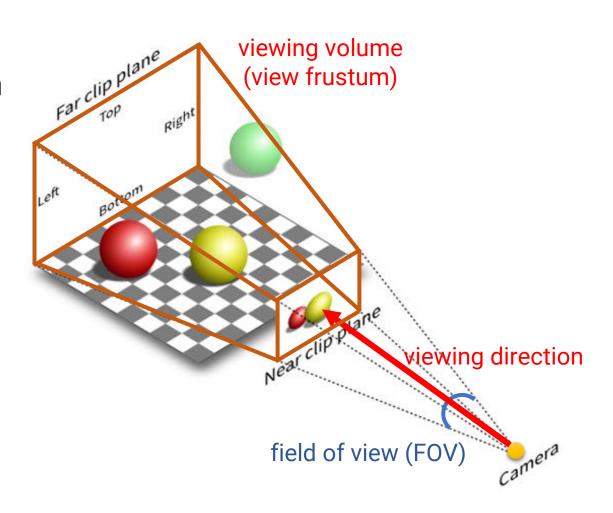
Computer Graphics Camera (cont.)

Every object will always be in focus



Camera Properties

- Camera position
- Viewing direction
- Field of view
 - In angle
- Aspect ratio
 - Width/Height
- View volume
 - Near clip plane
 - Far clip plane

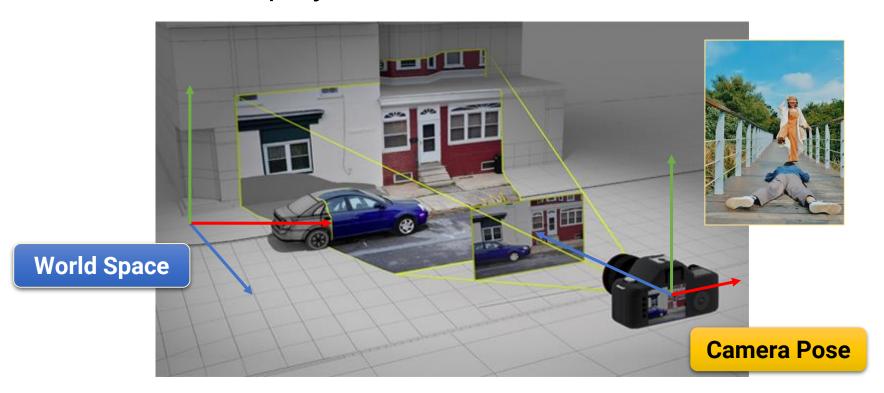


Outline

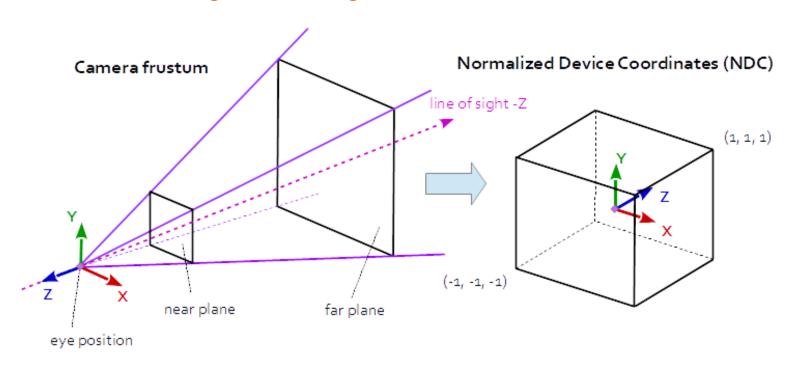
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Camera (View) Transform

- The camera can be at an arbitrary position and have an arbitrary viewing direction in the world space
- This makes the projection difficult in terms of mathematics



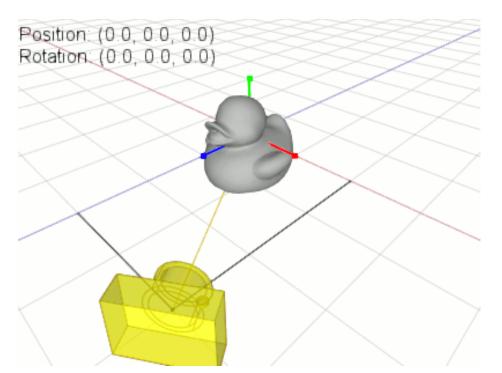
- To keep the math of projection simpler, we additionally define a camera (view, eye) space
 - In the camera space, the camera is at the origin (0, 0, 0) and looking at the negative Z-axis

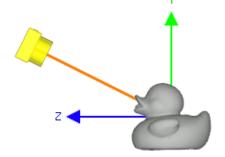


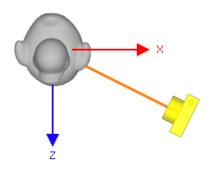
OpenGL itself is not familiar with the concept of a camera

Instead, we simulate one by moving all objects in the

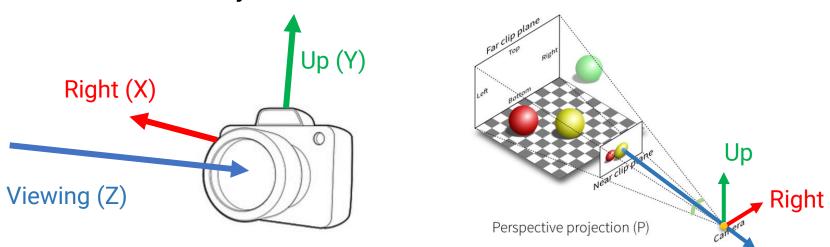
scene in the reverse direction







- For each object, we transform its world coordinate to the camera coordinate by
 - Moving it with the inverse translation of the camera's position
 - Rotate the object to match the camera's local frame



- Formed by the view direction (D), right (R), and up (U) vectors of the camera
- The three axes of the local frame should be orthogonal

- Set camera's local frame
 - However, it is usually difficult for a user to specify an orthogonal basis
 - OpenGL will do it for you (with the <u>Gram-Schmidt process</u>)

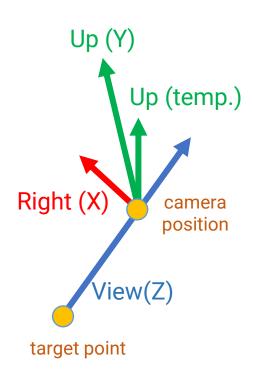
- Steps for setting camera's local frame
 - Determine the viewing dir. with the position of the camera and a target point

viewing direction = normalize(cameraPos - targetPos)

- Assume a temporal "up vector"
 - In most cases, we use the up direction (0, 1, 0) in the world frame
- Obtain the right vector by computing the cross product of the up vector and the viewing dir.

camera right = normalize(cross(up, viewing direction))

 Obtain the new up vector by computing the cross product of the viewing dir. and the right vector



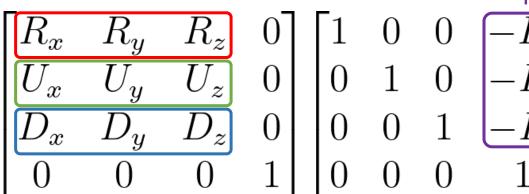
camera up = normalize(cross(viewing direction, camera right))

• Camera (view) transformation

 (P_x, P_y, P_z) is the camera's position

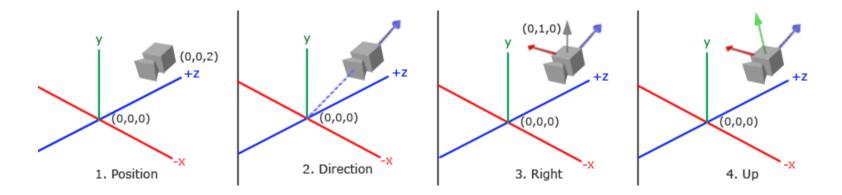
right vector (X) up vector (Y)

viewing vector (Z)



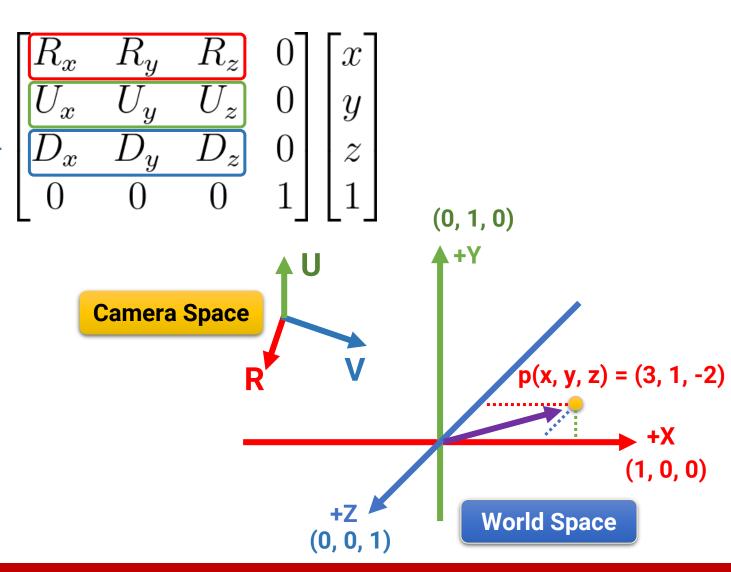
rotation matrix

translation matrix



right vector up vector

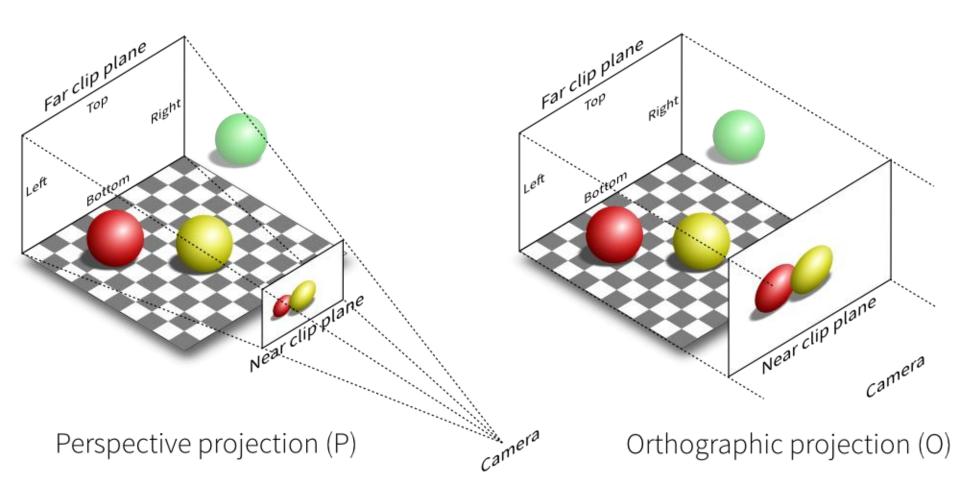
viewing vector



Outline

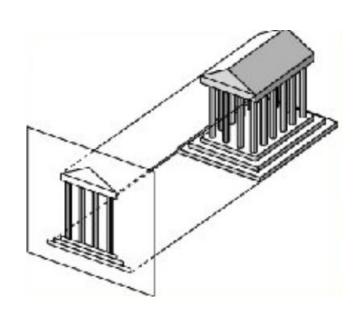
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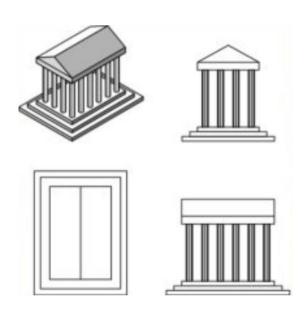
Projective Camera Models



Orthographic Projection

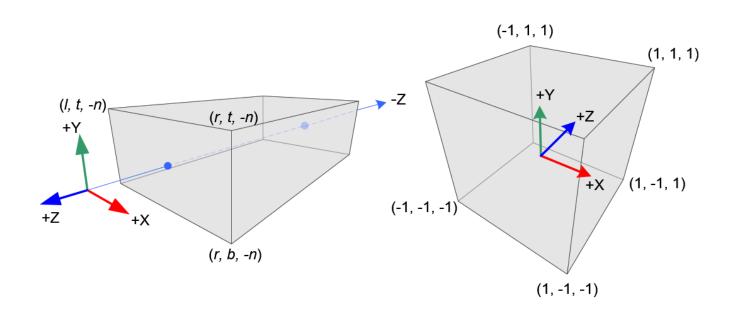
- Parallel projection with projectors perpendicular to the projection plane
- Preserve distance and angle
- Often used as front, side, and top views for 3D design





Orthographic Projection (cont.)

- Need to define the viewing volume with its six planes:
 left, right, top, bottom, near, and far
 - The viewing volume (frustum) is cube-like
- Map the xyz-coordinate to the range [-1, 1]



Orthographic Projection (cont.)

 Let the I, r, t, b, n, f be the boundaries of the left, right, top, bottom, near, and far planes



$$0 < x - l < r - l$$

$$0 \le \frac{x-l}{r-l} \le 1$$



$$0 \le \frac{x-l}{r-l} \le 1 \qquad \longrightarrow \qquad 0 \le 2(\frac{x-l}{r-l}) \le 2$$

$$\longrightarrow$$
 $-1 \le 2(\frac{x-l}{r-l}) - 1 \le 1$ \longrightarrow $-1 \le \frac{2x}{r-l} - \frac{r+l}{r-l} \le 1$

$$\leq \frac{2x}{r-l} - \frac{r+l}{r-l} \leq 1$$

Orthographic Projection (cont.)

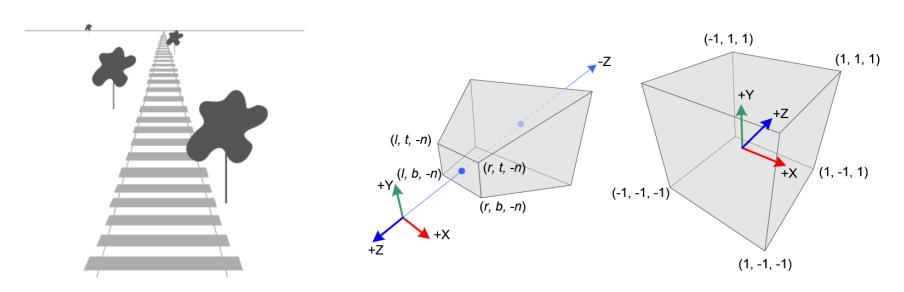
- Let the I, r, t, b, n, f be the boundaries of the left, right, top, bottom, near, and far planes
- An orthographic projection matrix can be written as

$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$-1 \le \frac{2x}{r-l} - \frac{r+l}{r-l} \le 1$$

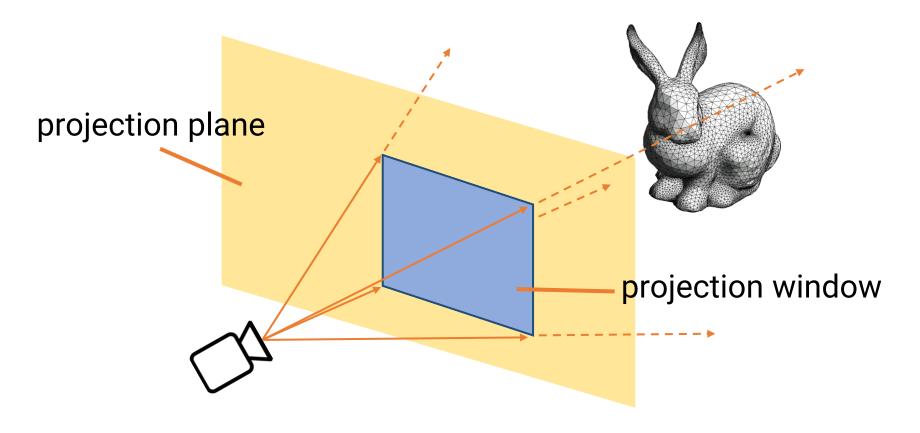
Perspective Projection

- In our real lives, the objects that are farther away appear much smaller
- This effect is called perspective
- A perspective projection tries to mimic the vision of human eyes

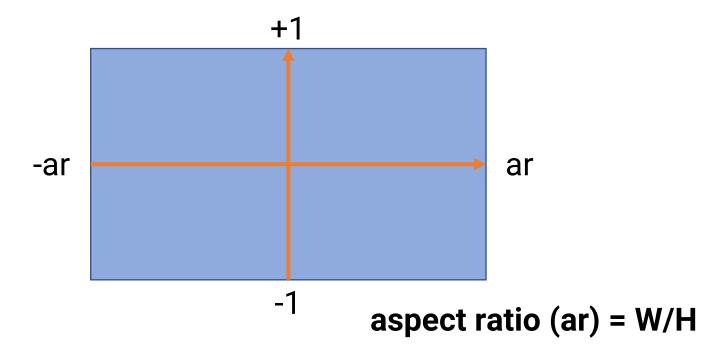


- Four components for the perspective projection matrix
 - The aspect ratio of the screen
 - The ratio between the width and the height (W/H)
 - The vertical field of view
 - The vertical angle of the camera through which we are looking at the world
 - The location of the near Z plane
 - Used to clip objects that are too close to the camera
 - The location of the far Z plane
 - Used to clip objects that are too distant from the camera

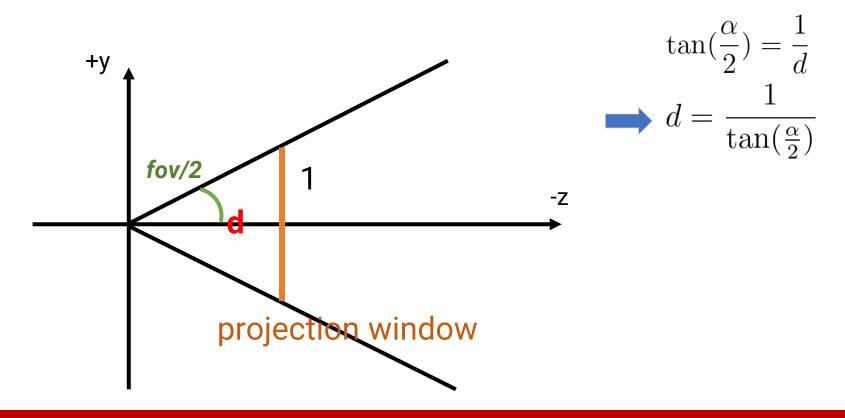
- Derivation of the perspective projection matrix
 - The projection plane and the projection window



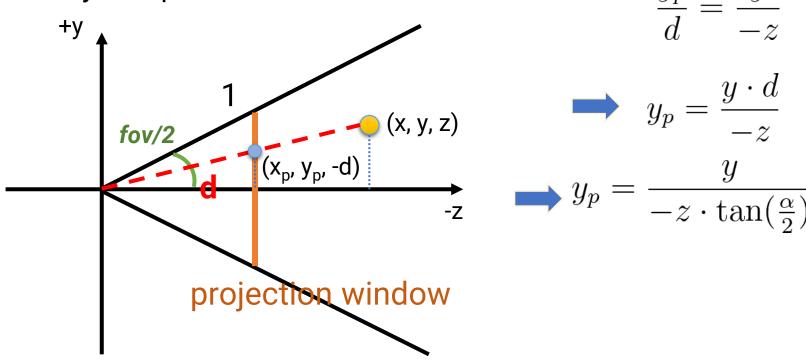
- Derivation of the perspective projection matrix
 - Determine the height of the projection window as 2
 - The width of the projection window becomes 2 times the aspect ratio (ar)



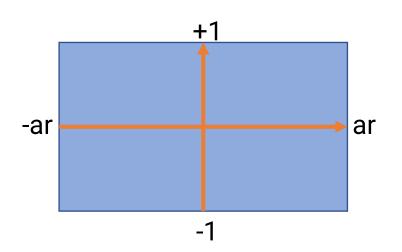
- Derivation of the perspective projection matrix
 - We can determine the distance from the camera to the projection window based on the field of view (fov)



- Derivation of the perspective projection matrix
 - Assume we want to find the projected coordinate (x_p, y_p) of a 3D point (x, y, z)
 - The y component can be derived as ...



- Derivation of the perspective projection matrix
 - Do the same derivation for the x component
 - Note in the x-direction we have to multiply the aspect ratio ar
 - After that, we can obtain the following equations



$$x_p = \frac{x}{ar \cdot (-z) \cdot \tan(\frac{\alpha}{2})}$$

$$y_p = \frac{y}{-z \cdot \tan(\frac{\alpha}{2})}$$

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$x_p = \frac{x}{ar \cdot (-z) \cdot \tan(\frac{\alpha}{2})} \qquad y_p = \frac{y}{-z \cdot \tan(\frac{\alpha}{2})}$$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} & & & & & & \\ & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$x_p = \frac{x}{ar \cdot (-z) \cdot \tan(\frac{\alpha}{2})}$$
 $y_p = \frac{y}{-z \cdot \tan(\frac{\alpha}{2})}$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ & & \mathbf{f(z)} & & \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions
 - Assume the Z function has a shape f(z) = A(-z) + B
 - After perspective division, it becomes

$$z_p = A - rac{B}{z}$$

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ w \end{bmatrix} = \begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ 0 & 0 & A & B \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$f(-nearZ) = -1 \implies A - \frac{B}{-nearZ} = -1 \implies A = -1 - \frac{B}{nearZ}$$

$$f(-farZ) = 1 \implies A - \frac{B}{-farZ} = 1 \implies A = 1 - \frac{B}{farZ}$$

$$2 = \frac{B}{farZ} - \frac{B}{nearZ}$$

$$\Rightarrow$$
 $B(nearZ - farZ) = 2 \cdot farZ \cdot farZ$

$$B = \frac{2 \cdot farZ \cdot farZ}{nearZ - farZ}$$

$$A = \frac{-nearZ - farZ}{nearZ - farZ}$$

- Derivation of the perspective projection matrix
 - Fill-in the matrix, based on the following conditions

$$\begin{bmatrix} x_p \\ y_p \\ z_p \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ 0 & 0 & \frac{-nearZ - farZ}{nearZ - farZ} & \frac{2 \cdot farZ \cdot nearZ}{nearZ - farZ} \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Camera Models Comparison

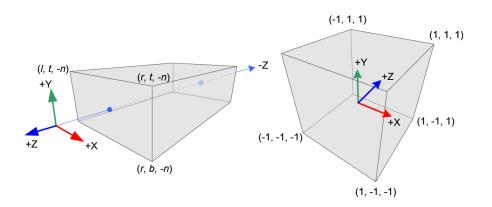




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Ortho Projection Matrix



$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

 glm::mat4x4 ortho(const float left, const float right, const float bottom, const float top, const float near, const float far)

```
glm::mat4x4 goP = glm::ortho(-5.0f, 5.0f, -5.0f, 5.0f, 0.01f, 100.0f);
```

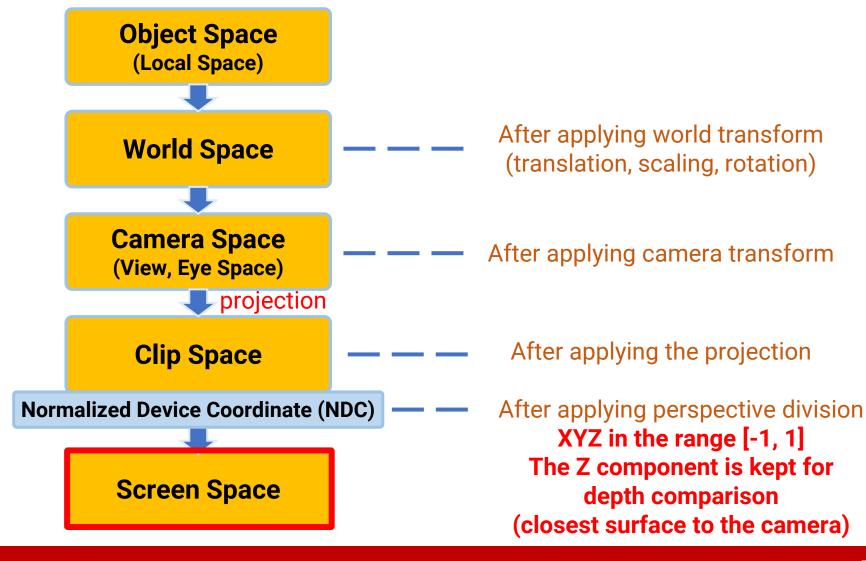
Perspective Projection Matrix

$$\begin{bmatrix} \frac{1}{ar \cdot \tan(\frac{\alpha}{2})} & 0 & 0 & 0 \\ 0 & \frac{1}{\tan(\frac{\alpha}{2})} & 0 & 0 \\ 0 & 0 & \frac{-nearZ - farZ}{nearZ - farZ} & \frac{2 \cdot farZ \cdot nearZ}{nearZ - farZ} \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

glm::mat4x4 perspective(const float fovy ,

glm::mat4x4 gP = glm::perspective(fovy, aspectRatio, nearZ, farZ);

The Full Vertex Transform Pipeline



Apply the Transformation on CPU

- To transform a vertex from object space to clip space, we multiply its position with the model-view-projection (MVP) matrix
- We can pre-multiply part of the matrix if some of them are fixed
 - For example, we can pre-multiply the camera (view) and the projection matrix to form a VP matrix, and change the model matrix to perform object animation
- Remember to do the perspective division

Apply the Transformation on CPU (cont.)

```
qlm::mat4x4 M = qlm::rotate(qlm::mat4x4(1.0f), qlm::radians(30.0f), qlm::vec3(0, 1, 0));
qlm::vec3 cameraPos = qlm::vec3(0.0f, 0.5f, 2.0f);
glm::vec3 cameraTarget = glm::vec3(0.0f, 0.0f, 0.0f);
qlm::vec3 cameraUp = qlm::vec3(0.0f, 1.0f, 0.0f);
qlm::mat4x4 V = qlm::lookAt(cameraPos, cameraTarget, cameraUp);
float fov = 40.0f;
float aspectRatio = (float)screenWidth / (float)screenHeight;
float zNear = 0.1f;
float zFar = 100.0f;
glm::mat4x4 P = glm::perspective(glm::radians(fov), aspectRatio, zNear, zFar);
qlm::mat4x4 MVP = P * V * M;
// Apply CPU transformation.
mesh->ApplyTransformCPU(MVP);
```

vertexPositions[i].z,

1.0f);

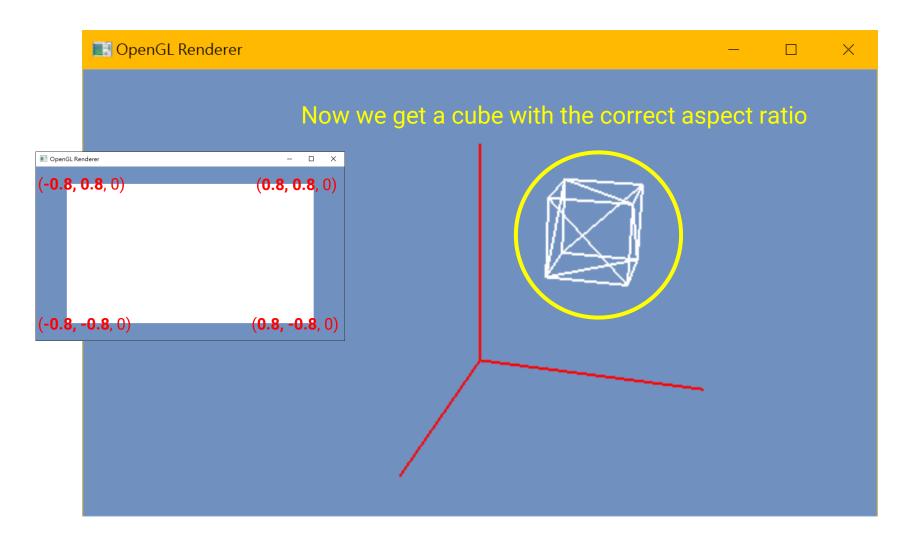
Apply the Transformation on CPU (cont.)

```
void ApplyTransformCPU(std::vector<glm::vec3>& vertexPositions, const glm::mat4x4& mvpMatrix)
   for (unsigned int i = 0 ; i < vertexPositions.size(); ++i) {</pre>
        glm::vec4 p = mvpMatrix * glm::vec4(vertexPositions[i], 1.0f);
        if (p.w \neq 0.0f) {
            float inv = 1.0f / p.w;
                                                   A useful coding technique available
           vertexPositions[i].x = p.x * inv;
                                                    in shader programming
           vertexPositions[i].y = p.y * inv;
           vertexPositions[i].z = p.z * inv;
                                                   It combines a 3d vector and a 1d
                                                    scalar to form a 4d vector
                       perspective division

    You can also write

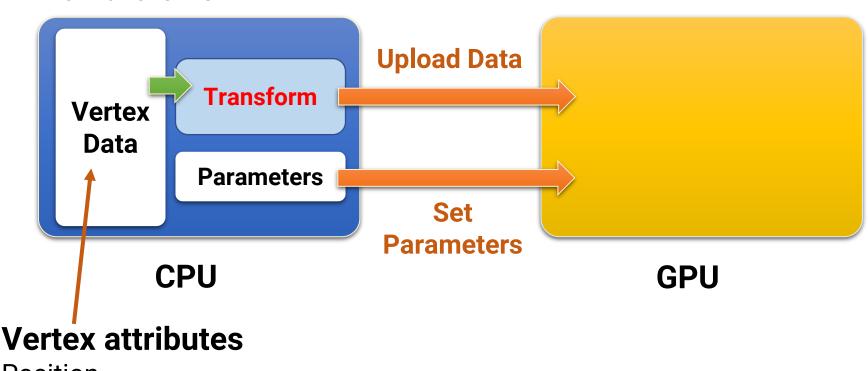
                                                     glm::vec4(vertexPositions[i].x,
                                                                vertexPositions[i].y,
```

Apply the Transformation on CPU (cont.)



Apply the Transformation on CPU

 So far, we have performed the transformation of vertices on the CPU



Position Normal

Texture coordinate

Apply the Transformation on GPU

- However, doing this job on CPU is not cost-effective
 - CPU is good at doing sequential, complex jobs
 - But vertex transform is simple and can be done in parallel
- Next class, we will introduce the GPU graphics pipeline and the vertex shaders for parallel processing

